# Windham School District



# Math K-8 Curriculum

Approved by the Windham School Board on 7/12/2022

## WINDHAM SCHOOL DISTRICT Math

### <u>TEAM</u>

All of the math teachers, K-12, participated in the mathematics curriculum by reading, writing, offering input, and editing the mathematics curriculum. This collaboration was extremely valuable.

A special thank you to the following teachers who also took time out of their summer vacation to help lead the mathematics curriculum review:

Jessica Benson	GBS	Sara Whitney	GBS
Judiann Burzlaff	GBS	Robert Hemmer	WCS
Jamie Carrier	GBS	Alex krishnamoorthy	WCS
Danielle Catabia	GBS	Jordan Lemay	WCS
Cindy Clemons	GBS	Ashley Clemons	WMS
Anne Connors	GBS	Jessica Cyr	WMS
Janet Dancy	GBS	Leah Doughty	WMS
Lisa lannuzzi	GBS	Cathy Croteau	WHS
Becky Schneider	GBS	Stephen Latvis	WHS
Doug Stahlheber	GBS	Amit Sharma	WHS
Erin Russell	GBS	Shannan McKenna	SAU

### **Mission Statement**

The Windham School District K-12 Mathematics Curriculum has undergone a formal review and revision during the 2021-2022 school year. Previously, the mathematics curriculum was approved in April 2018. Mathematics teachers, representing all grade levels, worked together to revise the math curriculum to ensure that it is a comprehensive math curriculum incorporating both the Common Core State Standards as well as Local Windham School District Standards. There was also a vertical review of core mastery standards to ensure that teachers are emphasizing the same key concepts through a spiral review format. This will help ensure that students are prepared for both state assessments as well as the following grade level or course.

There are three versions of the Windham K-12 Math Curriculum. By grade level or course, there is a summary overview section followed by a more detailed version of the curriculum. The summary overview section gives both parents and teachers a quick list of the concepts to be taught, which includes both vocabulary and skills that will be learned. The second detailed version of the curriculum also includes essential questions and the formal list of Common Core Standards. At the end of this document, there is also a mastery overview document. This document shows the concepts and skills, per grade level or course, that will be emphasized, reviewed, and assessed multiple times throughout the school year.

### <u>Title of Curriculum</u>: Kindergarten Mathematics

Unit Name	What (content, vocab)	Why (enduring understandings)	How (skills)
Place Value: Numbers and Operations in Base 10	<ul> <li>Numbers 11 to 19</li> <li>Vocabulary: how many more?</li> <li>Tens and ones</li> <li>Relationship between whole and parts</li> <li>Counting on</li> <li>10 can be added to another digit to make a whole number.</li> </ul>	<ul> <li>Numbers from 11-19 can be represented as the sum of 10 and some more.</li> <li>A pattern is a repetition of shapes, numbers, or any item selected. These patterns can be used to help solve problems.</li> </ul>	<ul> <li>Identify the value of a digit in a 2 digit number (11-19)</li> <li>Use ten frames to understand base ten</li> <li>Identify symbols +, -, and = in equations</li> <li>Count on from a number to find how many in all.</li> <li>Put parts together to find a whole and taking a whole apart to find parts.</li> </ul>
Operations and Algebraic Thinking: Addition and Subtraction	sentence, add, equal, equation, sum,	<ul> <li>Addition and subtraction can be shown in many different ways. These include putting together, taking apart, separating, and pattern building.</li> <li>Subtraction equations using - and = can be used to show subtraction situations.</li> <li>Equations using plus signs and equal signs can be used to show parts of a whole.</li> <li>The ability to solve problems is the heart of mathematics.</li> </ul>	<ul> <li>Demonstrate fluency of addition and subtraction facts (0 to 5).</li> </ul>
Counting and Cardinality: Counting and Ordering Numbers	<ul> <li>Numbers and counting 0 to 100</li> <li>The name and formation for each number 0 to 10.</li> <li>Counting begins with zero.</li> </ul>	<ul> <li>There is a unique symbol that goes with each number word.</li> <li>There is more than one way to show a number.</li> </ul>	<ul> <li>Count to find how many objects and write the number 0 to 20.</li> <li>Count to 100 by ones and tens.</li> <li>Counting forward from any given number to 100.</li> </ul>

	<ul> <li>Meaning of greater than, less than, and equal groups</li> <li>1:1 correspondence when counting</li> </ul>	<ul> <li>There is a specific order to the set of whole numbers.</li> <li>Zero is a number that tells how many objects there are when there are none.</li> <li>Counting tells the total number in a group no matter which order the objects are counted.</li> <li>Two groups of objects are equal if they can be directly matched, one-to-one, with no extras in either group.</li> </ul>	<ul> <li>Identify and compare numbers, between 1 and 10, in terms of greater than, less than or equal.</li> </ul>
Geometry	<ul> <li>Two-dimensional shapes (squares, circles, triangles, rectangles, and hexagons)</li> <li>Three-dimensional shapes (cubes, cones, cylinders, and spheres)</li> <li>Describe position of objects using above, below, beside, in front of, behind, next to.</li> <li>Objects can be described, classified, analyzed, compared, and created by their attributes.</li> </ul>	<ul> <li>Shapes are everywhere in our world.</li> <li>Objects can be classified into two categories, based on whether they have or do not have particular attributes.</li> </ul>	<ul> <li>Describe objects using names of shapes.</li> <li>Identify two and three-dimensional shapes.</li> <li>Name shapes using attributes.</li> <li>Analyze and compare two- and three-dimensional shapes, in different sizes and orientations, using informal language to describe their similarities, differences, parts (e.g. number of sides and vertices) and other attributes (e.g. having sides of equal length).</li> <li>Construct shapes using various materials.</li> <li>Describe relative position of objects using positional words.</li> <li>Name shapes regardless of their overall size or orientation.</li> <li>Compose simple shapes to form larger shapes (e.g join two triangles to make a rectangle).</li> </ul>
Measurement and Data	<ul> <li>Vocabulary: category, classify, chart, tally mark</li> </ul>	• Measuring identifies how long things are, how much things are, how much they weigh, and how much they hold.	<ul> <li>Describe measurable attributes of objects, such as length or weight.</li> <li>Describe several measurable attributes of a single object.</li> </ul>

<ul> <li>objects have measurable attributes, such as length or weight, that can be recognized and described.</li> <li>objects can have similar measurable attributes.</li> <li>objects can be sorted and classified by attribute</li> <li>objects in a group can be counted, sorted and compared</li> </ul>	<ul> <li>Objects can be classified into two categories, based on whether they have or do not have particular attributes.</li> </ul>	<ul> <li>Compare two objects with a measurable attribute in common to see which object has more of / less of a given attribute and describe the difference.</li> <li>Classify objects into categories.</li> <li>Sort and classify objects by attribute.</li> <li>Count the number of objects in each category and sort the categories by how many objects (0 to 10) are in each category (e.g. 2 circles, 1 triangle, 3 rectangles).</li> <li>Use tally marks to count.</li> <li>Chart data</li> </ul>
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## Unit #1: Place Value: Numbers and Operations in Base 10

	Stage 1 Desired Results	
ESTABLISHED GOALS:		Transfer
Students will begin their formal study of mathematics. In this unit, students will build a foundation for understanding place value by focusing on composing and decomposing numbers 11 - 19 into a group of 10 ones and some additional ones. To help visualize this, students		mathematics. using higher numbers to 100. g of base 10, and number naming fluency to build skills of
<ul> <li>will use objects, drawings and equations.</li> <li><i>Content Standards:</i></li> <li><i>K.NBT.A.1</i> Compose and decompose numbers from 11 to 19 into ten ones and some further ones, e.g., by using objects or drawings, and record each composition or decomposition by a drawing or equation (such as 18 = 10 + 8); understand that these numbers are composed of ten ones and one, two, three, four, five, six, seven, eight, or nine ones</li> </ul>	<ul> <li>ENDURING UNDERSTANDINGS</li> <li>Numbers from 11-19 can be represented as the sum of 10 and some more.</li> <li>A pattern is a repetition of shapes, numbers, or any items selected. These patterns can be used to help solve problems.</li> </ul>	<ul> <li>ESSENTIAL QUESTIONS</li> <li>How does knowing that teen numbers are made of ten and more help me to know the number?</li> <li>Why can I start with any number and continue counting?</li> <li>Why do we count in increasing order?</li> <li>Where have I seen these numbers in my life?</li> <li>Why do I need to count how many?</li> <li>How can I show ways to make 11, 12, 13, 14, 15, 16, 17, 18, 19, or 20?</li> <li>Why do you need to count in order?</li> <li>How can one problem help me to solve another?</li> </ul>
		Acquisition
	<ul> <li>Students will understand</li> <li>Numbers 11-19</li> <li>Vocabulary: how many more?</li> <li>Tens and ones</li> <li>Relationship between whole and parts</li> <li>Counting on</li> </ul>	<ul> <li>Students will be skilled at</li> <li>Identifying the value of a digit in a 2 digit number (11-19)</li> <li>Adding 10 and another digit to make a whole number.</li> <li>Using ten frames to understand base ten</li> <li>Being mindful of symbols in equations</li> <li>Counting on from 10</li> <li>Finding parts of a whole</li> </ul>

	• 10 can be added to another digit to make a whole number.	
Used in Content Area Standards		21 <sup>st</sup> Century Skills
		Problem solving
not applicable		Communication
		Perseverance

Stage 2 - Evidence	
Evaluative Criteria	Assessment Evidence
	ASSESSMENT: Written Assessments or Projects
	Other Evidence: independent practice, classroom observations and discussions

## **Unit 2: Operations & Algebraic Thinking - Addition & Subtraction**

idents will be able to independently use their add and subtract to solve more complex eq add and subtract to find differences in daily	uations.
add and subtract to solve more complex eq add and subtract to find differences in daily	uations.
add and subtract to find differences in daily	
	1:5
	life.
add and subtract to complete fact families.	
Меа	ning
	<ul><li>ESSENTIAL QUESTIONS</li><li>Why doesn't the order numbers in an</li></ul>
DU r t f f	Mea JRING UNDERSTANDINGS Addition and subtraction can be shown in many different ways. These include putting together, taking apart, separating, and pattern building. Subtraction equations using - and = can be used to show subtraction situations. Equations using plus signs and equal signs can be used to show parts of a whole. The ability to solve problems is the heart

	Acquisition	
	<ul> <li>Students will understand</li> <li>Vocabulary: in all, join, addition sentence, add, equal, equation, sum, left, separate, subtraction sentence, take away, subtract, difference.</li> <li>Symbols: Plus sign (+), equal sign (=)minus sign (-)</li> <li>Adding is joining 2 numbers or groups, subtracting is taking apart</li> <li>The addition symbol can be read as "plus" or "and."</li> </ul>	<ul> <li>Students will be skilled at</li> <li>Identifying the value of a digit in a 2 digit number (11-19).</li> <li>Using ten frames to understand base ten.</li> <li>Identifying symbols +, -, = in equations.</li> <li>Counting on from to find how many in all.</li> <li>Putting parts together to make a whole and taking a whole apart to find parts.</li> <li>Using patterns to develop fluency</li> <li>Demonstrating fluency of addition and subtraction facts (0 - 5).</li> </ul>
	<ul> <li>The minus sign can be read as "take away."</li> <li>The equal sign symbol can be read as "equals" or "is" or "same as".</li> <li>Equations can be written with addends before the sum or the sum before the</li> </ul>	<ul> <li>Representing addition and subtraction with objects (6 - 10) fingers, mental images, drawings, and sounds.</li> <li>Solving addition and subtraction word problems.</li> </ul>
	<ul><li>addends.</li><li>Fact families</li></ul>	<ul> <li>Decomposing numbers 0 -10 into pairs in more than one way by using objects and drawings and equations</li> </ul>
Used in Content Area Standards		21 <sup>st</sup> Century Skills
not applicable		<ul><li> Problem solving</li><li> Communication</li><li> Perseverance</li></ul>

Stage 2 - Evidence	
Evaluative Criteria	Assessment Evidence
	ASSESSMENT: Written Assessments or Projects
OTHER EVIDENCE: independent practice, classroom observations and discussions	

## **Unit 3: Counting & Cardinality - Counting & Ordering Numbers**

#### **Stage 1 Desired Results** ESTABLISHED GOALS: Transfer Students will continue their study of mathematics. In Students will be able to independently use their learning to... this unit, students will learn to write, identify and count correctly form and identify numbers in mathematics. • objects in a variety of arrangements, and understand build skills of addition, subtraction, story problem comprehension, etc. by using 1:1 correspondence, • the quantity of a group in order to compare groups to comparing numbers, and number names. find greater than, less than and equal to. Meaning ESSENTIAL QUESTIONS ENDURING UNDERSTANDINGS Content Standards: Why do I need to count how many? There is a unique symbol that goes with each K.CC.A.1 Count to 100 by ones and by tens. Why do you need to count in order? number word. K.CC.A.2 Count forward beginning from a given There is more than one way to show a number. Can we count how many objects no matter how • • number within the known sequence (instead of There is a specific order to the set of whole we set them up? having to begin at 1). Where have I seen numbers in my life? numbers. • K.CC.A.3 Write numbers from 0 to 20. Represent a Zero is a number that tells how many objects Why do we need to know the numbers? • • number of objects with a written numeral 0-20 How can I show ways to make 0,1,2,3,4,5,6, 7, there are when there are none. (with 0 representing a count of no objects) Counting tells the total number in a group no 8, 9, or 10? K.CC.B.4 Understand the relationship between matter which order the objects are counted. • How is zero different from the other numbers? numbers and quantities; connect counting to Two groups of objects are equal if they can be • Why are the groups equal or not equal? cardinality directly matched, one-to-one, with no extras in K.CC.B.5 Count to answer "how many?" questions either group. about as many as 20 things arranged in a line, a Counting helps us solve problems in our lives. rectangular array, or a circle, or as many as 10 Acquisition things in a scattered configuration; given a number Students will understand... Students will be skilled at... from 1-20, count out that many objects.

The name and formation for each number from

0-10

Counting begins with zero

•

•

the number 0-20.

Counting to 100 by ones and tens.

K.CC.C.6 Identify whether the number of objects • in one group is greater than, less than, or equal to •

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Counting to find how many objects and writing

<ul> <li>the number of objects in another group, e.g., by using matching and counting strategies.1</li> <li>K.CC.C.7 Compare two numbers between 1 and 10 presented as written numerals.</li> </ul>	<ul> <li>Meaning of greater than, less than, and equal groups</li> <li>Vocabulary: total, zero, number, part, whole, group order, compare, equal/equal to, greater than, less than, same number as, not</li> <li>1:1 correspondence</li> </ul>	<ul> <li>Counting forward from any given number to 100.</li> <li>Identifying and comparing numbers, between 1 and 10, in terms of greater than, less than or equal to.</li> </ul>
Used in Content Area Standards		21 <sup>st</sup> Century Skills
not applicable		<ul><li>Problem solving</li><li>Communication</li><li>Perseverance</li></ul>

Stage 2 - Evidence	
Evaluative Criteria	Assessment Evidence
	ASSESSMENT: Written Assessments or Projects
	OTHER EVIDENCE: independent practice, classroom observations and discussions

# Windham School District Curriculum **Mathematics - Kindergarten Unit 4: Geometry**

	Stage 1 Desired Results	
ESTABLISHED GOALS:	Tran	sfer
Students will continue their study of mathematics. In	Students will be able to independently use their lea	rning to
this unit, students will identify two and three	• name and recognize shapes in their authentic for	orms and within their environment
dimensional shapes as well as analyze and compare	<ul> <li>compare and sort shapes by kind</li> </ul>	
various shapes by their attributes.	Меа	ning
<ul> <li>Content Standards:</li> <li>CCSS.MATH.CONTENT.K.G.A.1 Describe objects in</li> </ul>	<ul> <li>ENDURING UNDERSTANDINGS</li> <li>Shapes are everywhere in our world.</li> <li>Objects can be classified into two categories,</li> </ul>	<ul><li>ESSENTIAL QUESTIONS</li><li>How do shapes make up our world?</li></ul>
the environment using names of shapes, and describe the relative positions of these objects	based on whether they have or do not have particular attributes.	
using terms such as above, below, beside, in front	Acqui	sition
<ul> <li>of, behind, and next to.</li> <li>CCSS.MATH.CONTENT.K.G.A.2 Correctly name shapes regardless of their orientations or overall size.</li> <li>CCSS.MATH.CONTENT.K.G.A.3 Identify shapes as two-dimensional (lying in a plane, "flat") or three-dimensional ("solid").</li> <li>CCSS.MATH.CONTENT.K.G.B.4 Analyze and compare two- and three-dimensional shapes, in different sizes and orientations, using informal language to describe their similarities, differences, parts (e.g., number of sides and vertices/"corners") and other attributes (e.g., having sides of equal length).</li> </ul>		<ul> <li>Students will be skilled at</li> <li>describing objects in the environment using names of shapes.</li> <li>identifying two-dimensional and three-dimensional shapes.</li> <li>naming shapes using attributes.</li> <li>analyzing and comparing two- and three-dimensional shapes, in different sizes and orientations, using informal language to describe their similarities, differences, parts (e.g. number of sides and vertices) and other attributes (e.g., having sides of equal length).</li> <li>constructing shapes using various materials (e.g. sticks and clay balls), and draw shapes.</li> </ul>

<ul> <li>CCSS.MATH.CONTENT.K.G.B.5 Model shapes in the world by building shapes from components (e.g., sticks and clay balls) and drawing shapes.</li> <li>CCSS.MATH.CONTENT.K.G.B.6 Compose simple shapes to form larger shapes. For example, "Can you join these two triangles with full sides touching to make a rectangle?"</li> </ul>	<ul> <li>describing the relative position of objects using positional words.</li> <li>naming shapes regardless of their orientations or overall size.</li> <li>composing simple shapes to form larger shapes. (For example, "Can you join these two triangles with full sides touching to make a rectangle?").</li> </ul>
Used in Content Area Standards	21 <sup>st</sup> Century Skills
not applicable	<ul> <li>Problem solving</li> <li>Communication</li> <li>Perseverance</li> </ul>

Stage 2 - Evidence		
Evaluative Criteria	Assessment Evidence	
	ASSESSMENT: Written Assessments or Projects	
Other Evidence: independent practice, classroom observations and discussions		

## Windham School District Curriculum Mathematics - Kindergarten Unit 5: Measurement & Data

	Stage 1 Desired Results		
ESTABLISHED GOALS:	Trai	nsfer	
Students will continue their study of mathematics. In	Students will be able to independently use their learning to		
this unit, students will be able to measure an object's	<ul> <li>understand differences in objects based on size.</li> </ul>		
length, width, height and volume and compare these	• use charts to understand data (how many more, how many fewer, which is the most? which is the		
attributes to those of other objects.	least? etc.)		
	Мес	ning	
Content Standards:	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS	
• K.MD.A.1 Describe measurable attributes of	• Measuring identifies how long things are, how	<ul> <li>Can all things be measured?</li> </ul>	
objects, such as length or weight. Describe several		• How do we use measurement every day?	
measurable attributes of a single object.	• Objects can be classified into two categories,	<ul> <li>Why do we measure things?</li> </ul>	
• K.MD.A.2 Directly compare two objects with a	based on whether they have or do not have	How many ways can you sort a group of	
measurable attribute in common, to see which	particular attributes.	objects?	
object has "more of"/"less of" the attribute, and		How can classifying data help to answer	
describe the difference. For example, directly compare the heights of two children and describe		questions?	
one child as taller/shorter.		Why do we chart our data?	
<ul> <li>K.MD.B.3 Classify objects into given categories;</li> </ul>	•	isition	
count the numbers of objects in each categories,		Students will be skilled at	
sort the categories by count.	• vocabulary: category, classify, chart, tany mark	• describing measurable attributes of objects,	
sort the categories by count.	• objects have measurable attributes, such as	such as length or weight.	
	length or weight, that can be recognized and described.	<ul> <li>describing several measurable attributes of a single object.</li> </ul>	
	• objects can have similar measurable attributes.	<ul> <li>comparing two objects with a measurable</li> </ul>	
	<ul> <li>objects can be sorted and classified by</li> </ul>	attribute in common to see which object has	
	attribute.	more of/less of a given attribute and describe	
	• objects in a group can be counted, sorted and	the difference.	
	compared.	classifying objects into categories.	

	•	sorting and classifying objects by attribute. counting the number of objects in each category and sorting the categories by how many objects (0 to 10) are in each category (e.g. 2 circles, 1 triangle, 3 rectangles). using tally marks to count. charting data using real life objects and pictographs.
Used in Content Area Standards		21 <sup>st</sup> Century Skills
not applicable	•	Problem solving Communication Perseverance

Stage 2 - Evidence		
Evaluative Criteria	Assessment Evidence	
	ASSESSMENT: Written Assessments or Projects	
Other Evidence: independent practice, classroom observations and discussions		

### Title of Curriculum: Grade 1 Mathematics

Unit Name	What (content, vocab)	Why (enduring understandings)	How (skills)
Counting	<ul> <li>Counting follows a sequence</li> <li>Numbers represent an object (1:1 correspondence)</li> <li>Numbers 1-120</li> <li>Numbers can be expressed in pictures, objects and numerals</li> </ul>	<ul> <li>Counting helps us solve problems in our lives.</li> </ul>	<ul> <li>Identify the value of a whole number (0 to 120)</li> <li>Count by 1s, 2s, 5s, 10s</li> <li>Order whole number from 0-120</li> <li>Write whole numbers from 0 -120</li> <li>Recognize visual representations of numbers (0-120)</li> <li>Create visual representations using models and written numbers.</li> <li>Represent a quantity of objects with a numeral</li> </ul>
Place Value	<ul> <li>Tens and ones</li> <li>Symbols &lt;, &gt;, and =</li> <li>2-digit numbers</li> <li>Multiples of 10 (10, 20, 30, 40, 50, 60, 70, 80, 90)</li> </ul>	<ul> <li>Numbers can be organized by ones and tens.</li> <li>Place value can help to solve math problems more efficiently.</li> <li>Place value can be used to compare numbers using symbols.</li> </ul>	<ul> <li>ordering whole numbers (0-120).</li> <li>Represent ten ones as a bundle called "ten".</li> <li>Identify the digit in the tens and ones places in a given two digit number.</li> <li>Identify the value of each digit within a 2-digit number</li> <li>Use mental math to add groups of 10 to a number</li> <li>Compare two-digit numbers using &lt;, &gt;, =</li> <li>add within 100, including adding a two-digit number and a one digit number (23+7=30), and adding a two-digit number and a multiple of 10 (23+20=43).</li> <li>understand that in adding two-digit numbers, one adds tens and tens, ones and ones; and sometimes it is necessary to compose a ten.</li> <li>mentally finding ten more and ten less than a given two-digit number without having to count and explain reasoning.</li> <li>subtracting multiples of 10 in the range of 10-90 from multiples of 10 in the range 10-90 (positive or zero differences).</li> </ul>

			<ul> <li>relating strategies used to add or subtract two two-digit numbers to a written method and explain reasoning used</li> </ul>
Addition and Subtraction	<ul> <li>Addition and subtraction</li> <li>Drawings, symbols, equations</li> <li>Numbers 1- 20</li> <li>Properties of addition and subtraction</li> </ul>	<ul> <li>Addition and subtraction can be shown in many different ways, including putting together, taking apart and separating.</li> </ul>	<ul> <li>Use addition and subtraction within 20 to solve problems, including word problems (adding to, taking from, putting together, taking apart, comparing) by using objects, drawings, and equations with a symbol for the unknown number to represent the problem.</li> <li>Solve word problems using addition of three whole numbers whose sum is less than or equal to 20.</li> <li>Fluently add and subtract facts within 10</li> <li>Determine the unknown number in an addition or subtraction equation relating to three whole numbers (8+?=10).</li> </ul>
Geometry	<ul> <li>2-D and 3-D shapes</li> <li>Equal shares of a whole</li> </ul>	<ul> <li>Shapes are everywhere in our world.</li> <li>A whole can be divided into equal shares.</li> <li>Addition and subtraction can be represented by models &amp; equal equations.</li> </ul>	Distinguish between defining and non-defining attributes
Measurement and Data	<ul><li>Length</li><li>Tools for measurement</li><li>Data</li></ul>	<ul> <li>Measuring objects allows us to compare the size of objects.</li> </ul>	

<ul> <li>Graphs, charts, pictures</li> <li>Graphing categories</li> <li>Analog clock</li> <li>Digital clock</li> <li>Hour hand</li> <li>Minute hand</li> </ul>	<ul> <li>Data and graphs are used to make decisions and solve problems.</li> <li>Time can be measured in a variety of forms including to the nearest hour and half hour.</li> </ul>	<ul><li>units (5 same size pencils) by laying multiple copies of a shorter object end to end.</li><li>comparing the lengths of two objects indirectly by</li></ul>
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## **Unit 1: Counting**

#### **Stage 1 Desired Results** ESTABLISHED GOALS: Transfer Students will continue their study of Students will be able to independently use their learning to... mathematics. In this unit, students will Recognize the value and order of numbers be able to count sequentially, read and Create and recognize visual representations of numbers write numbers correctly, and recognize Meaning visual representations of numbers. ESSENTIAL QUESTIONS ENDURING UNDERSTANDINGS Counting helps us solve problems in our lives. What can numbers represent? • Content Standards: How can numbers be represented using symbols, words and • CCSS.1.NBT.A. 1. Count to 120, tools? starting at any number less than Why do we need numbers? • 120. In this range, read and write numerals and represent a number Acquisition of objects with a written numeral. Students will understand... Students will be skilled at... CCSS.MP.4 Model with identifying the value of a whole number (0 to 120). counting follows a sequence. numbers represent an object (1:1 counting forward by 1, 2, 5, 10s (0 to 120). mathematics. • writing whole numbers (0 to 120). CCSS.MP.6 Attend to precision. correspondence). • • CCSS.MP7 Look for and make use of recognizing visual representations of numbers (0 to 120). • • Numbers 1-120. • understand numbers can be expressed in creating visual representation using models and written structure. • • CCSS.MP8 Look for and express pictures, objects and numerals. numbers (0 to 120). ordering whole numbers (0 to 120). regularity in repeated reasoning • Representing a quantity of objects with a number. • Used in Content Area Standards 21<sup>st</sup> Century Skills **Problem Solving** • not applicable Communication • Perseverance

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
	ASSESSMENT: Written Assessments or Projects	
OTHER EVIDENCE: independent practice, classroom observations and discussions		

## **Unit 2: Place Value**

St	tage 1 Desired Results
ESTABLISHED GOALS:	Transfer
Students will continue their study of mathematics. In this unit,	Students will be able to independently use their learning to
students will learn to organize numbers based on ones and tens.	<ul> <li>Make sense of and solve various math problems and real life problems</li> </ul>
They will be able to compare numbers using symbols. Students'	Recognize the value and order of numbers
understanding of place value will help them to solve math problems	<ul> <li>Use appropriate tools strategically</li> </ul>
more efficiently.	Create and recognize visual representations of numbers
	Meaning
<ul> <li>Content Standards:</li> <li>CCSS.1.NBT.B. 2. Understand that the two digits of a two-digit</li> </ul>	<ul> <li>ENDURING UNDERSTANDINGS</li> <li>Numbers can be organized by ones</li> <li>How does understanding place value help us to</li> </ul>
number represent amounts of tens and ones. Understand the	and tens compare and order numbers?
following as special cases: - 10 can be thought of as a bundle of ten ones – called a "ten" The numbers from 11 to 19 are composed of a ten and one, two, three, four, five, six, seven,	<ul> <li>Place value can help to solve math problems more efficiently.</li> <li>How can knowing the value of a number help us to make decisions?</li> </ul>
eight, or nine ones The numbers 10, 20, 30, 40, 50, 60, 70,	<ul> <li>Place value can be used to compare numbers using symbols.</li> <li>Why are zero and ten important?</li> </ul>
80, 90 refer to one, two, three, four, five, six, seven, eight, or	Acquisition
<ul> <li>nine tens (and 0 ones).</li> <li>CCSS.1.NBT.B.3. Compare two two-digit numbers based on meanings of the tens and ones digits, recording the results of comparisons with the symbols &gt;, =, and &lt;. Use place value understanding and properties of operations to add and subtract.</li> <li>CCSS.1.NBT.C.4. Add within 100, including adding a two-digit number and a one-digit number, and adding a two-digit number and a multiple of 10 using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and</li> </ul>	<ul> <li>Students will understand</li> <li>two digits of a 2-digit number represents amounts of tens and ones.</li> <li>symbols &lt;, &gt;, and = can be used to compare numbers</li> <li>value of zero in a multiple of 10 (10, 20, 30, 40, etc).</li> <li>meaning of base-ten and its use for solving number and real life</li> <li>Students will be skilled at</li> <li>representing ten ones as a bundle called "ten".</li> <li>identifying the digit in the tens and one places in a given two-digit number.</li> <li>identifying the value of each digit within a 2-digit number.</li> <li>Using mental math to add groups of 10 to a number.</li> <li>comparing two two-digit numbers using &lt;, &gt;, and =.</li> </ul>

Used in Content Area Standards not applicable	<ul> <li>21<sup>st</sup> Century Skills</li> <li>Problem Solving</li> <li>Communication</li> <li>Perseverance</li> </ul>
<ul> <li>subtraction; relate the strategy to a written method and explain the reasoning used.</li> <li>CCSS.1.NBT.C. 5. Given a two-digit number, mentally find 10 more or 10 less than the number, without having to count; explain the reasoning used.</li> <li>CCSS.1.NBTC. 6. Subtract multiples of 10 in the range 10 to 90 from multiples of 10 in the range 10 to 90 (positive or zero differences), using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method and explain the reasoning used. CCSS.MP1 Make sense of problems and persevere in solving them.</li> <li>CCSS.MP4 Model with mathematics.</li> <li>CCSS.MP4 Model with mathematics.</li> <li>CCSS.MP8 Look for and make use of structure.</li> <li>CCSS.MP8 Look for and express regularity in repeated reasoning.</li> </ul>	<ul> <li>adding within 100, including adding a two-digit number and a one digit number (23+7=30), and adding a two-digit number and a multiple of 10 (23+20=43).</li> <li>understanding that in adding two-digit numbers, one adds tens and tens, ones and ones; and sometimes it is necessary to compose a ten.</li> <li>mentally finding ten more and ten less than a given two-digit number without having to count and explain reasoning.</li> <li>subtracting multiples of 10 in the range of 10 to 90 from multiples of 10 in the range 10 to 90 (positive or zero differences).</li> <li>relating strategies used to add or subtract two two-digit numbers to a written method and explain reasoning used</li> </ul>

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
	ASSESSMENT: Written Assessments or Projects	
Other Evidence: independent practice, classroom observations and discussions		

## Windham School District Curriculum Mathematics - Grade 1 Unit 3: Addition & Subtraction

Stage 1 Desired Results			
ESTABLISHED GOALS:	Transfer		
Students will continue their study of mathematics. In this unit, students will be able to use multiple strategies to solve addition and subtraction word problems. Students will demonstrate fluency in addition and subtraction problems within 10.	<ul> <li>Students will be able to independently use their learning to</li> <li>Apply addition and subtraction strategies to solve problems in everyday life.</li> </ul>		
	Meaning		
<ul> <li>Content Standards:</li> <li>CCSS.1.OA A.1. Use addition and subtraction within 20 to solve word problems involving situations of adding to taking from, putting together, taking apart, and comparing, with unknowns in all positions, e.g., by using objects, drawings, and equations with a symbol for the unknown number to represent the problem.</li> <li>CCSS.1.OA.A.2. Solve word problems that call for addition of three whole numbers whose sum is less than or equal to 20, e.g., by using objects, drawings, and equations with a symbol for the unknown number to represent</li> </ul>	<ul> <li>ENDURING UNDERSTANDINGS</li> <li>Addition and subtraction can be shown in many different ways including putting together, taking apart, and separating.</li> <li>Addition and subtraction can be represented by models and equations.</li> <li>ESSENTIAL QUESTIONS</li> <li>How do addition and subtraction help me function in my world?</li> <li>How does comparing numbers help us solve problems?</li> </ul>		
the problem. Understand and apply properties of operations and the	<ul> <li>Students will understand</li> <li>multiple ways to solve addition and subtraction equations with whole numbers.</li> <li>addition and subtraction procedures have real world application.</li> <li>commutative and associative properties of addition and subtraction.</li> <li>Students will be skilled at</li> <li>using addition and subtraction within 20 to solve problems, including word problems (adding to, taking from, putting together, taking apart, comparing) by using objects, drawings, and equations with a symbol for the unknown number to represent the problem.</li> <li>solving word problems that call for addition of three whole numbers</li> </ul>		

<ul> <li>CCSS.1.OA.C. 6 Add and subtract within 20, demonstrating fluency for addition and subtraction within 10. Use strategies such as counting on; making ten (e.g., 8+6=8+2+4=10+4=14); decomposing a number leading to a ten (e.g., 13-4=13-3-1=10-1=9); using the relationship between addition and subtraction (e.g., knowing that 8+4=12, one knows 12-8=4); and creating equivalent but easier or known sums (e.g., adding 6+7 by creating the known equivalent 6+6+1=12+1=13).</li> <li>CCSS.1. OA.D.7. Understand the meaning of the equal sign, and determine if equations involving addition and subtraction are true or false. For example, which of the following equations are true and which are false? 6=6, 7=8-1, 4+1=5+2. CCSS.</li> <li>1.OA.D. 8. Determine the unknown whole number in an addition or subtraction equation relating to three whole numbers. For example, determine the unknown number that makes the equation true in each of the equations 8+? =11, 5=? +3, 6+6=?</li> <li>CCSS.MP1 Make sense of problems and persevere in solving them.</li> <li>CCSS.MP2 Reason abstractly and quantitatively.</li> <li>CCSS.MP4 Model with mathematics.</li> <li>CCSS.MP7 Look for and make use of structure.</li> </ul>	<ul> <li>number models, objects and drawings are various ways to solve problems.</li> <li>meaning of the symbols and the equal sign within equations.</li> <li>an unknown number in an equation can be determined by demonstrating the relationship between addition and subtraction</li> </ul>	•	whose sum is less than or equal to 20. fluently adding and subtracting facts within ten. determining the unknown number in an addition or subtraction equation relating to three whole numbers (8+? =10).
Used in Content Area Standards			21 <sup>st</sup> Century Skills
not applicable		•	Problem Solving Communication Perseverance

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
Other Evidence: independent practice, classroom observations and discussions		

## **Unit 4: Geometry**

### **Stage 1 Desired Results**

### ESTABLISHED GOALS:

Students will continue their study of mathematics. In this unit, students will identify two-dimensional and three-dimensional shapes according to defining attributes. Students will be able to partition circles, squares, and rectangles into two and four equal parts, describing those parts as halves, fourths, or quarters.

### Content Standards:

- CCSS.1.G.A. 1. Distinguish between defining attributes (e.g., triangles are closed and three-sided) versus non-defining attributes (e.g. color, orientation, overall size); build and draw shapes to possess defining attributes.
- CCSS.1.G.A.2. Compose two-dimensional shapes (rectangles, squares, trapezoids, triangles, half-circles, and quarter-circles) or three-dimensional shapes (cubes, right rectangular prisms, right circular cones, and right circular cylinders) to create a composite shape, and compose new shapes from the composite shape.
- CCSS.1.G.A. 3. Partition circles and rectangles into two and four equal shares, describe the shares using the words halves, fourths, and quarters, and use the phrases half of, fourth of, and quarter of. Describe the whole as two of, or four of the shares.

Tra	Insfer
Students will be able to independently use their lea	arning to
• Divide shapes into equal shares and identify the	ose shares
Recognize shapes in their environment	
Ме	aning
ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS
• Shapes are everywhere in our world.	• How do shapes make up our world? How is the
• A whole can be divided into equal shares.	world of geometry connected to the world of
	numbers?
Acqu	lisition
Students will understand	Students will be skilled at
<ul> <li>Two and three-dimensional objects can be described, classified and analyzed by their attributes.</li> <li>The names of two and three-dimensional shapes are based on their attributes.</li> <li>shapes can be partitioned in equal shares.</li> </ul>	<ul> <li>distinguishing between defining (triangles have three sides) and non-defining attributes (color, orientation, overall size).</li> <li>building and drawing shapes with defining attributes.</li> <li>composing (making) two-dimensional shapes to create a composite shape (e.g. two trapezoids to create a hexagon).</li> <li>composing (making) three-dimensional shapes (e.g. 6 squares to create a cube).</li> <li>comparing new shapes made from composite shapes.</li> <li>partitioning circles and rectangles into two and four equal shares</li> </ul>

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
	ASSESSMENT: Written Assessments or Projects	
	OTHER EVIDENCE: independent practice, classroom observations and discussions	

## **Unit 5: Measurement & Data**

Stage 1 Desired Results				
ESTABLISHED GOALS:	Transfer			
Students will continue their study of mathematics. In	Students will be able to independently use their lea	rning to		
this unit, students will make accurate measurements	make accurate measurements			
using non-standard units. They will be able to read,	• order objects from longest to shortest or shortes	st to longest based on measurement		
create, and ask and answer questions using different	<ul> <li>read different types of graphs in different situati</li> </ul>	ons and use the information to make accurate		
types of graphs. Students will also write and tell time to				
the hour and half hour.	• display data in a variety of ways.			
		ning and make sense of the data to apply to their		
Content Standards:	everyday lives.	0		
• CCSS.1.MD.A. 1. Order three objects by length;	<ul> <li>accurately tell and write time to help make decisions.</li> </ul>			
compare the lengths of two objects indirectly by	Meaning			
using a third object.		ESSENTIAL QUESTIONS		
<ul> <li>CCSS.1.MD.A. 2. Express the length of an object as</li> </ul>	<ul> <li>Measuring objects allow us to compare the size</li> </ul>			
a whole number of length units, by laying multiple	of objects,	<ul><li>Why is measuring important?</li></ul>		
copies of a shorter object (the length unit) end to				
end; understand that the length measurement of	<ul> <li>Data and graphs are used to make decisions</li> </ul>	<ul> <li>How can data help us to make decisions and askin machineral</li> </ul>		
an object is the number of same-size length units	and solve problems.	solve problems?		
that span it with no gaps or overlaps. Limit to	• Time can be measured in a variety of forms	• How can time affect the decisions we make?		
	including to the nearest hour and half hour.			
contexts where the object being measured is	Acquisition			
spanned by a whole number of length units with	Students will understand	Students will be skilled at		
no gaps or overlaps.	• attributes (e.g. length, height) of objects are	<ul> <li>measuring and recording the length of an</li> </ul>		
• CCSS.1.MD.B. 3. Tell and write time in hours and	measurable and can be quantified using unit	object using same size units that span the		
half-hours using analog and digital clocks.	amounts.	object with no gaps or overlaps. expressing the		
• CCSS.1.MD.C. 4. Organize, represent, and interpret	• time can be determined using an analog or a	length of an object by stating the length as a		
data with up to three categories; ask and answer	digital clock.	whole number of units (5 same size pencils) by		
questions about the total number of data points,				

Used in Content Area Standards not applicable		<ul> <li>number of data points: How many in each category? How many more or less are in one category than in another?</li> <li>telling and writing time to the hour and half-hour using analog and digital clocks.</li> <li>21<sup>st</sup> Century Skills</li> <li>Problem Solving</li> <li>Communication</li> <li>Perseverance</li> </ul>
		<ul> <li>organizing and representing data with up to three categories (Pets: dog, cat, bird).</li> <li>interpreting data with up to three categories.</li> <li>asking and answering questions about the tot</li> </ul>
<ul> <li>how many in each category, and how many more or less are in one category than in another.</li> <li>CCSS.MP1 Make sense of problems and persevere in solving them.</li> <li>CCSS.MP4 Model with mathematics.</li> <li>CCSS.MP5 Use appropriate tools strategically.</li> <li>CCSS.MP6 Attend to precision.</li> <li>CCSS.MP7 Look for and make use of structure.</li> </ul>	<ul> <li>the different features of a clock such as hour hand and minute hand.</li> <li>questions can be answered by collecting and analyzing data.</li> <li>data represents real world objects and ideas.</li> <li>data can be represented in different forms (chart, graph, picture).</li> </ul>	<ul> <li>laying multiple copies of a shorter object end end.</li> <li>comparing the lengths of two objects indirect by using a third object (a pencil, a shoe, a cube).</li> <li>measuring the length of an object using same size units that span the object with no gaps or overlaps.</li> <li>ordering three objects by length.</li> </ul>

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
Other Evidence: independent practice, classroom observations and discussions		

### Title of Curriculum: Grade 2 Mathematics

Unit Name	What (content, vocab)	Why (enduring understandings)	How (skills)
Time and Money	<ul> <li>Analog and digital clocks</li> <li>Hour and minute hand</li> <li>Coins and bills</li> <li>\$ and cent symbols</li> </ul>	<ul> <li>Time can be given in many forms including to the nearest 5 minutes.</li> <li>When counting money, it is usually easier to start with the coin with the greater value.</li> <li>The same amount of money can be represented using different combinations of coins and bills.</li> </ul>	<ul> <li>Writing time from analog and digital clock to the nearest five minutes, using a.m. and p.m.</li> <li>Determining total amount of a collection of various coins (half dollars, quarters, dimes, nickels, pennies).</li> <li>Showing an amount several different ways using</li> </ul>
Addition and Subtraction within 20	<ul> <li>Addition &amp; subtraction drawings, symbols, equations, properties</li> <li>Sum, difference</li> <li>Fact Families</li> <li>Equal Groups / Arrays</li> <li>Odd and even</li> </ul>	<ul> <li>There are strategies for learning addition and subtraction facts within 20 that will help with fluency. This includes counting on, making ten, and decomposing.</li> </ul>	<ul> <li>Solving one- and two- step problems using addition and subtraction within 20 with unknowns in all positions.</li> <li>demonstrating fluency of addition and subtraction facts within 20., using mental math strategies.</li> <li>writing fact families that consist of 2 addition and 2 subtraction equations using 3 numerals.</li> <li>arranging objects in rectangular arrays with up to 5 rows and 5 columns and writing an equation to express the total as a sum of equal addends.</li> </ul>
Addition and Subtraction for Larger Units	<ul> <li>Addition and subtraction equations</li> <li>Regrouping</li> <li>Composing and decomposing three digit numbers</li> </ul>	<ul> <li>Students will use place value understanding and properties of operations to solve two-digit three-digit addition and subtraction equations.</li> <li>Two digit numbers can be broken apart using tens and ones and added in different ways.</li> </ul>	<ul> <li>adding and subtracting numbers within 100 using place value strategies.</li> <li>breaking apart numbers into tens and ones to find their sums and differences.</li> <li>explaining their mathematical thinking.</li> <li>adding up to four 2-digit numbers</li> <li>understanding addends can be added in any order.</li> <li>adding 10 or 100 mentally using place value</li> </ul>

	<ul> <li>Three-digit numbers can be broken apart using hundreds, tens, and ones and added in different ways.</li> <li>adding 3 digit numbers using such as adding partial sums, of traditional algorithms and me</li> </ul>	compensation,
Representing and Interpreting Data	<ul> <li>Bar graphs, picture graphs and line plots</li> <li>Data</li> <li>Data</li> <li>Some questions can be answered by collecting and analyzing data.</li> <li>Data can be represented visually using charts &amp; graphs</li> <li>collecting measurement data of several objects to the near showing the measurements b where the horizontal scale is near the several objects to the near showing the measurements be whole-number units.</li> </ul>	a data set with up to Spring, Summer). action, and comparing tion presented in a bar by measuring lengths est whole unit and y making a line plot,
Geometry	<ul> <li>2D and 3D shapes</li> <li>Equal shares of a whole</li> <li>Fraction</li> <li>Halves</li> <li>Thirds</li> <li>Fourths</li> <li>Quarters</li> <li>Attributes</li> <li>Attributes<td>or a given number of d attributes, such as a given number of equal terals, pentagons, ones, and cylinders. and columns of es within the rows and ober of squares. into two, three or ing the equal shares ectively. halves, three thirds, of identical wholes</td></li></ul>	or a given number of d attributes, such as a given number of equal terals, pentagons, ones, and cylinders. and columns of es within the rows and ober of squares. into two, three or ing the equal shares ectively. halves, three thirds, of identical wholes

Measurement	<ul> <li>Rulers, yard and meter sticks, tape measures</li> <li>Number lines</li> <li>Units of measure: inches, feet, yards, centimeters and meters</li> <li>Length</li> </ul>	<ul> <li>Some attributes of objects are measurable and can be quantified using unit amounts.</li> <li>Objects can be measured using multiple units of measurement.</li> </ul>	different units of measure, and describing how the two measurements relate to the size of the unit
Place Value	<ul> <li>Base 10 blocks</li> <li>Hundreds charts</li> <li>&lt;, &gt;, = symbols</li> <li>2, 3, 4 digit numbers</li> <li>Greater than</li> <li>Less than</li> <li>Equal to</li> <li>Value</li> </ul>	<ul> <li>The value of a number can be determined by the place value of the number.</li> <li>Place value can be used to compare and order numbers.</li> </ul>	• Representing 3 digit numbers using models, words,

## **Unit 1: Time & Money**

## Stage 1 Desired Results

	Slage I Desireu Results		
ESTABLISHED GOALS:		Transfer	
Students will continue their study of	Students will be able to independently use their learning to		
mathematics. In this unit, students will be able	• tell and write time to the nearest 5 minutes.		
to tell and write time to the nearest 5 minutes.	<ul> <li>show an amount using dollars and/or coins.</li> </ul>		
Students will be able to show an amount using	Meaning		
dollars and/or coins.	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS	
	• Time can be given in many forms including o	• How would life be different if we couldn't measure	
Content Standards:	the nearest 5 minutes.	time?	
• CCSS.2.MD 7. Tell and write time from	• When counting money, it is usually easier to	• What would the world be like without money?	
analog and digital clocks to the nearest five	start with the coin with the greater value.	• How can time affect the decisions we make?	
minutes using a.m. and p.m.	<ul> <li>The same account of money can be</li> </ul>		
<ul> <li>CCSS.2.MD 8. Solve word problems</li> </ul>	represented using different combinations of		
involving dollar bills, quarters, dimes,	coins and bills.		
nickels, and pennies, using dollar and cent			
symbols appropriately. Example: If you	A	Acquisition	
	Students will understand	Students will be skilled at	
many cents do you have?	<ul> <li>analog and digital clocks</li> </ul>	• telling time from analog and digital clock to the nearest	
	<ul> <li>time to the nearest five minutes</li> </ul>	five minutes, using a.m. and p.m.	
	• am. and pm.	<ul> <li>writing time from analog and digital clock to the nearest</li> </ul>	
	• names and value of quarters, nickels, pennies,	five minutes, using a.m. and p.m.	
	dimes, dollar bills	• Determining the total amount of a collection of various	
	<ul> <li>dollar and cent symbols</li> </ul>	coins (half dollars, quarters, dimes, nickels, pennies).	
		showing an amount several different ways using	
		quarters, dimes, nickels and pennies.	
		<ul> <li>solving word problems involving dollar bills and coins.</li> </ul>	
Used in Content Area Standards		21 <sup>st</sup> Century Skills	

	٠	Problem Solving
not applicable	•	Communication
	•	Perseverance

Stage 2 - Evidence	
Evaluative Criteria	Assessment Evidence
	ASSESSMENT: Written Assessments or Projects
Other Evidence: independent practice, classroom observations and discussions	

## **Unit 2: Addition & Subtraction Within 20**

	Stage 1 Desired Results		
ESTABLISHED GOALS:	Tran	nsfer	
Students will continue their study of mathematics. In	Students will be able to independently use their learning to		
this unit, students will use addition and subtraction	• use addition and subtraction strategies to solve problems in everyday life.		
strategies to solve problems in everyday life.	Meaning		
<ul> <li>Content Standards:</li> <li>2.OA.A.1. Use addition and subtraction within 100 to solve one- and two-step word problems involving situations of adding to, taking from, putting together, taking apart, and comparing with unknowns in all positions; e.g., by using drawings</li> </ul>	• There are strategies for learning addition and subtraction facts within 20 that will help with fluency. This includes counting on, making ten, and decomposing.	<ul> <li>ESSENTIAL QUESTIONS</li> <li>How would life be different if we couldn't add or subtract?</li> <li>Why is being able to add and subtract important?</li> <li>What would happen if you could only add, and not subtract?</li> </ul>	
<ul> <li>and equations with a symbol for the unknown number to represent the problem.</li> <li>2.OA.B.2. Fluently add and subtract within 20 using mental strategies. By the end of Grade 2, know from memory all sums of two one-digit numbers.</li> <li>2.OA.C.3 Determine whether a group of objects (up to 20) has an odd or even number of members, e.g., by pairing objects or counting them by 2s; write an equation to express an even number as a sum of two equal addends.</li> <li>2.OA.C.4 Use addition to find the total number of objects arranged in rectangular arrays with up to 5 rows and up to 5 columns; write an equation to express the total as a sum of equal addends.</li> </ul>	<ul> <li>Students will understand</li> <li>how to identify the sum and difference in addition and subtraction equations.</li> <li>fact families are a group of four facts using the same three numbers.</li> <li>whether a number is odd or even</li> <li>how to arrange objects into arrays and write equations that represent the array</li> </ul>	<ul> <li>isition</li> <li>Solving one- and two- step problems using addition and subtraction within 20 with unknowns in all positions.</li> <li>demonstrating fluency of addition and subtraction facts within 20., using mental math strategies.</li> <li>writing fact families that consist of 2 addition and 2 subtraction equations using 3 numerals.</li> <li>arranging objects in rectangular arrays with up to 5 rows and 5 columns and writing an equation to express the total as a sum of equal addends.</li> </ul>	

Used in Content Area Standards	21 <sup>st</sup> Century Skills
	Problem solving
not applicable	Communication
	Perseverance

Stage 2 - Evidence	
Evaluative Criteria	Assessment Evidence
	ASSESSMENT: Written Assessments or Projects
	OTHER EVIDENCE: independent practice, classroom observations and discussions

## **Unit 3: Addition & Subtraction For Larger units**

	Stage 1 Desired Results		
ESTABLISHED GOALS:	Transfer		
Students will continue their study of mathematics. In this unit, students will add and subtract within 100, and 1000 using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction.	<ul> <li>Students will be able to independently use their learning to</li> <li>add and subtract within 100, using concrete models or drawings and strategies based on place value,</li> </ul>		
Content Standards:	Meaning		
<ul> <li>CCSS.2 NBT.B.5. Fluently add and subtract within 100 using strategies based on place value, properties of operations, and/or the relationship between addition and subtraction.</li> <li>CCSS.2 NBT.B.6. Add up to four two-digit numbers using strategies based on place value and</li> </ul>	<ul> <li>ENDURING UNDERSTANDINGS</li> <li>Two digit numbers can be broken apart using tens and ones and added in different ways.</li> <li>Three-digit numbers can be broken apart using hundreds, tens, and ones and added in different ways.</li> </ul>	<ul> <li>ESSENTIAL QUESTIONS</li> <li>How do we understand place value and use properties of operations to add and subtract?</li> <li>How does the position of a digit in a number affect its value?</li> </ul>	
properties of operations.	Acquisition		
<ul> <li>CCSS.2.NBT.B.7 Add and subtract within 1000, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method. Understand that in adding or subtracting three-digit numbers, one adds or subtracts hundreds and hundreds, tens and tens, ones and ones; and sometimes it is necessary to compose or decompose tens or hundreds.</li> </ul>	<ul> <li>a variety of strategies to add and subtract.</li> <li>how to compose and decompose 2 and 3-digit numbers to add and subtract.</li> <li>place value</li> <li>properties of operations of addition and subtraction</li> </ul>	<ul> <li>Students will be skilled at</li> <li>adding and subtracting numbers within 100 using place value strategies.</li> <li>breaking apart numbers into tens and ones to find their sums and differences.</li> <li>explaining their mathematical thinking.</li> <li>adding up to four 2-digit numbers</li> <li>understanding addends can be added in any order.</li> <li>adding 10 or 100 mentally using place value</li> </ul>	

<ul> <li>CCSS.2.NBT.B.8 Mentally add 10 or 100 to a given number 100-900 and mentally subtract 10 or 100 from a given number 100-900.</li> <li>CCSS.2.NBT.B.9 Explain why addition and subtraction strategies work, using place value and the properties of operations.</li> </ul>	<ul> <li>adding 3 digit numbers using a variety of strategies such as adding partial sums, compensation, traditional algorithms and mental math.</li> </ul>
Used in Content Area Standards	21 <sup>st</sup> Century Skills
not applicable	<ul> <li>Problem Solving</li> <li>Communication</li> <li>Perseverance</li> </ul>

Stage 2 - Evidence		
Evaluative Criteria	Assessment Evidence	
ASSESSMENT: Written Assessments or Projects		
Other Evidence: independent practice, classroom observations and discussions		

### **Unit 4: Representing & Interpreting Data**

Stage 1 Desired Results			
ESTABLISHED GOALS:	Transfer		
Students will continue their study of	Students will be able to independently use their learning to		
mathematics. In this unit, students will use data	<ul> <li>use data and graphs to make decisions and solve problems.</li> </ul>		
and graphs to make decisions and solve		Meaning	
problems.	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS	
Content Standards:	• Some questions can be answered by	• Why is graphing important?	
CCSS.2. MD 9. Generate measurement data	collecting and analyzing data.	<ul> <li>Is one graph better than another?</li> </ul>	
by measuring lengths of several objects to	• Data can be represented visually using	• How do graphs help us learn about our world?	
the nearest whole unit, or by making	charts and graphs.		
repeated measurements of the same object. Show the measurements by making a line		Accusicities	
plot, where the horizontal scale is marked		Acquisition	
off in whole-number units.	Students will understand	Students will be skilled at	
• CCSS.2. MD 10. Draw a picture graph and a	<ul> <li>Data represents real world objects and ideas.</li> </ul>		
bar graph (with single-unit scale) to	lueas.	scale) to represent a data set with up to four categories. (Fall, Winter, Spring, Summer).	
represent a data set with up to four		<ul> <li>Solving simple addition, subtraction, and comparing word</li> </ul>	
categories. Solve simple put-together,		problems using information presented in a bar graph and a	
take-apart, and compare problems using		picture graph.	
information presented in a bar graph.		Collecting measurement data by measuring lengths of several	
		objects to the nearest whole unit and showing the	
		measurements by making a line plot, where the horizontal	
		scale is marked off in whole-number units.	
Used in Content Area Standards		21 <sup>st</sup> Century Skills	
		Problem solving	
not applicable		Communication	
		Perseverance	

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
Other Evidence: independent practice, classroom observations and discussions		

## **Unit 5: Geometry**

	Stage 1 Desired Results		
ESTABLISHED GOALS:	Transfer		
Students will continue their study of mathematics. In	Students will be able to independently use their learning to		
this unit, students will be able to identify shapes in the	<ul> <li>identify shapes in the world around them based on their attributes .</li> </ul>		
world around them based on their attributes and also	divide wholes into equal shares.		
be able to divide wholes into equal shares.	Meaning		
<ul> <li>Content Standards:</li> <li>CCSS.2.G.1. Recognize and draw shapes having specified attributes, such as a given number of angles or a given number of equal faces. Identify triangles, quadrilaterals, pentagons, hexagons, and cubes.</li> <li>CCSS.2.G.2. Partition a rectangle into rows and columns of same-size squares and count to find the total number of them</li> <li>CCSS.2.G.3. Partition circles and rectangles into two, three, or four equal shares, describe the shares using the words halves, thirds, half of, a third of, etc., and describe the whole as two halves, three thirds, four fourths. Recognize that equal shares of identical wholes need not have the same shape.</li> </ul>	<ul> <li>Two-and-three-dimensional objects have unique attributes.</li> <li>A shape can be divided into equal sized parts.</li> </ul>	<ul> <li>ESSENTIAL QUESTIONS</li> <li>How can geometry be used to solve problems?</li> <li>How does understanding shapes help you to build?</li> <li>How can you prove that something is divided equally?</li> <li>isition</li> </ul>	
	<ul> <li>attributes of 2-D shapes (angles, sides, and vertices)</li> <li>attributes of 3-D shapes (angles, vertices, faces)</li> <li>2-D shapes can be divided into equal shares (halves, thirds, fourths).</li> <li>The names of shapes are based on their attributes</li> </ul>	<ul> <li>recognizing the specified attributes of shapes, such as a given number of angles or a given number of equal faces.</li> <li>drawing shapes with specified attributes, such as a given number of angles or a given number of equal faces.</li> <li>identifying triangles, quadrilaterals, pentagons, hexagons, cubes, pyramids, cones, and cylinders.</li> <li>dividing a rectangle into rows and columns of same-size squares.</li> </ul>	

	<ul> <li>and colu squares.</li> <li>dividing or four e shares as</li> <li>describir thirds, fo</li> <li>recognizion</li> </ul>	g the same-size squares within the rows imns to find the total number of circles and rectangles into two, three equal shares and describing the equal s halves, thirds, fourths respectively. ng the whole as two halves, three our fourths, etc. ing that equal shares of identical need not have the same shape.
Used in Content Area Standards		21 <sup>st</sup> Century Skills
	Problem	Solving
not applicable	Commur	nication
	Persever	rance

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
Other Evidence: independent practice, classroom observations and discussions		

### **Unit 6: Measurement**

#### **Stage 1 Desired Results** ESTABLISHED GOALS: Transfer Students will continue their study of mathematics. In Students will be able to independently use their learning to... this unit, students will be able to use their use their understanding of measuring tools to measure objects. understanding of measuring tools to measure objects. Meanina ENDURING UNDERSTANDINGS ESSENTIAL QUESTIONS Content Standards: Some attributes of objects are measurable and What would life be like if standard units of • CCSS.2.MD. 1 Measure the length of an object by can be quantified using unit amounts. measurement did not exist? selecting and using appropriate tools such as • Objects can be measured using multiple units • How does what we measure affect what we use rulers, yardsticks, meter sticks, and measuring of measurements. to measure? tapes. CCSS.2.MD. 2. Measure the length of an object Acauisition twice, using length units of different lengths for Students will understand... Students will be skilled at... the two measurements: describe how the two Use the appropriate tool for measuring objects measuring the length of an object twice, using • measurements relate to the size of the unit is important for accuracy. two different units of measure, and describing chosen. Measurements can be compared. how the two measurements relate to the size • CCSS.2.MD. 3 Estimate lengths using units of similarity between a measuring tool and a of the unit chosen. estimating lengths using • inches, feet, centimeters, and meters. units of inches, feet, centimeters, and meters. number line. CCSS.2.MD. 4. Measure to determine how much how to use rulers, yardsticks, meter sticks, and Estimating the length of an object using ٠ longer one object is than another, expressing the measuring tapes to measure objects. appropriate units for that object. length difference in terms of a standard-length measuring to determine how much longer one • object is than another. CCSS.2.MD.B5 Use addition and subtraction within expressing the differences in length in terms of 100 to solve word problems involving lengths that a standard length unit. are given in the same units, e.g., by using drawings using addition and subtraction within 100 to • (such as drawings of rulers) and equations with a

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unit.

solve word problems involving lengths that are given in the same unit by using drawings and

<ul> <li>symbol for the unknown number to represent the problem.</li> <li>CCSS.2.MD.B6 Represent whole numbers as lengths from 0 on a number line diagram with equally spaced points corresponding to the numbers 0, 1, 2, and represent whole-number sums and differences within 100 on a number line diagram.</li> </ul>	<ul> <li>equations with a symbol for the unknown number to represent the problem.</li> <li>representing whole numbers as lengths from 0 on a number line with equally spaced points corresponding to the numbers 0, 1, 2 and represent whole number sums and differences within 100 on a number line.</li> <li>generating measurement data by measuring lengths of several objects to the nearest whole unit or by making repeated measurements of the same object.</li> </ul>
Used in Content Area Standards	21 <sup>st</sup> Century Skills
not applicable	<ul> <li>Problem solving</li> <li>Communication</li> <li>Perseverance</li> </ul>

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
Other Evidence: independent practice, classroom observations and discussions		

## **Unit 7: Place Value**

	Stage I Desired Results		
ESTABLISHED GOALS:	Transfer		
Students will continue their study of mathematics. In	Students will be able to independently use their learning to		
this unit, students will understand the significance of	<ul> <li>understand the significance of ordering numbers in ones, tens, hundreds and thousands.</li> </ul>		
ordering numbers in ones, tens, hundreds and	<ul> <li>use place value to solve problems more efficient</li> </ul>	tly.	
thousands. Students will use place value to solve	Meaning		
problems more efficiently.	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS	
	• The value of a number can be determined by	• How does the value of a digit change when it is	
Content Standards:	the place value of the number.	moved from one place value to another?	
• 2.NBT.A.1. Understand that the three digits of a	• Place value can be used to compare and order	• Why is the number zero important in place	
three-digit number represent amounts of	numbers.	value?	
hundreds, tens, and ones; e.g., 706 equals 7			
hundreds, 0 tens, and 6 ones. Understand the	Acquisition		
following as special cases:	Students will understand	Students will be skilled at	
<ul> <li>- 100 can be thought of as a bundle of ten tens –</li> </ul>	<ul> <li>value of a digit based on its position in a</li> </ul>	• Representing 3 digit numbers using models,	
called a "hundred".	multi-digit number	words, and numbers.	
• - The numbers 100, 200, 300, 400, 500, 600 700,	<ul> <li>Numbers can be represented using number</li> </ul>	<ul> <li>Identifying and understanding the value of</li> </ul>	
800, 900 refer to one, two, three, four, five, six,	names, base ten blocks, expanded form and	digits in the hundreds, tens, and ones places	
seven, eight, or nine hundreds (and 0 tens and 0	numerals.	• Skip-counting to 1000 by 5s, 10s and 100s.	
ones).	<ul> <li>Numbers can be compared using symbols</li> </ul>	• Identify the hundreds, tens and ones place in a	
• 2.NBT.A.2. Count within 1000; skip-count by 5s,	• The number 100 can be thought of as a bundle	3 digit number.	
10s, and 100s.	of ten 10s.	Writing a 3-digit number using expanded	
• 2.NBT.A.3. Read and write numbers to 1000 using		notation.	
base-ten numerals, number names, and		• Comparing the value of two three-digit	
expanded form.		numbers.	
• 2.NBT.A.4. Compare two three-digit numbers			
based on meanings of the hundreds, tens, and			

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
Other Evidence: independent practice, classroom observations and discussions		

#### Title of Curriculum: Grade 3 Mathematics

Unit Name	What (content, vocab)	Why (enduring understandings)	How (skills)
Multiplication and Division	<ul> <li>Multiplication</li> <li>Repeated addition</li> <li>Relationship between multiplication and division</li> <li>Equal groups</li> <li>Array</li> <li>Commutative Property</li> <li>Associative Property</li> <li>Distributive Property</li> <li>Identity Property</li> <li>Zero Property</li> <li>Patterns</li> <li>Factors</li> <li>Products</li> <li>Unknown</li> <li>Equation</li> <li>Operation</li> </ul>	<ul> <li>There are many strategies for multiplication including repeated addition of equal groups, arrays and patterns for modeling</li> <li>Division can be represented by fair share or equal groups situations.</li> <li>Unknowns can be used in all positions when solving problems.</li> <li>Multiplication and division have an inverse relationship and can be used to solve problems and check answers.</li> </ul>	<ul> <li>Use repeated addition of equal groups to multiply.</li> </ul>
Multiplication & Division Math Fact Fluency		<ul> <li>Automaticity of multiplication facts 0-10 is beneficial when learning other computations in mathematics.</li> </ul>	<ul> <li>Use multiplication facts to solve division facts.</li> <li>Show a mastery of all multiplication facts 0 to 10 with accuracy and fluency</li> </ul>
Place Value	<ul> <li>Ones, tens, hundreds, thousands</li> <li>Round</li> <li>Estimate</li> <li>Multiples</li> </ul>	<ul> <li>Understanding place value is an important strategy for developing proficiency in addition and subtraction.</li> </ul>	<ul> <li>Round numbers to nearest ten or hundred.</li> <li>Use rounding in estimating sums and differences.</li> </ul>

Fractions	<ul> <li>Numerator and denominator</li> <li>Equal parts</li> <li>Unit Fraction</li> <li>Fraction tiles/ fraction strips</li> <li>Number lines</li> <li>Equivalent fractions</li> <li>Same numerator</li> <li>Same denominator</li> <li>Whole numbers</li> <li>half inch</li> <li>Quarter inch</li> <li>Line plot</li> </ul>	<ul> <li>A fraction describes the division of a whole into equal parts. The denominator tells how many equal parts the whole is divided into. The numerator tells how many equal parts are indicated.</li> </ul>	<ul> <li>Use rounding and estimating to assess the reasonableness of an answer.se place value to multiply one-digit numbers by multiples of 10 in the range of 10 to 90</li> <li>Write or draw a fraction to represent a drawing or place on a number line</li> <li>Partition a shape into parts with equal areas and label those areas with fractions</li> <li>Draw a number line from 0 to 1, partition it into equal parts and label each part with a fraction.</li> <li>Compare fractions that have the same numerator or fractions that have the same denominator and use &lt;, &gt;, or = by reasoning about their size and using a visual model</li> <li>Generate simple equivalent fractions using a line plot or visual fraction model.</li> <li>Express same numerator and denominator as one whole</li> <li>Represent a unit fraction on a number line</li> <li>Recognize fractions as parts to the whole with an understanding of the numerator and denominator parts.</li> <li>Students will understand how to use a ruler to measure lengths to the nearest half and quarter inch.</li> </ul>
Measurement and Data: Time	<ul> <li>Minute hand</li> <li>Hour hand</li> <li>AM and PM</li> <li>5 minute intervals</li> <li>Half past</li> <li>Quarter past</li> <li>Quarter of</li> <li>1 minute intervals</li> </ul>	<ul> <li>Time can be measured using different units that are related to one another.</li> <li>The minute hand takes 5 minutes to move from one number to the next on a typical clock.</li> </ul>	<ul> <li>Tell time to the nearest minute.</li> <li>Solve problems using addition and subtraction of time intervals in minutes on a number line</li> </ul>

	<ul> <li>Elapsed time (shown on number line, clock, or paper)</li> </ul>		
Measurement and Data: Area and Perimeter	<ul> <li>Area</li> <li>Unit square</li> <li>Perimeter</li> <li>Square units</li> <li>Units</li> <li>Length x Width</li> <li>Distributive Property</li> </ul>	<ul> <li>Perimeter and area are attributes of plane figures.</li> <li>Area is application of multiplication</li> <li>Perimeter is an application of addition</li> <li>There is a distinct difference between area and perimeter and how they are measured.</li> </ul>	<ul> <li>Measure area by counting squares</li> <li>Find area of a rectangle by using multiplication</li> <li>Solve problems involving area of rectangles and perimeters of polygons.</li> <li>Use area models to represent the Distributive Property.</li> <li>Add to find areas of shapes that consist of non-overlapping rectangles.</li> <li>Find the perimeter of a polygon.</li> <li>When given the perimeter of a polygon and some side lengths, find an unknown side length.</li> <li>Show that different rectangles can have the same perimeter as well as that different rectangles can have the same area.</li> </ul>
Measurement and Data: Mass and Volume	<ul> <li>Liquid volume/ capacity</li> <li>Mass</li> <li>Grams and kilograms</li> <li>Milliliters and liters</li> </ul>	<ul> <li>Capacity is a measure of the amount of liquid a container can hold.</li> <li>Mass is a measure of the quantity of matter in an object. Weight and mass are different.</li> </ul>	<ul> <li>Measure and estimate liquid volumes and masses of objects using standard units.</li> <li>Solve one-step word problems involving any operation using mass and volume given in the same units.</li> </ul>
Geometry: Shapes and Attributes	<ul> <li>Polygon (closed shapes)</li> <li>Attributes</li> <li>Side</li> <li>Angle, vertex</li> <li>Parallel sides</li> <li>Quadrilateral</li> <li>Rectangle, square, rhombus, parallelogram, trapezoid</li> <li>Category/ Categorize</li> </ul>	<ul> <li>There are many types of quadrilaterals including rhombuses, rectangles, and squares.</li> <li>Shapes are categorized based on attributes they share.</li> </ul>	<ul> <li>Identify types of quadrilaterals by their attributes (rhombuses, rectangles, and squares as examples of quadrilaterals.)</li> <li>Categorize shapes based on attributes they share.</li> </ul>

Measurement and Data: Picture Graphs and Bar	<ul><li>Bar graph</li><li>Picture Graph</li></ul>	• Some problems can be solved by making, reading, and analyzing a	• Use bar graphs and picture graphs, to answer questions and solve problems.
Graphs	<ul><li>Data</li><li>Scale</li></ul>	graph.	• Draw a bar graph or picture graph, with given data.
	<ul><li>Key</li><li>Survey</li><li>Tally marks</li></ul>		<ul> <li>Generate measurement data by measuring lengths using rulers marked with halves and fourths of an inch.</li> </ul>

# Windham School District Curriculum Mathematics - Grade 3 Unit 1: Multiplication & Division

Stage 1 Desired Results			
<ul> <li>STABLISHED GOALS:</li> <li>Students will continue their study of mathematics. In this unit, tudents will represent and solve problems involving multiplication and division.</li> <li>Content Standards: <ul> <li>CCSS.MATH.CONTENT.3.OA.A.1: Interpret products of whole numbers, e.g., interpret 5 × 7 as the total number of objects in 5 groups of 7 objects each.</li> </ul> </li> <li>CCSS.MATH.CONTENT.3.OA.A.2: Interpret whole-number quotients of whole numbers, e.g., interpret 5. × 8 as the number of objects in each share when 56 objects are partitioned equally into 8 shares, or as a number of shares when 56 objects are partitioned into equal shares of 8 objects each.</li> </ul>	<ul> <li>Trans</li> <li>Students will be able to independently use thei</li> <li>understand what multiplication is and how</li> <li>understand what division is and how to rep</li> <li>solve multiplication and division facts using</li> <li>Mean</li> <li>ENDURING UNDERSTANDINGS</li> <li>There are many strategies for multiplication including repeated addition of equal groups, arrays and patterns for modeling</li> <li>Division can be represented by fair share or equal groups situations.</li> <li>Unknowns can be used in all positions when solving problems.</li> <li>Multiplication and division have an inverse</li> </ul>	r learning to to represent it. resent it. the strategies and properties.	
<ul> <li>CCSS.MATH.CONTENT.3.OA.A.3: Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.1</li> <li>CCSS.MATH.CONTENT.3.OA.A.4: Determine the unknown whole number in a multiplication or division equation relating three whole numbers.</li> <li>CCSS.MATH.CONTENT.3.OA.B.5: Apply properties of operations as strategies to multiply and divide.</li> </ul>	Acquise         problems and check answers.         Acquise         Students will understand         properties of multiplication: commutative, associative, and distributive.         relationship between multiplication and division	<ul> <li>ition</li> <li>Students will be skilled at</li> <li>Use repeated addition of equal groups to multiply.</li> <li>Use patterns to multiply with different factors.</li> </ul>	

<ul> <li>CCSS.MATH.CONTENT.3.OA.B.6: Understand division as an unknown-factor problem.</li> <li>CCSS.MATH.CONTENT.3.OA.C.7: Fluently multiply and divide within 100, using strategies such as the relationship between multiplication and division (e.g., knowing that 8 × 5 = 40, one knows 40 ÷ 5 = 8) or properties of operations. By the end of Grade 3, know from memory all products of two one-digit numbers.</li> <li>CCSS.MATH.CONTENT.3.OA.D.8: Solve two-step word problems using the four operations. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.</li> <li>CCSS.MATH.CONTENT.3.OA.D.9: Identify arithmetic patterns</li> </ul>	<ul> <li>multiplication is the number of objects in a number of equal groups.</li> </ul>	<ul> <li>Use strategies to multiply (e.g. manipulatives, pictures, other facts they know).</li> <li>Apply properties of operations as strategies to multiply and divide (Commutative, Distributive and Associative Property).</li> <li>Determine the unknown whole number in a multiplication or division equation</li> <li>Show mastery of all multiplication facts 0 to 10 with accuracy and fluency</li> <li>Use multiplication facts to solve division facts</li> <li>Solve one and two-step word problems</li> </ul>
(including patterns in the addition table or multiplication table), and explain them using properties of operations. Used in Content Area Standards		using all four operations <b>21<sup>st</sup> Century Skills</b>
		Problem solving
not applicable		<ul> <li>Communication</li> </ul>
	•	Perseverance

Stage 2 - Evidence		
Evaluative Criteria	Assessment Evidence	
ASSESSMENT: Written Assessments or Projects		
Other Evidence: independent practice, classroom observations and discussions		

## **Unit 2: Multiplication & Division Math Fact Fluency**

	Stage 1 Desired Results		
ESTABLISHED GOALS:	Transfer		
Students will continue their study of mathematics. In	Students will be able to independently use their lea	rning to	
this unit, students will fluently multiply and divide	Master multiplication facts within 100		
within 100.	Use multiplication to solve division facts		
	Мес	ning	
Content Standards:	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS	
<ul> <li>CCSS.MATH.CONTENT.3.OA.C.7: Fluently multiply and divide within 100, using strategies such as the relationship between multiplication and division (e.g., knowing that 8 × 5 = 40, one knows 40 ÷ 5 =</li> </ul>	• Automaticity of multiplication facts 0-10 is beneficial when learning other computations in mathematics.	• Why do we need to know math facts?	
8) or properties of operations. By the end of Grade	Acquisition		
3, know from memory all products of two	Students will understand	Students will be skilled at	
one-digit numbers.	<ul> <li>Multiplication facts 0 - 10</li> </ul>	• using multiplication facts to solve division facts.	
		<ul> <li>stating all multiplication facts 0 to 10 with</li> </ul>	
		accuracy and fluency	
Used in Content Area Standards		21 <sup>st</sup> Century Skills	
not applicable		Perseverance	
		Communication	

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
Other Evidence: independent practice, classroom observations and discussions		

# Windham School District Curriculum Mathematics - Grade 3 Unit 3: Place Value

	Stage I Desired Results		
ESTABLISHED GOALS:	Transfer		
Students will continue their study of mathematics. In	Students will be able to independently use their learning to		
this unit, students will use place value to add and	<ul> <li>Multiply one-digit numbers by multiples of 10 ir</li> </ul>	n the range of of 10 to 90	
subtract within 1,000. Students will round to the	<ul> <li>Estimate answers to check for accuracy and und</li> </ul>	lerstanding.	
nearest 10 and 100 and use that to estimate sums and	Мес	aning	
differences. Students will multiply single digit numbers	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS	
by multiples of 10 in the range of 10 - 90.	Understanding place value is an important	<ul> <li>Why is estimation useful?</li> </ul>	
	strategy for developing proficiency in addition	<ul> <li>How does place value affect estimation?</li> </ul>	
Content Standards:	and subtraction.	• Why is estimation used in our everyday lives?	
• CCSS.MATH.CONTENT.3.NBT.A.1: Use place value		<ul> <li>When is adding and subtraction two and</li> </ul>	
understanding to round whole numbers to the		three-digit numbers useful in our everyday	
nearest 10 or 100.		lives?	
• CCSS.MATH.CONTENT.3.NBT.A.2: Fluently add and		isition	
subtract within 1000 using strategies and	Students will understand	Students will be skilled at	
algorithms based on place value, properties of	• rounding of two-digit and three-digit whole	<ul> <li>multiplying one-digit whole numbers by</li> </ul>	
operations, and/or the relationship between	numbers .	multiples of 10 in the range 10 to 90.	
addition and subtraction.	• regrouping for multi-digit arithmetic.	<ul> <li>rounding numbers to the nearest ten or</li> </ul>	
CCSS.MATH.CONTENT.3.NBT.A.3: Multiply one-digit	• place value	hundred (up to 1,000)	
whole numbers by multiples of 10 in the range		<ul> <li>rounding when estimating sums and</li> </ul>	
10-90 (e.g., $9 \times 80$ , $5 \times 60$ ) using strategies based		differences.	
on place value and properties of operations.		<ul> <li>estimating to assess the reasonableness of their</li> </ul>	
		answers.	
		<ul> <li>regrouping when performing multi-digit</li> </ul>	
		arithmetic.	

		•	using place value to break large addition problems into smaller ones that are easier to add.
Used in Content Area Standards			21 <sup>st</sup> Century Skills
		•	Problem Solving
not applicable		•	Communication
		•	Perseverance

Stage 2 - Evidence		
Evaluative Criteria	Assessment Evidence	
	ASSESSMENT: Written Assessments or Projects	
OTHER EVIDENCE: independent practice, classroom observations and discussions		

## **Unit 4: Fractions**

Stage 1	Desired Results	
ESTABLISHED GOALS:	Transj	fer
Students will continue their study of mathematics. In this unit, students will recognize the relationship between parts and whole. Students will write and represent fractions using pictures, number lines and other visual tools. Students will be able to compare fractions of the same size whole.	<ul> <li>Students will be able to independently use f</li> <li>Explain how numbers are fractions</li> <li>Expand their knowledge of a number line</li> </ul>	
Constant Chan develop	Meani	<b>,</b>
<ul> <li>Content Standards:</li> <li>CCSS.MATH.CONTENT.3.NF.A.1: Understand a fraction 1/b as the quantity formed by 1 part when a whole is partitioned into b equal parts; understand a fraction a/b as the quantity formed by a part of size 1/b.</li> <li>CCSS.MATH.CONTENT.3.NF.A.2: Understand a fraction as a number on the number line; represent fractions on a number line diagram.</li> </ul>	• A fraction describes the division of a whole into equal parts. The	<ul> <li>ESSENTIAL QUESTIONS</li> <li>How is a fraction related to a whole?</li> </ul>
• CCSS.MATH.CONTENT.3.NF.A.2.A: Represent a fraction 1/b on a number	Acquisi	tion
	<ul> <li>Students will understand</li> <li>a fraction is a quantity formed when a part of a whole is divided into equal parts.</li> <li>a fraction is made up of equal parts.</li> <li>equivalent fractions</li> <li>Numerator and denominator</li> <li>Equal parts</li> <li>Unit Fraction</li> <li>Fraction tiles/ fraction strips</li> <li>Number lines</li> <li>Equivalent fractions</li> </ul>	<ul> <li>Students will be skilled at</li> <li>writing a fraction to represent a drawing or place on a number line.</li> <li>partitioning a shape into parts with equal areas and labeling those areas with fractions.</li> <li>drawing a number line from 0 to 1, partitioning it into equal parts and labeling each part with a fraction.</li> <li>drawing a number line with more than 1 whole, partitioning it into</li> </ul>

Stage 2 - Evidence		
Evaluative Criteria	Assessment Evidence	
	ASSESSMENT: Written Assessments or Projects	
OTHER EVIDENCE: independent practice, classroom observations and discussions		

### Unit 5: Time

	Stage 1 Desired Results	
ESTABLISHED GOALS:	Transf	er
Students will continue their study of mathematics.	nue their study of mathematics. Students will be able to independently use their learning to	
In this unit, students will tell and write time to the		
nearest minute. Students will solve problems	clocks.	
involving time intervals.	Meanii	ng
	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS
Content Standards:	• Time can be measured using different units that are	• Why is a clock designed the way it is?
<ul> <li>CCSS.MATH.CONTENT.3.MD.A.1: Tell and</li> </ul>	related to one another.	• How is time measured?
write time to the nearest minute and	• The minute hand takes 5 minutes to move from one	• How are problems related to time used in our
measure time intervals in minutes. Solve	number to the next on a typical clock.	everyday life?
word problems involving addition and	Acquisition	
	Students will understand	Students will be skilled at
	Fractions of time.	<ul> <li>telling time to the nearest minute.</li> </ul>
line diagram.	Minute hand	<ul> <li>Solving problems using time.</li> </ul>
	Hour hand	
	AM and PM	
	• 5 minute intervals	
	Half past	
	Quarter past	
	Quarter of	
	1 minute intervals	
	Elapsed time (shown on number line, clock, or paper)	
Used in Content Area Standards		21 <sup>st</sup> Century Skills
		Communication
not applicable		Perseverance

Stage 2 - Evidence		
Evaluative Criteria	Assessment Evidence	
	ASSESSMENT: Written Assessments or Projects	
OTHER EVIDENCE: independent practice, classroom observations and discussions		

### **Unit 6: Area & Perimeter**

Stage 1 Desired Results			
ESTABLISHED GOALS:	Transfer		
Students will continue their study of mathematics. In this unit,	Students will be able to independently use their learning to		
students will find the area and perimeter of given shapes.	explain the difference between perimeter and area		
	<ul> <li>solve real world problems involving the area perimeter.</li> </ul>		
Content Standards:			
• CCSS.MATH.CONTENT.3.MD.C.5: Recognize area as an attribute of	Meaning		
plane figures and understand concepts of area measurement.	ENDURING UNDERSTANDINGS ESSENTIAL QUESTIONS		
• CCSS.MATH.CONTENT.3.MD.C.5.A: A square with side length 1	• Perimeter and area are attributes of • How do we use area and perimeter in our		
unit, called "a unit square," is said to have "one square unit" of	plane figures. everyday lives?		
area, and can be used to measure area.	Area is application of multiplication		
CCSS.MATH.CONTENT.3.MD.C.5.B: A plane figure which can be	Perimeter is an application of		
covered without gaps or overlaps by <i>n</i> unit squares is said to have	addition		
an area of <i>n</i> square units.	There is a distinct difference		
CCSS.MATH.CONTENT.3.MD.C.6: Measure areas by counting unit	between area and perimeter and		
squares (square cm, square m, square in, square ft, and	how they are measured.		
improvised units).	Acquisition		
	Students will understand Students will be skilled at		
multiplication and addition.	• a unit square as a square with a side • measuring the area by counting squares.		
• CCSS.MATH.CONTENT.3.MD.C.7.A: Find the area of a rectangle	length of 1 unit <ul> <li>finding the area of a rectangle using</li> </ul>		
with whole-number side lengths by tiling it, and show that the	<ul> <li>area as a certain number of unit multiplication.</li> </ul>		
area is the same as would be found by multiplying the side	squares with no gaps or overlaps • solving real world problems involving the		
lengths.	Area area of rectangles and perimeters of		
• CCSS.MATH.CONTENT.3.MD.C.7.B: Multiply side lengths to find	Unit square polygons.		
areas of rectangles with whole-number side lengths in the context	Perimeter     using area models to represent the		
of solving real world and mathematical problems, and represent	Square units distributive property.		
	Units		

<ul> <li>whole-number products as rectangular areas in mathematical reasoning.</li> <li>CCSS.MATH.CONTENT.3.MD.C.7.C: Use tiling to show in a concrete case that the area of a rectangle with whole-number side lengths <i>a</i> and <i>b</i> + <i>c</i> is the sum of <i>a</i> × <i>b</i> and <i>a</i> × <i>c</i>. Use area models to represent the distributive property in mathematical reasoning.</li> <li>CCSS.MATH.CONTENT.3.MD.C.7.D: Recognize area as additive. Find areas of rectilinear figures by decomposing them into non-overlapping rectangles and adding the areas of the non-overlapping parts, applying this technique to solve real world problems.</li> <li>CCSS.MATH.CONTENT.3.MD.D.8: Solve real world and mathematical problems involving perimeters of polygons, including finding the perimeter given the side lengths, finding an unknown side length, and exhibiting rectangles with the same perimeter and different areas or with the same area and different perimeters.</li> </ul>	<ul> <li>model</li> <li>perimeter as the outside distance around a polygon.</li> </ul>	<ul> <li>using addition to find areas of shapes that consist of non-overlapping rectangles.</li> <li>finding the perimeter of a polygon.</li> <li>when given the perimeter of a polygon and some side lengths, finding an unknown side length.</li> <li>showing that different rectangles can have the same perimeter</li> <li>showing that different rectangles can have the same area</li> <li>finding the perimeter of a polygon.</li> </ul>
Used in Content Area Standards		21 <sup>st</sup> Century Skills
not applicable		<ul><li>Communication</li><li>Perseverance</li><li>Problem solving</li></ul>

Stage 2 - Evidence		
Evaluative Criteria	Assessment Evidence	
ASSESSMENT: Written Assessments or Projects		
OTHER EVIDENCE: independent practice, classroom observations and discussions		

# Windham School District Curriculum Mathematics - Grade 3 Unit 7: Mass & Volume

	Stage I Desileu Results	
ESTABLISHED GOALS:	Transfer	
Students will continue their study of mathematics. In	Students will be able to independently use their learning to	
this unit, students will use standard units to read and	<ul> <li>use standard units of measurement of mass and volume to solve problems.</li> </ul>	
write mass and volume measurements.		Meaning
<ul> <li>Content Standards:</li> <li>CCSS.MATH.CONTENT.3.MD.A.2: Measure and estimate liquid volumes and masses of objects using standard units of grams (g), kilograms (kg), and liters (l).1 Add, subtract, multiply, or divide to solve one-step word problems involving masses or volumes that are given in the same units, e.g., by</li> </ul>	<ul> <li>ENDURING UNDERSTANDINGS</li> <li>Capacity is a measure of the amount of liquid a container can hold.</li> <li>Mass is a measure of the quantity of matter in an object. Weight and</li> </ul>	<ul> <li>ESSENTIAL QUESTIONS</li> <li>Why is measurement important in our lives?</li> <li>How is measurement used and shared around the world?</li> </ul>
	mass are different. Acquisition	
using drawings (such as a beaker with a measurement scale) to represent the problem.	<ul> <li>Students will understand</li> <li>mass, volume, and length.</li> <li>appropriate units to use when measuring mass and volume: grams, kilograms, liters</li> </ul>	<ul> <li>Students will be skilled at</li> <li>measuring liquid volumes and masses of objects using standard units of grams, kilograms and liters.</li> <li>estimating liquid volumes and masses of objects using standard units of grams, kilograms and liters.</li> <li>solving one-step word problems involving any operation using mass and volume given in the same units.</li> </ul>
Used in Content Area Standards		21 <sup>st</sup> Century Skills
not applicable		<ul><li>Communication</li><li>Perseverance</li><li>Problem solving</li></ul>

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
OTHER EVIDENCE: independent practice, classroom observations and discussions		

## **Unit 8: Geometry Shapes & Attributes**

	Stage I Desired Results		
ESTABLISHED GOALS:	Transfer		
Students will continue their study of	Students will be able to independently use their learning to		
mathematics. In this unit, students will be	<ul> <li>distinguish quadrilaterals based on their attributes.</li> </ul>		
able to identify and classify quadrilaterals	• Categorize shapes based on shared attributes.		
based on their attributes.	Ме	aning	
<ul> <li>Content Standards:</li> <li>CCSS.MATH.CONTENT.3.G.A.1: Understand that shapes in different categories (e.g., rhombuses, restanded at here) may share</li> </ul>	<ul> <li>ENDURING UNDERSTANDINGS</li> <li>There are many types of quadrilaterals including rhombuses, rectangles, and squares.</li> <li>Shapes are categorized based on attributes they share.</li> </ul>	<ul> <li>ESSENTIAL QUESTIONS</li> <li>How can two-dimensional shapes be described, analyzed and classified?</li> <li>Why is a square always a rectangle, but a rectangle isn't always a square?</li> </ul>	
rectangles, and others) may share attributes (e.g., having four sides), and		How does math define different shapes in our world?	
that the shared attributes can define a			
that the shared attributes can define a larger category (e.g., quadrilaterals). Recognize rhombuses, rectangles, and squares as examples of quadrilaterals, and draw examples of quadrilaterals that do not belong to any of these subcategories.	<ul> <li>Students will understand</li> <li>shapes and their attributes (i.e. angles, lines, sides).</li> <li>hierarchical way for defining shapes into larger categories (i.e. quadrilaterals) and subcategories (such as rectangles).</li> <li>Polygon (closed shapes)</li> <li>Attributes</li> <li>Side</li> <li>Angle, vertex</li> <li>Parallel sides</li> <li>Quadrilateral</li> <li>Rectangle, square, rhombus, parallelogram, trapezoid</li> <li>Category/ Categorize</li> </ul>	<ul> <li>Students will be skilled at</li> <li>recognizing rhombuses, rectangles and squares as examples of quadrilaterals.</li> <li>drawing quadrilaterals that do not belong to any special subcategories of quadrilaterals (such as rhombuses, rectangles and squares).</li> <li>categorizing shapes based on their properties and attributes they share</li> </ul>	

Used in Content Area Standards	21 <sup>st</sup> Century Skills
	Communication
not applicable	Perseverance
	Problem solving

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
	ASSESSMENT: Written Assessments or Projects	
OTHER EVIDENCE: independent practice, classroom observations and discussions		

## Unit 9: Measurement & Data - Picture Graphs & Bar Graphs

	Stage 1 Desired Results		
ESTABLISHED GOALS:	Transfer		
Students will continue their study of	Students will be able to independently use their learning to		
mathematics. In this unit, students will create	<ul> <li>read and understand graphs and what they represent.</li> </ul>		
graphs to show data. Students will analyze and	• compare data using a graph setting.		
interpret pictures and bar graphs.		Meaning	
	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS	
Content Standards:	<ul> <li>Some problems can be solved by making,</li> </ul>	• How can we use graphs to represent and show data?	
CCSS.MATH.CONTENT.3.MD.B.3: Draw a	reading, and analyzing a graph.	How can understanding (interpreting) pictures and bar	
scaled picture graph and a scaled bar		graphs help us to understand real world data?	
graph to represent a data set with several		Acquisition	
categories. Solve one- and two-step "how	Students will understand	Students will be skilled at	
many more" and "how many less"	Bar graph	Use bar graphs and picture graphs, to answer questions	
problems using information presented in	Picture Graph	and solve problems.	
scaled bar graphs.	• Data	• Draw a bar graph or picture graph, with given data.	
	• Scale	Generate measurement data by measuring lengths	
	• Key	using rulers marked with halves and fourths of an inch.	
	Survey		
	Tally marks		
Used in Content Area Standards		21 <sup>st</sup> Century Skills	
not applicable		Communication	
		Perseverance	
		Problem solving	
		Critical Thinking	

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
OTHER EVIDENCE: independent practice, classroom observations and discussions		

#### Title of Curriculum: Grade 4 Mathematics

Unit Name	What (content, vocab)	Why (enduring understandings)	How (skills)
Place Value	<ul> <li>Round</li> <li>Compare</li> <li>Periods (ones, thousands etc.)</li> <li>Determine operation</li> <li>Break down (steps)</li> <li>Estimate to check</li> </ul>	<ul> <li>Place value is based on groups of ten and helps to organize our number system.</li> <li>Place value can be used to compare and order numbers.</li> </ul>	<ul><li>standard, and word form</li><li>Round whole numbers to any place</li></ul>
Multi-digit Addition and Subtraction	<ul> <li>Line up place value</li> <li>Regroup</li> <li>Determine operation</li> <li>Break down (steps)</li> <li>Estimate to check</li> </ul>	<ul> <li>Place value, properties of operations, and the relationship between addition and subtraction can be used in fluently adding &amp; subtracting whole numbers</li> <li>Operations with whole numbers can be used to solve word problems.</li> </ul>	<ul> <li>lining up numbers before adding/subtracting</li> <li>adding multi digit number with regrouping</li> <li>using borrowing when subtracting</li> <li>identifying whether a word problem requires addition or subtraction</li> </ul>
Multi-digit Multiplication and Division	<ul> <li>Different algorithms</li> <li>Inverse operations</li> <li>Equations</li> <li>Rectangular arrays</li> <li>Area models</li> <li>Determine operation</li> <li>Break down (steps)</li> <li>Estimate to check</li> </ul>	<ul> <li>Multiplication and division have an inverse relationship. The inverse relationship between multiplication and division can be used to solve problems.</li> <li>When dividing the remainder must be less than the divisor. The nature of the question</li> </ul>	<ul><li>one-digit whole number</li><li>Multiply two two-digit numbers</li><li>Demonstrate that multiplication is the inverse</li></ul>

Factors and Multiples	<ul> <li>factor and multiple</li> <li>prime and composite</li> <li>a whole number as a product of each of its factors.</li> <li>1 is neither prime nor composite.</li> </ul>	<ul> <li>asked determines how to interpret and use the remainder.</li> <li>Each estimation technique gives a way to replace numbers with other numbers that are close and easy to compute with mentally.</li> <li>Every counting number is divisible by 1 and itself.</li> <li>Some counting numbers are divisible by numbers beyond 1 and itself.</li> <li>The product of any nonzero number and any other nonzero number is divisible by each number and called a multiple of each number.</li> </ul>	
Algebra: Patterns	<ul> <li>Predictable</li> <li>Numerical/Geometrical</li> <li>Rules</li> <li>Determine operation</li> </ul>	<ul> <li>Relationships can be described and generalizations made for mathematical situations that have numbers or objects that repeat in predictable ways.</li> <li>Some patterns consist of shapes or numbers that are arranged in a unit that repeats.</li> </ul>	<ul> <li>Assess the reasonableness of answers</li> <li>extending a given pattern.</li> <li>writing a rule for a given pattern.</li> <li>identifying the features of a pattern.</li> <li>creating a pattern</li> <li>Naming a pattern's rule.</li> </ul>

		<ul> <li>Some sequences have patterns that can be described using mathematical rules.</li> <li>Some real-world quantities have a mathematical relationship; the value of one quantity can be found if you know the value of another quantity.</li> </ul>	
Fractions and Decimals	<ul> <li>The same fractional amount can be represented by an infinite set of different but equivalent fractions.</li> <li>Benchmark fractions such as ½ are useful when comparing two fractions to each other.</li> <li>Fractions can be built from unit fractions by applying and extending understandings of operations on whole numbers.</li> <li>There is an equivalence between fractions and decimals.</li> </ul>	<ul> <li>The same fractional amount can be represented by an infinite set of different but equivalent fractions.</li> <li>Benchmark fractions such as ½ are useful when comparing two fractions to each other.</li> <li>Fractions can be built from unit fractions by applying and extending understandings of operations on whole numbers.</li> <li>There is an equivalence between fractions and decimals.</li> </ul>	<ul> <li>Use models and pictures to show fraction addition and subtraction</li> </ul>

Measurement & Data: Conversion and Area/Perimeter	<ul> <li>Systems of measurement</li> <li>Relative units</li> <li>Measurement equivalence</li> <li>Area and perimeter</li> <li>Formulas for rectangles</li> <li>Determine operation</li> <li>Break down (steps)</li> <li>Estimate to check</li> </ul>	<ul> <li>Some attributes of objects are measurable and can be quantified using unit amounts.</li> <li>Time can be expressed using different units that are related to each other.</li> <li>Some problems can be solved by applying the formula for the perimeter of a rectangle or the formula for the area of a rectangle.</li> </ul>	<ul> <li>Solve fraction addition and subtraction using a line plot</li> <li>finding area and perimeter using formulas.</li> <li>applying area and perimeter in real world problems.</li> <li>solving problems related to the addition and subtraction of time in minutes.</li> <li>finding elapsed time.</li> <li>using strategies such as a number line to solve problems relating to time intervals.</li> <li>showing measurement data on a line plot and draw a horizontal scale using whole numbers, halves, and quarters.</li> </ul>
Measurement & Data: Lines and Angles	<ul> <li>Formed by two rays common endpoint</li> <li>Fraction of a circle</li> <li>Angle represents turn</li> <li>Lines, line segments, and rays</li> <li>Right, acute, and obtuse</li> <li>Symmetry</li> <li>Determine operation</li> <li>Break down (steps)</li> <li>Estimate to check</li> </ul>	<ul> <li>Line segments and rays are sets of points that describe parts of lines, shapes and solids.</li> <li>Angles are formed by two intersecting lines or by rays with a common endpoint and are classified by size.</li> </ul>	<ul> <li>Measure angles with a protractor</li> <li>Represent an angle measurement as a fraction of a circle (over 360)</li> <li>Draw an angle with a given measurement</li> <li>Find unknown angle using addition and subtraction</li> <li>Identify points, lines, line segments, rays, perpendicular, and parallel lines.</li> <li>Identify right, acute, and obtuse angles.</li> <li>Identify right triangles</li> <li>Classify two-dimensional figures based on parallel and perpendicular lines</li> <li>Identify and draw lines of symmetry on two-dimensional figures</li> <li>Use multiple strategies to solve problems</li> <li>Assess the reasonableness of answers</li> </ul>

## **Unit 1: Place Value**

	Stage 1 Desired Results		
ESTABLISHED GOALS:	Transfer		
Students will continue their study of mathematics. In	Students will be able to independently use their learning to		
this unit, students will use place value to read, write,	<ul> <li>read multi digit numbers from 1,000-1,000,000.</li> </ul>		
compare and round whole numbers to a given place.	• compare two multi digit numbers from 1,000-1,000,000.		
	Меа	ning	
	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS	
• CCSS.MATH.CONTENT.4.NBT.A.1: Recognize that in	• Place value is based on groups of ten and helps	<ul> <li>How is our number system organized?</li> </ul>	
a multi-digit whole number, a digit in one place	to organize our number system.	• How does the position of a digit in a number	
represents ten times what it represents in the	• Place value can be used to compare and order	affect its value?	
place to its right. For example, recognize that 700 ÷	numbers.	<ul> <li>In what ways can numbers be composed and</li> </ul>	
70 = 10 by applying concepts of place value and		decomposed?	
division.		<ul> <li>When can rounding be useful and in what</li> </ul>	
		situations should we not round?	
CCSS.MATH.CONTENT.4.NBT.A.2: Read and write     multi digit whole numbers using base ten			
multi-digit whole numbers using base-ten	Acqui		
		Students will be skilled at	
Compare two multi-digit numbers based on	• That a digit in one place represents ten times	Regroup numbers to the next place value	
meanings of the digits in each place, using >, =, and < symbols to record the results of	what it represents in the place to its right.	• Write a multi-digit whole number in expanded,	
	Base-ten numerals, number names, and	standard, and word form	
comparisons.	expanded form.	Round whole numbers to any place	
<ul> <li>CCSS.MATH.CONTENT.4.NBT.A.3: Use place value understanding to round multi-digit whole numbers</li> </ul>	Round	Compare multi-digit whole numbers	
understanding to round multi-digit whole numbers		Read multi-digit numbers	
to any place.	<ul> <li>Periods (ones, thousands etc.)</li> </ul>	Order multi-digit numbers	
CCSS.MATH.CONTENT.4.OA.A.3: Solve multi-step	Determine operation	Use multiple strategies to solve problems	
word problems posed with whole numbers and	Break down (steps)	<ul> <li>Assess the reasonableness of answers</li> </ul>	
having whole-number answers using the four	Estimate to check		
operations, including problems in which			

<ul> <li>remainders must be interpreted. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.</li> <li>*Grade 4 expectations in this domain are limited to whole numbers less than or equal to 1,000,000.</li> </ul>	
Used in Content Area Standards	21 <sup>st</sup> Century Skills
not applicable	<ul><li>Problem solving</li><li>Communication</li><li>Perseverance</li></ul>

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
OTHER EVIDENCE: independent practice, classroom observations and discussions		

### **Unit 2: Multi-Digit Addition & Subtraction**

Stage 1 Desired Results		
ESTABLISHED GOALS:	Transfer	
Students will continue their study of mathematics. In	Students will be able to independently use their learning to	
this unit, students will fluently add and subtract	• Add and subtract multi-digit numbers from 1,000-1,0	00,000.
multi-digit whole numbers.	Meaning	
<ul> <li>Content Standards:</li> <li>CCSS.MATH.CONTENT.4.NBT.B.4: Fluently add and subtract multi-digit whole numbers using the standard algorithm.</li> <li>CCSS.MATH.CONTENT.4.OA.A.3: Solve multi-step word problems posed with whole numbers and having whole-number answers using the four</li> </ul>	• Place value, properties of operations, and the	<ul> <li>ESSENTIAL QUESTIONS</li> <li>Why is it important to be fluent in adding and subtracting multi-digit whole numbers?</li> </ul>
operations, including problems in which	Acquisitio	n
remainders must be interpreted. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.*Grade 4 expectations in this domain are limited to whole numbers less than or equal to 1,000,000.	<ul> <li>Students will understand</li> <li>Placement of the digits (line up the digits) when adding/subtracting</li> <li>That you add/subtract from right to left</li> <li>borrowing for subtracting</li> <li>regrouping for adding <ul> <li>Line up place value</li> <li>Regroup</li> <li>Determine operation</li> <li>Break down (steps)</li> <li>Estimate to check</li> </ul> </li> </ul>	<ul> <li>Students will be skilled at</li> <li>lining up numbers before adding/subtracting</li> <li>adding multi digit number with regrouping</li> <li>using borrowing when subtracting</li> <li>identifying whether a word problem requires addition or subtraction</li> </ul>
Used in Content Area Standards		21 <sup>st</sup> Century Skills
		Problem solving

not applicable	Communication
	Perseverance

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
OTHER EVIDENCE: independent practice, classroom observations and discussions		

### **Unit 3: Multi-Digit Multiplication & Division**

#### Stage 1 Desired Results

ESTABLISHED GOALS:	Transfer		
Students will continue their study of mathematics. In	Students will be able to independently use their learning to		
this unit, students will be able to multiply a whole	demonstrate the connection between multiplication and division.		
number (up to four digits) by a one digit whole number	<ul> <li>multiply multi-digit numbers</li> </ul>		
as well as two two digit numbers.	• divide 4 digit dividends by 1 digit divisors		
	Меа	ining	
Content Standards:	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS	
<ul> <li>CCSS.MATH.CONTENT.4.NBT.B.5: Multiply a whole number of up to four digits by a one-digit whole number, and multiply two two-digit numbers, using strategies based on place value and the properties of operations. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models.</li> <li>CCSS.MATH.CONTENT.4.NBT.B.6: Find whole-number quotients and remainders with up to four-digit dividends and one-digit divisors, using</li> </ul>	<ul> <li>Multiplication and division have an inverse relationship. The inverse relationship between multiplication and division can be used to solve problems.</li> <li>When dividing the remainder must be less than the divisor. The nature of the question asked determines how to interpret and use the remainder.</li> <li>Each estimation technique gives a way to replace numbers with other numbers that are</li> </ul>	<ul> <li>How can we use a model to show how the standard algorithm works?</li> <li>Why is place value important in all algorithms for multiplication?</li> </ul>	
strategies based on place value, the properties of	Acqui	isition	
<ul> <li>operations, and/or the relationship between multiplication and division. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models.</li> <li>CCSS.MATH.CONTENT.4.OA.A.3: Solve multi-step word problems posed with whole numbers and having whole-number answers using the four operations, including problems in which</li> </ul>		<ul> <li>Students will be skilled at</li> <li>multiplying with multiples of 10</li> <li>estimating products</li> <li>multiplying a whole number (up to four digits) by a one-digit whole number.</li> <li>multiplying two two-digit numbers.</li> </ul>	

remainders must be interpreted. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.	•	demonstrating that multiplication is the inverse of division. showing mastery of all division facts 0-9 with accuracy and fluency. finding whole-number quotients and remainders with up to four-digit dividends and one-digit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division.
Used in Content Area Standards		21 <sup>st</sup> Century Skills
	•	Problem solving
not applicable	•	Communication
	•	Perseverance

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
OTHER EVIDENCE: independent practice, classroom observations and discussions		

# Windham School District Curriculum Mathematics - Grade 4 Unit 4: Factors & Multiples

#### **Stage 1 Desired Results**

	Stage I Desired Results		
ESTABLISHED GOALS:	Transfer		
Students will continue their study of mathematics. In	Students will be able to independently use their learning to		
this unit, students will identify factors and multiples as	• Name factors and multiples of a given number.		
well as find prime and composite numbers.	<ul> <li>Identify prime and composite numbers.</li> </ul>		
	Ме	aning	
Content Standards:	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS	
CCSS.MATH.CONTENT.4.OA.B.4: Find all factor	• Every counting number is divisible by 1 and	<ul> <li>In what ways are factors and multiples</li> </ul>	
pairs for a whole number in the range 1-100.	itself.	connected and what is the difference between	
Recognize that a whole number is a multiple of	• Some counting numbers are divisible by	them?	
each of its factors. Determine whether a given	numbers beyond 1 and itself.		
whole number in the range 1-100 is a multiple of a	• The product of any nonzero number and any		
given one-digit number. Determine whether a	other nonzero number is divisible by each		
given whole number in the range 1-100 is prime or	number and called a multiple of each number.		
composite.			
CCSS.MATH.CONTENT.4.OA.A.3: Solve multistep	Acqu	isition	
word problems posed with whole numbers and	Students will understand	Students will be skilled at	
having whole-number answers using the four	<ul> <li>factor and multiple</li> </ul>	• Finding all factor pairs for a whole number in	
operations, including problems in which	<ul> <li>prime and composite</li> </ul>	the range 1 to 100	
remainders must be interpreted. Represent these	• a whole number as a product of each of its	• Recognizing that a whole number is a multiple	
problems using equations with a letter standing for	factors.	of each of its factors	
the unknown quantity. Assess the reasonableness	• 1 is neither prime nor composite.	• Determining whether a given whole number, in	
of answers using mental computation and		the range 0 to 100, is a multiple of a given	
estimation strategies including rounding.		one-digit number	
		• Determining whether a given whole number, in	
		the range 0 to 100, is prime or composite.	
		• Using factors and multiples to solve problems	

	<ul> <li>including finding equivalent fractions.</li> <li>Using multiple strategies to solve problems</li> <li>Assessing the reasonableness of answers</li> </ul>
Used in Content Area Standards	21 <sup>st</sup> Century Skills
	Communication
not applicable	Perseverance
	Critical Thinking

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
OTHER EVIDENCE: independent practice, classroom observations and discussions		

### **Unit 5: Algebra - Patterns**

Stage 1 Desired Results		
ESTABLISHED GOALS:	Transfer	
Students will continue their study of mathematics. In this unit, students will generate and analyze patterns.	<ul> <li>Students will be able to independently use their learning to</li> <li>Use patterns found in a sequence to solve real-world prob</li> <li>Meaning</li> </ul>	
<ul> <li>Content Standards:</li> <li>CCSS.MATH.CONTENT.4.OA.C.5: Generate a number or shape pattern that follows a given rule. Identify apparent features of the pattern that were not explicit in the rule itself.</li> <li>CCSS.MATH.CONTENT.4.OA.A.3: Solve multi-step word problems posed with whole numbers and having whole-number answers using the four operations,</li> </ul>	• Relationships can be described and generalizations made for mathematical situations that have numbers or objects that repeat in predictable ways.	<ul> <li>ESSENTIAL QUESTIONS</li> <li>How do patterns help us to make predictions and solve problems?</li> <li>How are geometric and numerical patterns similar and different from one another?</li> <li>How can we identify features of a pattern?</li> <li>How does understanding patterns help you understand relationships between numbers?</li> </ul>
including problems in which remainders	Acquisition Students will understand patterns can be predictable. difference between a numerical and geometric pattern. pattern rules.	<ul> <li>Students will be skilled at</li> <li>extending a given pattern.</li> <li>writing a rule for a given pattern.</li> <li>identifying the features of a pattern.</li> <li>creating a pattern</li> <li>Naming a pattern's rule.</li> </ul>
Used in Content Area Standards not applicable		<ul> <li>21<sup>st</sup> Century Skills</li> <li>Communication</li> <li>Perseverance</li> </ul>

	<ul><li>Critical thinking</li><li>Problem solving</li></ul>
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Stage 2 - Evidence	
Evaluative Criteria Assessment Evidence	
ASSESSMENT: Written Assessments or Projects	
OTHER EVIDENCE: independent practice, classroom observations and discussions	

# Windham School District Curriculum Mathematics - Grade 4 Unit 6: Fractions/Decimals

<ul> <li>example, express 3/10 as 30/100, and add 3/10 + 4/100 = 34/100.</li> <li>CCSS.MATH.CONTENT.4.NF.C.6: Use decimal notation for fractions with denominators 10 or 100. For example, rewrite 0.62 as 62/100; describe a length as 0.62 meters; locate 0.62 on a number line diagram.</li> <li>CCSS.MATH.CONTENT.4.NF.C.7: Compare two decimals to hundredths by reasoning about their size. Recognize that comparisons are valid only when the two decimals refer to the same whole. Record the results of comparisons with the symbols &gt;, =, or &lt;, and justify the conclusions, e.g., by using a visual model.</li> <li>CCSS.MATH.CONTENT.4.NF.B.4: Apply and extend previous understandings of multiplication to multiply a fraction by a whole number.</li> <li>CCSS.MATH.CONTENT.4.NF.B.4.A: Understand a fraction a/b as a multiple of 1/b. For example, use a visual fraction model to represent 5/4 as the product 5 × (1/4), recording the conclusion by the equation 5/4 = 5 × (1/4).</li> <li>CCSS.MATH.CONTENT.4.NF.B.4.B: Understand a multiple of a/b as a multiple of 1/b, and use this understanding to multiply a fraction by a whole number. For example, use a visual fraction model to express 3 × (2/5) as 6 × (1/5), recognizing this product as 6/5. (In general, n × (a/b) = (n × a)/b.)</li> <li>CCSS.MATH.CONTENT.4.NF.B.4.C: Solve word problems involving multiplication of a fraction by a whole number, e.g., by using visual fraction models and equations to represent the problem. For example, use a visual fraction model to express 3 × (2/5) as 6 × (1/5), recognizing this product as 6/5. (In general, n × (a/b) = (n × a)/b.)</li> </ul>	<ul> <li>Why is a hundredth smaller than a tenth when a hundred is bigger than a ten?</li> <li>How are decimals related to fractions?</li> <li>Acquisition</li> <li>addition and subtraction of fractions as joining and separating parts referring to the same whole.</li> <li>fractions with the same denominator can be decomposed into a sum of fractions in more than one way.</li> <li>fractions can be expressed as a multiple of a whole number and fraction</li> <li>when two fractions are equivalent.</li> <li>benchmark fractions</li> <li>numerators and denominators</li> <li>place value system for decimals up to the thousandths place.</li> <li>solving value system for decimals up to the thousandths place.</li> <li>when two fractions are equivalent.</li> <li>benchmark fractions</li> <li>numerators and denominators</li> <li>place value system for decimals up to the thousandths place.</li> <li>when two fractions are equivalent.</li> <li>comparing fractions with like and unlike denominators</li> <li>using visual models to compare fractions.</li> <li>using visual models to compare fractions.</li> <li>identifying the relationship of "10 times as much" and "1/10 of" in multi-digit numbers within our place value system.</li> </ul>
multiplication of a fraction by a whole number, e.g., by using visual	as much" and "1/10 of" in multi-digit

will be 5 people at the party, how many pounds of roast beef will be needed? Between what two whole numbers does your answer lie?	<ul> <li>comparing decimals.</li> <li>identifying the place value of any digit in numbers 0.001 to 10,000,000.</li> <li>explaining the pattern in the number of zeroes and placement of the decimal point when a number is multiplied or divided by a power of 10.</li> <li>rounding decimals to the nearest tenths, hundredths, and thousandths.</li> </ul>
Used in Content Area Standards	21 <sup>st</sup> Century Skills
not applicable	<ul> <li>Communication</li> <li>Perseverance</li> <li>Problem solving</li> <li>Critical Thinking</li> </ul>

Stage 2 - Evidence	
Evaluative Criteria Assessment Evidence	
ASSESSMENT: Written Assessments or Projects	
OTHER EVIDENCE: independent practice, classroom observations and discussions	

### Unit 7: Measurement & Data - Conversion & Area/Perimeter

Stage 1 Desired Results			
ESTABLISHED GOALS:	Trar	nsfer	
Students will continue their study of mathematics. In	Students will be able to independently use their lea	Students will be able to independently use their learning to	
this unit, students will find equivalence in units of	• Understand when the different forms of measur	-	
measure as well as use measurement formulas to find	• Find equivalence in units of measure		
area/perimeter.	• Use different forms of measurement to solve rea	al-world problems	
		ining	
Content Standards:		ESSENTIAL QUESTIONS	
CCSS.MATH.CONTENT.4.MD.A.1: Know relative	• Some attributes of objects are measurable and	• What is the importance of measuring?	
sizes of measurement units within one system of	can be quantified using unit amounts.	<ul> <li>What is a system of measurement and why are</li> </ul>	
units including km, m, cm; kg, g; lb, oz.; l, ml; hr,	<ul> <li>Time can be expressed using different units that</li> </ul>		
min, sec. Within a single system of measurement,	are related to each other.	<ul> <li>What is the purpose of having more than one</li> </ul>	
express measurements in a larger unit in terms of	<ul> <li>Some problems can be solved by applying the</li> </ul>	unit of measurement within a system?	
a smaller unit. Record measurement equivalents in		<ul> <li>What are some real-world situations where we</li> </ul>	
a two-column table. For example, know that 1 ft is	formula for the area of a rectangle.	would use area and perimeter?	
12 times as long as 1 in. Express the length of a 4 ft		<ul> <li>How are area and perimeter related?</li> </ul>	
snake as 48 in. Generate a conversion table for feet		• How are area and perimeter related.	
and inches listing the number pairs (1, 12), (2, 24),	Acqui	isition	
(3, 36),	Students will understand	Students will be skilled at	
	Systems of measurement	• finding area and perimeter using formulas.	
<ul> <li>CCSS.MATH.CONTENT.4.MD.A.2: Use the four</li> </ul>	Relative units	<ul> <li>applying area and perimeter in real world</li> </ul>	
operations to solve word problems involving	Measurement equivalence	problems.	
distances, intervals of time, liquid volumes, masses	Area and perimeter	<ul> <li>solving problems related to the addition and</li> </ul>	
of objects, and money, including problems	<ul> <li>Formulas for rectangles</li> </ul>	subtraction of time in minutes.	
involving simple fractions or decimals, and	<ul> <li>Determine operation</li> </ul>	<ul> <li>finding elapsed time.</li> </ul>	
problems that require expressing measurements	<ul> <li>Break down (steps)</li> </ul>	<ul> <li>using strategies such as a number line to solve</li> </ul>	
given in a larger unit in terms of a smaller unit.	<ul> <li>Estimate to check</li> </ul>	problems relating to time intervals.	
Represent measurement quantities using diagrams			

Used in Content Area Standards	21 <sup>st</sup> Century Skills     Communication
having whole-number answers using the four operations, including problems in which remainders must be interpreted. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.	21 <sup>st</sup> Contury Skills
<ul> <li>such as number line diagrams that feature a measurement scale.</li> <li>CCSS.MATH.CONTENT.4.MD.A.3: Apply the area and perimeter formulas for rectangles in real world and mathematical problems. For example, find the width of a rectangular room given the area of the flooring and the length, by viewing the area formula as a multiplication equation with an unknown factor.</li> <li>CCSS.MATH.CONTENT.4.OA.A.3: Solve multi-step word problems posed with whole numbers and</li> </ul>	<ul> <li>showing measurement data on a line plot and drawing a horizontal scale using whole numbers, halves, and quarters.</li> </ul>

Stage 2 - Evidence	
Evaluative Criteria Assessment Evidence	
	ASSESSMENT: Written Assessments or Projects
OTHER EVIDENCE: independent practice, classroom observations and discussions	

### **Unit 8: Measurement & Data Lines & Angles**

S	tage 1 Desired Results	
<ul> <li>ESTABLISHED GOALS:</li> <li>Estudents will continue their study of mathematics. In this unit, tudents will understand concepts of angles and angle neasurement as well as understand and classify lines, angles, and hapes.</li> <li>Content Standards:</li> <li>CCSS.MATH.CONTENT.4.MD.C.5: Recognize angles as geometric shapes that are formed wherever two rays share a common endpoint, and understand concepts of angle is measurement:</li> <li>CCSS.MATH.CONTENT.4.MD.C.5.A: An angle is measured with reference to a circle with its center at the common endpoint of the rays, by considering the fraction of the circular arc between the points where the two rays intersect the circle. An angle that turns through 1/360 of a circle is called a "one-degree angle," and can be used to measure angles.</li> </ul>	Tran Students will be able to independently use th Find angle measurements and use them in Understand the connection between lines	n solving real-world problems s, angles, and circles. aning ESSENTIAL QUESTIONS • When measuring angles, why is it important to use the correct measuring tool? • How do angles relate to circles and
• CCSS.MATH.CONTENT.4.MD.C.5.B: An angle that turns through <i>n</i> one-degree angles is said to have an angle measure of <i>n</i>	Acqu	isition
<ul> <li>degrees.</li> <li>CCSS.MATH.CONTENT.4.OA.A.3: Solve multi-step word problems posed with whole numbers and having whole-number answers using the four operations, including problems in which remainders must be interpreted. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers</li> </ul>	<ul> <li>Students will understand</li> <li>angle is formed when two rays share a common endpoint.</li> <li>angles as a fraction of a circle.</li> <li>angles as turns.</li> <li>lines, line segments, and rays.</li> </ul>	<ul> <li>Students will be skilled at</li> <li>measuring angles with a protractor.</li> <li>representing an angle measurement as a fraction over 360.</li> <li>drawing an angle with a given measurement.</li> </ul>

<ul> <li>CCSS.MATH.CONTENT.4.G.A.1: Draw points, lines, line segments, rays, angles (right, acute, obtuse), and perpendicular and parallel lines. Identify these in two-dimensional figures.</li> <li>CCSS.MATH.CONTENT.4.G.A.2: Classify two-dimensional figures based on the presence or absence of parallel or perpendicular lines, or the presence or absence of angles of a specified size. Recognize right triangles as a category, and identify right triangles.</li> <li>CCSS.MATH.CONTENT.4.G.A.3: Recognize a line of symmetry for a two-dimensional figure as a line across the figure such that the figure can be folded along the line into matching parts. Identify line-symmetric figures and draw lines of symmetry.</li> </ul>	<ul> <li>right triangles</li> <li>line of symmetry means that a figure can be folded on a line into matching parts.</li> </ul>	<ul> <li>addition, subtraction, or sums of parts.</li> <li>identifying points, lines, line segments, rays, perpendicular, and parallel lines in two-dimensional figures.</li> <li>identify right, acute, and obtuse angles in two-dimensional figures.</li> <li>classifying two-dimensional figures based on parallel and perpendicular lines.</li> <li>identifying and drawing lines of symmetry in two-dimensional figures.</li> </ul>
not applicable		<ul> <li>Communication</li> <li>Perseverance</li> <li>Problem solving</li> <li>Critical Thinking</li> </ul>

Stage 2 - Evidence	
Evaluative Criteria Assessment Evidence	
	ASSESSMENT: Written Assessments or Projects
OTHER EVIDENCE: independent practice, classroom observations and discussions	

#### Title of Curriculum: 5th Grade Mathematics

Unit Name	What (content, vocab)	Why (enduring understandings)	How (skills)
Unit 1: Numbers and Operations: Place Value of Decimals; Adding and Subtracting Decimals	<ul> <li>place value system</li> <li>decimal places to thousandths</li> <li>exponents</li> <li>powers of 10</li> <li>decimal point placement</li> </ul>	<ul> <li>The Base Ten numeration system is a scheme for recording numbers using digits 0-9, groups of ten and place value.</li> <li>Place value patterns lead to a deeper understanding of decimal place value and increases the skill of reading and writing decimals.</li> <li>Place value can be used to compare and order whole numbers and decimals.</li> </ul>	<ul> <li>Identify the relationship between digits of a number in reference "10 times as much" and "1/10 of"</li> <li>Read and write decimals in standard, expanded and word form</li> <li>Identify place value</li> </ul>
Unit 2: Numbers and Operations: Multiplying Multi-digit Whole Numbers and Decimals	<ul> <li>place value</li> <li>regrouping</li> <li>multi-digit whole numbers</li> <li>array area model</li> <li>partial products</li> <li>product</li> <li>decimal operations</li> <li>decimal point placement</li> <li>standard multiplication algorithm</li> </ul>	<ul> <li>The standard multiplication algorithm involving decimals is an extension of the standard algorithm for multiplying whole numbers. Place value determines the placement of the decimal point in a product.</li> <li>The product of two decimals less than one is less than either factor.</li> </ul>	<ul> <li>Explain answers using words, rectangular arrays, and/or area models</li> <li>Multiply decimals to hundredths</li> <li>Check for reasonableness of answers using estimation</li> <li>Solve problems using multiplication of</li> </ul>
Unit 3: Numbers and Operations: Dividing Multi-digit Whole Numbers	<ul><li> divisor</li><li> dividend</li><li> quotient</li></ul>	<ul> <li>Using models can help students understand the standard</li> </ul>	Divide multi-digit whole numbers

and Decimals	decimal point placement	<ul> <li>algorithm for dividing whole numbers.</li> <li>Estimation techniques are beneficial when checking for reasonableness of answers.</li> <li>Dividing by 2-digit divisors is just an extension of the steps for dividing with 1-digit divisors.</li> <li>A number divided by a decimal can be represented as an equivalent calculation using place value to change the divisor to a whole number.</li> <li>Recognize the connection between multiplication and division of whole numbers</li> <li>Explain answers using words, rectangular arrays, and/or area models</li> <li>Check for reasonableness of answers using estimation</li> <li>Solve problems using division including decimals</li> <li>Divide decimals to hundredths</li> </ul>
Unit 4: Numbers and Operations: Adding and Subtracting Fractions and Mixed Numbers	<ul> <li>fractions</li> <li>fraction bar</li> <li>common denominator</li> <li>mixed number</li> <li>improper fraction</li> <li>equivalent fractions</li> <li>simplest form</li> </ul>	<ul> <li>The same fractional amount can be represented by an infinite set of different but equivalent fractions.</li> <li>A fraction in simplest form is when 1 is the only common factor of the numerator and denominator.</li> <li>A number line can be used to estimate fractions to the nearest half or whole fraction.</li> <li>All whole numbers can be represented as fractions.</li> <li>Fractional amounts greater than 1 can be represented using a whole number and a fraction.</li> <li>Add and subtract fractions with unlike denominators.</li> <li>Add and subtract mixed numbers</li> <li>Determine equivalent fractions</li> <li>Use estimation to check for reasonableness of answers</li> <li>Solve real world word problems using addition and subtraction of fractions and mixed numbers</li> </ul>
Unit 5: Numbers and Operations: Multiplying and Dividing Fractions and Mixed Numbers	<ul> <li>improper fraction</li> <li>mixed number</li> <li>equivalence</li> <li>simplest form</li> <li>area</li> </ul>	<ul> <li>When you multiply two fractions that are both less than 1, the product is smaller than either fraction.</li> <li>Multiply fractions with whole numbers</li> <li>Multiply mixed numbers</li> <li>Solve word problems involving multiplying fractions and/or mixed numbers</li> </ul>

	<ul> <li>inverse operations</li> <li>multiplication/division relationship</li> <li>reciprocal</li> </ul>	<ul> <li>One way to find the product of mixed numbers is to change the calculation to an equivalent one involving improper fractions.</li> <li>The inverse relationship between multiplication and division can be used to divide with fractions.</li> </ul>	<ul> <li>Find the area of a rectangle with fractional side lengths</li> <li>Compare the size of factors to the size of a product</li> <li>Solve real life word problems involving the division of whole numbers that give quotients of fractions or mixed numbers</li> <li>Divide unit fractions by whole numbers and whole numbers by unit fractions</li> <li>Explain answers using words, models and the relationship between multiplication and division</li> </ul>
Unit 6: Geometry and Data: Volume Concepts and Measurement Conversions	<ul> <li>volume</li> <li>cubic units</li> <li>formula</li> <li>base</li> <li>area</li> <li>unit cubes</li> <li>three-dimensional figure</li> <li>right rectangular prism</li> <li>solid figure</li> <li>measurement system</li> <li>conversions</li> <li>metric</li> <li>U.S. Customary</li> </ul>	<ul> <li>Many everyday objects closely approximate standard geometric solids.</li> <li>Volume is a measure of the amount of space inside a solid.</li> <li>Relationships exist that enable you to convert between units of measurements by multiplying or dividing.</li> </ul>	<ul> <li>Find the volume of a right rectangular prism by counting cubic units</li> <li>Find the volume of a right rectangular prism using a formula</li> <li>Create multiple solid figures given a common volume.</li> <li>Solve real world problems related to volume</li> <li>Find the volume of a solid figure formed by two right rectangular prisms</li> <li>Convert within a measurement system</li> <li>Solve multi-step, real world problems involving conversions within a measurement system</li> </ul>
Unit 7: Algebraic Thinking: Numerical Expressions	<ul> <li>grouping symbols</li> <li>parentheses, brackets, braces</li> <li>order of operations</li> <li>numerical expressions</li> </ul>	<ul> <li>There is an agreed upon order for which operations in a numerical expression are performed.</li> <li>Some mathematical phrases can be represented using mathematical expressions.</li> </ul>	<ul> <li>Simplify expressions involving parentheses, brackets, braces using order of operations</li> <li>Write simple expressions given verbal or word-form expressions</li> </ul>
Unit 8: Geometry and Data: Coordinate Plane and	<ul> <li>coordinate plane</li> <li>x-axis</li> </ul>	<ul> <li>Relationships can be described and generalizations made for</li> </ul>	Plot ordered pairs on a coordinate plane

Classifying Two-Dimensional Figures & Algebraic Thinking: Analyzing Patterns and Relationships	<ul> <li>y-axis</li> <li>origin</li> <li>coordinate</li> <li>ordered pair</li> <li>first support</li> </ul>	<ul> <li>mathematical situations that have numbers or objects that repeat in predictable ways.</li> <li>The coordinate system is a scheme that uses two</li> </ul>	<ul> <li>plane</li> <li>Represent real world problems involving the first quadrant of the coordinate plane</li> </ul>
	<ul> <li>first quadrant</li> <li>hierarchy</li> <li>properties/attributes</li> <li>categories/subcategories</li> <li>two-dimensional figures</li> </ul>	<ul> <li>perpendicular lines intersecting at a 0 to name the location of points on a plane.</li> <li>Mathematical relationships</li> </ul>	
	<ul> <li>classifying/grouping</li> <li>triangles by angles and by sides</li> <li>classifying quadrilaterals</li> <li>relationships between corresponding terms</li> </ul>	<ul> <li>represented by rules can also be represented by a graph of the rule. Ordered pairs that satisfy the rule can be used to graph the data.</li> <li>Two-dimensional figures can be</li> </ul>	<ul> <li>plane</li> <li>Explain the differences between the terms: axis, coordinate and ordered pairs</li> <li>Classify and group two-dimensional figures in a hierarchy based on properties</li> </ul>
	corresponding terms	<ul> <li>Two-dimensional figures can be classified in a hierarchy based on their properties.</li> </ul>	<ul> <li>Give all names for a given figure</li> <li>Name a common property of a group of figures</li> <li>Generate patterns given rules</li> <li>Identify relationships between corresponding terms</li> </ul>
			<ul> <li>Form ordered pairs from corresponding terms in two patterns and graph them on a coordinate plane</li> </ul>

# Windham School District Curriculum Mathematics - Grade 5 Unit 1: Numbers & Operations Place Value & Adding & Subtracting Decimals

Stage 1 Desired Results			
ESTABLISHED GOALS:	Tra	nsfer	
Students will continue their study in Mathematics in	Students will be able to independently use their learning to		
the area of Numbers and Operations. In this unit	<ul> <li>use knowledge of place value to manipulate null</li> </ul>	mbers using various operations to solve real-life word	
students will gain a deeper understanding about place	problems.		
value from millions to thousandths while mastering the	Мес	aning	
relationship between the different place values. They	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS	
will gain an understanding of how to add and subtract	• The Base Ten numeration system is a scheme	• How can you describe the relationship between	
decimals to the hundredths place.	for recording numbers using digits 0-9, groups	any two place-value positions?	
	of ten and place value.	<ul> <li>How can you use exponents to represent</li> </ul>	
Content Standards:	Place value patterns lead to a deeper	powers of 10?	
CCSS.5.NBT.2 Explain patterns in the number of	understanding of decimal place value and	<ul> <li>How do you represent whole numbers and</li> </ul>	
zeros of the product when multiplying a number	increases the skill of reading and writing	decimals?	
by powers of 10, and explain patterns in the	decimals.	How can you use place value to round decimals	
placement of the decimal point when a decimal is	• Place value can be used to compare and order	to a given place value?	
multiplied or divided by a power of 10. Use whole	whole numbers and decimals.	<ul> <li>How can you use base-ten blocks to model</li> </ul>	
number exponents to denote powers of 10.		decimal addition/subtraction?	
• CCSS.5.NBT.1. Recognize that in a multi-digit	Acquisition		
number, a digit in one place represents 10 times	Students will understand	Students will be skilled at	
as much as it represents in the place to its right	<ul> <li>place value system</li> </ul>	• identifying the relationship between digits of a	
and 1/10 of what it represents in the place to its	<ul> <li>decimal places to thousandths</li> </ul>	number in reference "10 times as much" and	
left.	• exponents	"1/10 of"	
• CCSS.5.NBT.3. Read, write, and compare decimals	<ul> <li>powers of 10</li> </ul>	<ul> <li>reading and writing decimals in standard,</li> </ul>	
to thousandths.	<ul> <li>decimal point placement</li> </ul>	expanded and word form	
		identifying place value	

<ul> <li>CCSS.5.NBT.4 Use place value understanding to round decimals to any place.</li> <li>CCSS.5.NBT.7. Add, subtract, multiply, and divide decimals to hundredths, using concrete models or drawings and strategies based on place value, properties, of operations, and/or the relationship between addition and subtractions; relate the strategy to a written method and explain the reasoning used.</li> <li>CCSS.MP5 Use appropriate tools strategically.</li> <li>CCSS.MP6 Attend to precision.</li> <li>CCSS.MP1 Make sense of problems and persevere in solving them. CCSS.MP4 Model with mathematics.</li> <li>CCSS.MP5 Use appropriate tools strategically.</li> <li>CCSS.MP5 Use appropriate tools strategically.</li> <li>CCSS.MP5 Use appropriate tools strategically.</li> </ul>	<ul> <li>Explaining patterns in the number of zeros and the placement of a decimal point when a number is multiplied or divided by a power 10</li> <li>rounding decimals</li> <li>comparing and ordering decimals</li> <li>Adding and subtracting decimals to hundredths</li> <li>Explaining and/or modeling answers</li> <li>Recognizing the connections between addition and subtraction of decimals</li> <li>Checking for reasonableness of answers using estimation</li> </ul>
repeated reasoning. Used in Content Area Standards	21 <sup>st</sup> Century Skills
	Critical thinking
	Communication

Stage 2 - Evidence		
Evaluative Criteria	Assessment Evidence	
	ASSESSMENT: Written Assessments or Projects	
	OTHER EVIDENCE: independent practice, classroom observations and discussions	

# Windham School District Curriculum Mathematics - Grade 5 Unit 2: Numbers & Operations Multiplying Whole Numbers & Decimals

	Stage 1 Desired Results	
ESTABLISHED GOALS:	Tra	nsfer
Students will continue their study in Mathematics in the	Students will be able to independently use their lea	rning to
area of Numbers and Operations. In this unit students	<ul> <li>use their knowledge of multiplying whole numb</li> </ul>	pers to multiply decimals and apply it to solving word
will master multi-digit multiplication of whole numbers	problems.	
and decimals.	Мес	aning
<ul> <li>Content Standards:</li> <li>CCSS.5.NBT.5. Fluently multiply whole numbers using the standard algorithm.</li> <li>CCSS.5.NBT.7. Add, subtract, multiply, and divide decimals to hundredths, using concrete models or drawings and strategies based on place value, properties, of operations, and/or the relationship between addition and subtractions; relate the strategy to a written method and explain the reasoning used.</li> <li>CCSS.MP4 Model with mathematics.</li> <li>CCSS.MP1 Make sense of problems and persevere in solving them. CCSS.MP4 Model with</li> </ul>	<ul> <li>ENDURING UNDERSTANDINGS</li> <li>The standard multiplication algorithm involving decimals is an extension of the standard algorithm for multiplying whole numbers. Place value determines the placement of the decimal point in a product.</li> <li>The product of two decimals less than one is less than either factor.</li> </ul>	area model) and a pattern to multiply a two digit number?
mathematics.	Acquisition	
CCSS.MP8 Look for and express regularity in	Students will understand	Students will be skilled at
repeated reasoning.	place value	multiplying multi-digit whole numbers fluently
	• regrouping	<ul> <li>solving multi-digit multiplication problems</li> </ul>

	<ul> <li>multi-digit whole numbers</li> <li>array area model</li> <li>partial products</li> <li>product</li> <li>decimal operations</li> <li>decimal point placement</li> <li>standard multiplication algorithm</li> </ul>	<ul> <li>explaining answers using words, rectangular arrays, and/or area models</li> <li>multiplying decimals to hundredths</li> <li>checking for reasonableness of answers using estimation</li> <li>solving problems using multiplication of decimals</li> </ul>
Used in Content Area Standards		21 <sup>st</sup> Century Skills
		Critical thinking
		Communication

Stage 2 - Evidence		
Evaluative Criteria	Assessment Evidence	
	ASSESSMENT: Written Assessments or Projects	
	OTHER EVIDENCE: independent practice, classroom observations and discussions	

# Windham School District Curriculum Mathematics - Grade 5 Unit 3: Numbers & Operations Dividing Whole Numbers & Decimals

Stage 1 Desired Results			
ESTABLISHED GOALS:	Trai	nsfer	
Students will continue their study in Mathematics in the Students will be able to independently use their learning to			
area of Numbers and Operations. In this unit students	• use their understanding of dividing decimals to	solve real-life word problems	
will master multi-digit division of whole numbers and	• gain a deeper understanding of estimation.		
will gain an understanding of how to divide decimals.	Мес	aning	
<ul> <li>Content Standards:</li> <li>CCSS.5.NBT.6. Find whole-number quotients of whole numbers with up to four-digit dividends and two-digit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division. Illustrate and explain the calculations by using equations, rectangular arrays, and/or area models.</li> <li>CCSS.5.NBT.7. Add, subtract, multiply, and divide decimals to hundredths, using concrete models or</li> </ul>	<ul> <li>ENDURING UNDERSTANDINGS</li> <li>Using models can help students understand the standard algorithm for dividing whole numbers.</li> <li>Estimation techniques are beneficial when checking for reasonableness of answers.</li> <li>Dividing by 2-digit divisors is just an extension of the steps for dividing with 1-digit divisors.</li> <li>A number divided by a decimal can be represented as an equivalent calculation using place value to change the divisor to a whole number.</li> </ul>		
drawings and strategies based on place value,	Acqu	isition	
	Students will understand	Students will be skilled at	
between addition and subtractions; relate the	• divisor	<ul> <li>dividing multi-digit whole numbers</li> </ul>	
strategy to a written method and explain the	dividend	<ul> <li>recognizing the connection between</li> </ul>	
reasoning used.	• quotient	multiplication and division of whole numbers	
	decimal point placement	<ul> <li>explaining answers using words, rectangular arrays, and/or area models</li> </ul>	

<ul> <li>CCSS.MP1 Make sense of problems and persevere in solving them. CCSS.MP4 Model with mathematics.</li> <li>CCSS.MP4 Model with mathematics.</li> <li>CCSS.MP5 Use appropriate tools strategically.</li> <li>CCSS.MP6 Attend to precision.</li> <li>CCSS.MP8 Look for and express regularity in repeated reasoning.</li> </ul>	<ul> <li>checking for reasonableness of answers using estimation</li> <li>solving problems using division including decimals</li> <li>dividing decimals to hundredths</li> </ul>
Used in Content Area Standards	21 <sup>st</sup> Century Skills
	Critical thinking
	Communication

Stage 2 - Evidence	
Evaluative Criteria Assessment Evidence	
ASSESSMENT: Written Assessments or Projects	
OTHER EVIDENCE: independent practice, classroom observations and discussions	

## Windham School District Curriculum Mathematics - Grade 5 Unit 4: Numbers & Operations Adding & Subtracting Fractions & Mixed Numbers

Stage 1 Desired Results		
ESTABLISHED GOALS:	Tran	nsfer
Students will continue their study in Mathematics in	Students will be able to independently use their learn	ing to
the area of Number and Operations. In this unit	<ul> <li>use adding and subtracting fractions to solve word</li> </ul>	l problems
students will gain an understanding of how to add	<ul> <li>Use their increased knowledge base in number an</li> </ul>	d operations when learning algebraic skills.
and subtract fractions and mixed numbers with	Mear	ning
unlike denominators.	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS
<ul> <li>Content Standards:</li> <li>CCSS.5.NF.1. Add and subtract fractions with unlike denominators (including mixed numbers) by replacing given fractions with equivalent fractions in such a way as to produce an equivalent sum or difference of fractions with like denominators. For example, 2/3 +5/3 = 15/12 = 23/12. (In general, a/b + c/d = (ad + bc)/bd).</li> <li>CCSS.5.NF.2. Solve word problems involving addition and subtraction of fractions referring to the same whole, including cases of unlike</li> </ul>	<ul> <li>The same fractional amount can be represented by an infinite set of different but equivalent fractions.</li> <li>A fraction in simplest form is when 1 is the only common factor of the numerator and denominator.</li> <li>A number line can be used to estimate fractions to the nearest half or whole fraction.</li> <li>All whole numbers can be represented as fractions.</li> <li>Fractional amounts greater than 1 can be represented using a whole number and a fraction</li> </ul>	<ul> <li>How can you use models to add and subtract fractions that have different denominators?</li> <li>How can you use your knowledge of factors to rewrite a pair of fractions so they have a common denominator?</li> <li>Can you explain why the denominators are not combined?</li> <li>How can you use regrouping to find the sums and differences of two mixed numbers?</li> </ul>
denominators, e.g., by using visual fraction	Acquis	
	Students will understand	Students will be skilled at
Use benchmark fractions and number sense of	• fractions	Adding and subtracting fractions with unlike
fractions to estimate mentally and assess the	• fraction bar	denominators
reasonableness of answers. For example,	common denominator	<ul> <li>Adding and subtracting mixed numbers</li> </ul>

<ul> <li>recognize an incorrect result 2/5 + 1/2 = 3/7, by observing that 3/7 &lt; 1/2.</li> <li>CCSS.MP4 Model with mathematics.</li> <li>CCSS.MP5 Use appropriate tools strategically.</li> <li>CCSS.MP6 Attend to precision.</li> <li>CCSS.MP8 Look for and express regularity in repeated reasoning.</li> </ul>	<ul> <li>mixed number</li> <li>improper fraction</li> <li>equivalent fractions</li> <li>simplest form</li> </ul>	<ul> <li>Determining equivalent fractions</li> <li>Using estimation to check for reasonableness of answers</li> <li>Solving real world word problems using addition and subtraction of fractions and mixed numbers</li> </ul>
Used in Content Area Standards		<ul> <li>21<sup>st</sup> Century Skills</li> <li>Critical thinking</li> <li>Communication</li> <li>Technology literacy</li> </ul>

Stage 2 - Evidence	
Evaluative Criteria Assessment Evidence	
ASSESSMENT: Written Assessments or Projects	
OTHER EVIDENCE: independent practice, classroom observations and discussions	

### **Unit 5: Numbers & Operations - Multiplying & Dividing Fractions**

Stage 1 Desi	red Results
ESTABLISHED GOALS:	Transfer
Students will continue their study in Mathematics in the area of Numbers and	Students will be able to independently use their learning to
Operation. In this unit students will gain an understanding of how to multiply and	• use their knowledge of multiplying fractions and mixed numbers to
fractions and mixed numbers. They will also gain an understanding of how to	simplify expressions and solve equations
divide fractions using the reciprocal of a unit fraction.	<ul> <li>make a connection between multiplying and dividing fractions</li> </ul>
	Use their knowledge of number operations in real-life contexts
Content Standards:	Meaning
• CCSS.5.NF.4. Apply and extend previous understandings of multiplication to	ENDURING UNDERSTANDINGS ESSENTIAL QUESTIONS
multiply a fraction or whole number by a fraction.	When you multiply two fractions     How can you use modeling to
• CCSS.5.NF.5. Interpret multiplication as scaling (resizing), by:	that are both less than 1, the visualize the process of fraction
	product is smaller than either multiplication?
• CCSS.MATH.CONTENT.5.NF.B.5.A: Comparing the size of a product to the size	
of one factor on the basis of the size of the other factor, without performing	• One way to find the product of the fractional part of a quantity?
the indicated multiplication.	mixed numbers is to change the
CCSS.MATH.CONTENT.5.NF.B.5.B: Explaining why multiplying a given number	
by a fraction greater than 1 results in a product greater than the given	involving improper fractions.
number (recognizing multiplication by whole numbers greater than 1 as a	The inverse relationship between
familiar case); explaining why multiplying a given number by a fraction less	multiplication and division can be
than 1 results in a product smaller than the given number; and relating the principle of fraction equivalence $a/b = (n \times a)/(n \times b)$ to the effect of	used to divide with fractions.
multiplying $a/b$ by 1.	Acquisition
<ul> <li>CCSS.5.NF.6. Solve real world problems involving multiplication of fractions</li> </ul>	Students will understand Students will be skilled at
and mixed numbers, e.g., by using visual fraction models or equations to	improper fraction     Multiplying using fractions and
represent the problem.	mixed number     whole numbers as factors
<ul> <li>CCSS.5.NF.3. Interpret a fraction as division of the numerator by the</li> </ul>	equivalence     Multiplying using mixed numbers
denominator ( $a/b = a \div b$ ). Solve word problems involving division of whole	simplest form
	• area

Used in Content Area Standards		<ul> <li>21<sup>st</sup> Century Skills</li> <li>Critical thinking</li> <li>Communication</li> </ul>
<ul> <li>numbers leading to answers in the form of fractions or mixed numbers, e.g., by using visual fraction models or equations to represent the problem. For example, interpret <sup>3</sup>/<sub>4</sub> as the result of dividing 3 by 4, noting that <sup>3</sup>/<sub>4</sub> multiplied by 4 equals 3, and that when 3 wholes are shared equally among 4 people each person has a share of size <sup>3</sup>/<sub>4</sub>. If 9 people want to share a 50-pound sack of rice equally by weight, how many pounds of rice should each person get? Between what two whole numbers does your answer lie?</li> <li>CCSS.5.NF.7. Apply and extend previous understandings of division to divide unit fractions by whole numbers and whole numbers by unit fractions.</li> <li>CCSS.5.NF.B.7.C: Solve real world problems involving division of unit fractions, e.g., by using visual fraction models and equations to represent the problem. For example, how much chocolate will each person get if 3 people share <sup>1</sup>/<sub>4</sub> lb. of chocolate equally? How many 1/3-cup servings are in 2 cups of raisins?</li> <li>CCSS.MP1 Make sense of problems and persevere in solving them.</li> <li>CCSS.MP2 Reason abstractly and quantitatively.</li> <li>CCSS.MP5 Use appropriate tools strategically.</li> <li>CCSS.MP8 Look for and express regularity in repeated reasoning.</li> </ul>	<ul> <li>inverse operations</li> <li>multiplication/division relationship</li> <li>reciprocal</li> </ul>	<ul> <li>Solving word problems involving multiplying fractions and/or mixed numbers</li> <li>Finding the area of a rectangle with fractional side lengths</li> <li>Comparing the size of factors to the size of a product</li> <li>Solving real life word problems involving the division of whole numbers that give quotients of fractions or mixed numbers</li> <li>Dividing unit fractions by whole numbers and whole numbers by unit fractions</li> <li>Explaining answers using words, models and the relationship between multiplication and division</li> </ul>

Stage 2 - Evidence	
Evaluative Criteria Assessment Evidence	
ASSESSMENT: Written Assessments or Projects	
OTHER EVIDENCE: independent practice, classroom observations and discussions	

## Windham School District Curriculum **Mathematics - Grade 5 Unit 6: Geometry & Data Volume Concepts & Measurement Conversions**

Stage 1 Desired Results		
ESTABLISHED GOALS:	Tra	nsfer
Students will continue their study in Mathematics in the area of	Students will be able to independently use th	neir learning to
Geometry and Data. In this unit students will gain an understanding	<ul> <li>use their conceptual understanding of v</li> </ul>	olume to compare volumes of different solids
of volume as an attribute of solid figures and how to compute the	<ul> <li>apply their knowledge of measurement</li> </ul>	
volume of right rectangular prisms. Students will also be able to	<ul> <li>Apply their knowledge of geometry con-</li> </ul>	cepts in real life contexts
convert measurements within the metric or U.S. Customary systems.	Мес	aning
<ul> <li>Content Standards: CCSS.5.MD.1. Convert among different-sized standard measurement units within a given measurement system (e.g., convert 5 cm to 0.05m), and use these conversions in solving multi-step, real world problems.</li> <li>CCSS.5.MD.3. Recognize volume as an attribute of solid figures and understand concepts of volume measurement.</li> <li>CCSS.5.MD.4. Measure volumes by counting unit cubes, using cubic cm, cubic in, cubic ft., and improvised units.</li> <li>CCSS.5.MD.5. Relate volume to the operations of multiplication and addition and solve real world and CCSS.MP1 Make sense of problems and persevere in solving them.</li> <li>CCSS.MP3 Construct viable arguments and critique the reasoning of others.</li> <li>CCSS.MP6 Attend to precision.</li> <li>CCSS.MP7 Look for and make use of structure.</li> </ul>	<ul> <li>ENDURING UNDERSTANDINGS</li> <li>Many everyday objects closely approximate standard geometric solids.</li> <li>Volume is a measure of the amount of space inside a solid.</li> <li>Relationships exist that enable you to convert between units of measurements by multiplying or dividing.</li> </ul>	<ul> <li>ESSENTIAL QUESTIONS</li> <li>What is a unit cube and how can you use it to build a solid figure?</li> <li>How can you use unit cubes to find the volume of a right rectangular prism and cube?</li> <li>How can you use multiplication to find the volume of a right rectangular prism?</li> <li>How does the area of the base of a prism relate to the volume of a right rectangular prism?</li> <li>How can you compare and convert metric units using base ten multiplication and division knowledge?</li> <li>How can you compare and convert customary units of length, capacity, and weight?</li> </ul>

CCSS.MP8 Look for and express regularity in repeated	Acquisition	
reasoning. mathematical problems involving volume.	<ul> <li>Students will understand</li> <li>volume</li> <li>cubic units</li> <li>formula</li> <li>base</li> <li>area</li> <li>unit cubes</li> <li>three-dimensional figure</li> <li>right rectangular prism</li> <li>solid figure</li> </ul>	<ul> <li>Students will be skilled at</li> <li>Finding the volume of a right rectangular prism by counting cubic units</li> <li>Finding the volume of a right rectangular prism using a formula</li> <li>Creating multiple solid figures given a common volume.</li> <li>Solving real world problems related to volume</li> <li>Finding the volume of a solid figure formed by two right rectangular prisms</li> <li>Converting within a measurement system</li> <li>Solving conversions within a measurement system</li> </ul>
Used in Content Area Standards		21 <sup>st</sup> Century Skills
		<ul> <li>Critical thinking</li> <li>Communication</li> <li>Technology literacy</li> </ul>

Stage 2 - Evidence	
Evaluative Criteria Assessment Evidence	
ASSESSMENT: Written Assessments or Projects	
OTHER EVIDENCE: independent practice, classroom observations and discussions	

### **Unit 7: Algebraic Thinking - Numerical Expressions**

Stage 1 Desired Results		
ESTABLISHED GOALS:	Tr	ansfer
Students will continue their study in Mathematics in the area of	Students will be able to independently use	e their learning to
Algebraic Thinking. In this unit students will solve various expressions	<ul> <li>apply order of operations to more cor</li> </ul>	nplex algebraic expressions within algebra.
using order of operations.	M	eaning
<ul> <li>Content Standards:</li> <li>CCSS.5.OA.1. Use parentheses, brackets, or braces in numerical expressions, and evaluate expressions with these symbols.</li> <li>CCSS.5.OA.2. Write simple expressions that record calculations with numbers, and interpret numerical expressions without evaluating them. For example, express the calculation "add 8 and"</li> </ul>	<ul> <li>ENDURING UNDERSTANDINGS</li> <li>There is an agreed upon order for which operations in a numerical expression are performed.</li> <li>Some mathematical phrases can be represented using mathematical expressions.</li> </ul>	<ul> <li>ESSENTIAL QUESTIONS</li> <li>Why are parentheses, brackets and braces important in numerical expressions?</li> <li>How does the order of operations impact the answer?</li> </ul>
7, then multiply by 2" as 2 x (8 = 7). Recognize that 3 x (18932 +	•	uisition
<ul> <li>921) is three times as large as 18932 + 921, without having to calculate the indicated sum or product.</li> <li>CCSS.MP1 Make sense of problems and persevere in solving them.</li> <li>CCSS.MP2 Reason abstractly and quantitatively</li> <li>CCSS.MP6 Attend to precision.</li> <li>CCSS.MP7 Look for and make use of structure.</li> <li>CCSS.MP8 Look for and express regularity in repeated reasoning.</li> </ul>	Students will understand • grouping symbols	<ul> <li>Students will be skilled at</li> <li>Simplifying expressions involving parentheses, brackets, braces using order of operations</li> <li>Writing simple expressions given verbal or word-form expressions</li> </ul>
Used in Content Area Standards		21 <sup>st</sup> Century Skills
		<ul><li>Critical thinking</li><li>Communication</li></ul>

Stage 2 - Evidence	
Evaluative Criteria Assessment Evidence	
ASSESSMENT: Written Assessments or Projects	
OTHER EVIDENCE: independent practice, classroom observations and discussions	

# Windham School District Curriculum

### **Mathematics - Grade 5**

### Unit 8: Geometry & Data - Coordinate Plane, Classifying Two-Dimensional Figures, & Analyzing Patterns & Relationships

Stage 1 Desired Results		
ESTABLISHED GOALS:	Transfer	
Students will continue their study in Mathematics in the	Students will be able to independently use their learning to	
area of Geometry and Data. In this unit students will	• use their understanding of graphing ordered pairs to make connections to real life problems such	
learn about the Coordinate Plane and be able to graph	as map locations.	
points and solve real-world problems by graphing points.	<ul> <li>see how different figures exist in our world</li> </ul>	
Students will also be able to classify and identify	apply number patterns to the coordinate plane when creating lines on a graph.	
characteristics of two dimensional figures. Lastly,	Meaning	
students will analyze and identify different number	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS
patterns and apply them to real-life word problems.	Relationships can be described and	<ul> <li>How can you identify and plot points on a</li> </ul>
	generalizations made for mathematical	coordinate grid?
Content Standards:	situations that have numbers or objects that	• How can you use a coordinate grid to display
• CCSS.5.G.1. Use a pair of perpendicular number	repeat in predictable ways.	data?
lines, called axes, to define a coordinate system, with		How can you identify a relationship within the
the intersection of the lines (the origin) arranged to	two perpendicular lines intersecting at a 0 to	numerical patterns they generate?
coincide with the 0 on each line and a given point in	name the location of points on a plane.	<ul> <li>How can you classify and compare triangles and</li> </ul>
the plan located by using an ordered pair of	Mathematical relationships represented by	quadrilaterals?
numbers, called its coordinates. Understand that the		What types of relationships can occur between
first number indicates how far to travel from the	the rule. Ordered pairs that satisfy the rule	corresponding terms in two different numerical
origin in the direction of one axis, and the second	can be used to graph the data.	patterns?
number indicates how far to travel in the direction of		
the second axis, with the convention that the names	hierarchy based on their properties.	
of the two axes and the coordinates correspond	Acquisition	
(e.g., <i>x</i> -axis and <i>x</i> -coordinate, <i>y</i> -axis and <i>y</i> -	Students will understand	Students will be skilled at
coordinate).	coordinate plane	Plotting ordered pairs on a coordinate plane

Stage 2 - Evidence		
Evaluative Criteria	Assessment Evidence	
	ASSESSMENT: Written Assessments or Projects	
	Other Evidence: independent practice, classroom observations and discussions	

### Title of Curriculum: Grade 6 Mathematics

Unit Name	What		Why?		How
	(Content and Vocabulary)		(Enduring Understanding)		(skills)
Unit 1: Number and Operations: Ratios and Proportional Relationships	<ul> <li>Ratios</li> <li>Unit Rates</li> <li>Proportions</li> <li>Fraction, decimal, percent conversions</li> <li>Terminating and repeating decimals</li> <li>ratios as a fraction or percentage</li> <li>equivalent ratios</li> <li>a rate is a ratio involving units</li> <li>100% is all of the original amount</li> </ul>	•	A ratio or rate describes the relationship between two quantities. Ratio reasoning can be applied to many different types of mathematical and real-life problems A rate is a type of ratio that represents a measure or quantity. Therefore the process for solving ratio problems can be applied to rates.	• • • •	Simplify ratios Compare ratios in different formats Find equivalent ratios Calculate unit rate Find a missing number in a proportion Interchange fractions, decimals and percents Find percent of a quantity. Solve percent real world problems
Unit 2: Number and Operations: Fractions and Decimals	<ul> <li>Factors</li> <li>Multiples</li> <li>Place Value</li> <li>Reciprocal</li> <li>Dividend</li> <li>Divisor</li> <li>Quotient</li> <li>the value of a digit in relationship to its position in a number</li> </ul>	•	Multiplication and division are inverse operations. Operations on decimals and whole numbers are based upon place value relationships. Number lines are visual models used to represent the density principle: between any two whole numbers are many rational numbers, including decimals and fractions. The magnitude of numbers affects the outcome of operations on them. Computational fluency includes applying the most effective and efficient strategy when applicable.	•	Divide fractions by fractions Find common factors, greatest common factors, and multiples Add,subtract, multiply and divide mixed numbers Divide decimals
Unit 3: Numbers and	Integers	•	Positive and negative numbers are	•	Create a number line with integers
Operations - Integers	<ul><li>Rational Number</li><li>Absolute Value</li></ul>		used together to describe quantities having opposite directions or values		

	<ul> <li>Opposite</li> <li>Number Line</li> <li>Coordinate Plane</li> <li>X Axis</li> <li>Y Axis</li> <li>Reflection</li> <li>Horizontal</li> <li>Vertical</li> <li>absolute value as the distance away from zero on a number line</li> </ul>	<ul> <li>All rational numbers can be represented as a point on the number line.</li> <li>Students will understand that absolute value is the distance from zero on a number line.</li> <li>The coordinate plane can be used to describe location in two dimensions, defined by an ordered pair.</li> </ul>	<ul> <li>Understand the relationship between a positive or negative number and its opposite</li> <li>Find missing values in a situation</li> <li>Graph with positive and negative coordinates</li> </ul>
Unit 4: Algebraic Thinking - expressions	<ul> <li>Algebraic expressions</li> <li>Exponents</li> <li>Constant</li> <li>Coefficient</li> <li>Term</li> <li>Like Terms</li> <li>Variable</li> <li>Distributive Property</li> </ul>	<ul> <li>Expressions are powerful tools for exploring, reasoning about, and representing situations.</li> <li>Variables have many different meanings, depending on context and purpose.</li> <li>Variables permit writing expressions whose values are unknown or vary under different circumstances.</li> <li>Two or more expressions may be equivalent, even when their symbolic forms differ.</li> <li>Linear expressions may be added to or subtracted from one another.</li> </ul>	understandings of arithmetic to algebraic expressions, including whole number exponents
Unit 5: Algebraic Thinking: Equations	<ul> <li>Equations</li> <li>Inequalities</li> <li>Greater than</li> <li>Less than</li> <li>Greater than or equal to</li> <li>Less than or equal to</li> <li>Dependant Variable</li> </ul>	<ul> <li>Solving an equation is a process of answering a question by finding the value of the variable that makes the equation true.</li> <li>An equation is two equivalent expressions.</li> <li>Variables are used to represent two</li> </ul>	<ul> <li>Write an equation to express one quantity, the dependent variable, in terms of the other quantity, the independent variable.</li> <li>Write an equation from data tables and graphs</li> <li>Define a variable and create an equation</li> </ul>

	<ul> <li>Independent Variable</li> <li>Constant</li> <li>Coefficient</li> <li>Substitution</li> <li>Equivalent</li> </ul>	quantities in a real world problem that change in relationship to one another.	<ul> <li>and / or an inequality from a word problem</li> <li>Solve one step equations and inequalities</li> </ul>
Unit 6: Geometry and Data - Area and Surface Area	<ul> <li>Length</li> <li>Width</li> <li>Parallelogram</li> <li>Altitude</li> <li>Trapezoid</li> <li>Area as space inside a figure</li> <li>Area of a parallelogram A = bh</li> <li>Area of a triangle A = ½ bh</li> <li>Area of a trapezoid A = ½ (b1 + b2)h</li> <li>Units squared</li> <li>Net</li> <li>Surface Area</li> <li>Area</li> <li>Composite Figures</li> <li>Kite</li> <li>Compose</li> <li>decompose</li> <li>irregular shapes</li> <li>Two-dimensional figures</li> <li>three-dimensional figures</li> <li>faces, edges, vertices.</li> <li>Solid</li> <li>prism</li> <li>lateral surface area</li> <li>area is the surface inside a flat, closed figure.</li> </ul>	<ul> <li>The area of all 2-dimensional figures can be calculated by breaking irregular shapes into rectangles or triangles.</li> <li>A three-dimensional figure can be represented by two-dimensional nets, which can help determine the surface area of three-dimensional figures.</li> </ul>	<ul> <li>Draw a net for a given solid</li> <li>Calculate area of the irregular shapes</li> <li>Calculate area and surface area using models</li> <li>Fluently calculate area and surface area using formulas</li> <li>Calculate surface area of rectangular prisms</li> </ul>

Unit 7: Geometry and Data - Volume	<ul> <li>irregular shapes are the combination of multiple figures.</li> <li>nets are three-dimensional figures drawn on a surface.</li> <li>surface area is the sum of the areas of all faces.</li> <li>Polygon</li> <li>Polyhedron</li> <li>Edge</li> <li>Vertex</li> <li>Length</li> <li>Width</li> <li>Depth</li> <li>Cubic Units</li> <li>Formula: V=LWH or V=Bh</li> <li>Irregular Figures</li> <li>Prism</li> <li>volume as the space inside a solid.</li> </ul>	<ul> <li>Volume is the number of cubes that can fit inside of a solid.</li> <li>The generic formula for volume is the area of the base multiplied by the height.</li> </ul>	<ul> <li>Find volume by packing it with unit cubes of the appropriate unit fraction edge lengths (modeling)</li> <li>Identify faces, edges, and vertices</li> <li>Calculate volume using models</li> <li>Fluently calculate volume using formulas</li> <li>Solve real word problems involving volume</li> </ul>
Unit 8: Geometry and Data - Statistics and Probability	<ul> <li>Variability</li> <li>Data</li> <li>statistical questioning</li> <li>statistical process</li> <li>Sample</li> <li>bar graph</li> <li>Frequency</li> <li>Mode</li> <li>dot plot</li> <li>Distribution</li> <li>Symmetric</li> <li>Outliers</li> <li>Histogram</li> <li>Measure of center</li> <li>Median</li> </ul>	<ul> <li>A statistical question anticipates variability in the data related to the question and accounts for it in the answers.</li> <li>A set of data collected to answer a statistical question has a distribution, which can be described by its center, spread, and overall shape.</li> <li>A measure of center for a numerical data set summarizes all of its values with a single number, while a measure of variation describes how its values vary with a single number.</li> </ul>	<ul> <li>Create statistical questions</li> <li>Determine measures of central tendency</li> <li>Choose which measure of central tendency is appropriate for a given set of points</li> <li>Analyze data from a given dot plot, histogram, and box plots</li> <li>Report observations about data using mathematical vocabulary: giving quantitative measures of center (median and/or mean) and variability (interquartile range and/or mean absolute deviation),</li> </ul>

balance point	
Mean	
<ul> <li>measures of variation</li> </ul>	
Range	
Quartile	
<ul> <li>Interquartile range (IQR)</li> </ul>	
Box-and-whisker plot	
Deviation	
Absolute Deviation	
Mean Absolute Deviation	
misleading data	
statistical variability	

# Windham School District Curriculum Mathematics - Grade 6 Unit 1: Numbers & Operations Ratios & Proportional Relationships

Stage 1 Desired Results			
ESTABLISHED GOALS:	Transfer		
<ul> <li>ESTABLISHED GOALS:</li> <li>Students will continue their study of mathematics in the area of numbers and operations. In this unit, students will explore the concepts and ratios and proportions and how they relate to real-world applications.</li> <li><i>Content Standards:</i> <ul> <li>CCSS.6.RP.1. Understand the concept of a ratio and use ratio language to describe a ratio relationship between two quantities.</li> <li>CCSS.6.RP.2 Understand the concept of a unit rate a/b associated with a ratio a:b with b ≠ 0, and use rate language in the context of a ratio relationship.</li> <li>CCSS.6.RP.3. Use ratio and rate reasoning to solve</li> </ul> </li> </ul>	<ul> <li>Students will be able to independently use their lea         <ul> <li>apply their knowledge of ratios and proportions</li> <li>Med</li> </ul> </li> <li>ENDURING UNDERSTANDINGS</li> <li>A ratio or rate describes the relationship between two quantities.</li> </ul>	rning to	
real-world and mathematical problems, e.g., by reasoning about tables of equivalent ratios, tape diagrams, double number line diagrams, or	Students will understand • Ratios • Unit Rates	isition Students will be skilled at Simplifying ratios Comparing ratios in different formats Finding equivalent ratios Calculating unit rate Finding the missing number in a proportion.	

<ul> <li>CCSS.MP8 Look for and express regularity in repeated reasoning</li> </ul>	<ul> <li>equivalent ratios</li> <li>a rate is a ratio involving units</li> <li>100% is all of the original amount</li> <li>Numbers can be expressed in different formats based on a given situation.</li> </ul>	<ul> <li>Converting between fractions, decimals and percents</li> <li>Finding a missing percent</li> <li>Finding the percent of a quantity</li> <li>Solving percent word problems</li> </ul>
Used in Content A	rea Standards	21 <sup>st</sup> Century Skills
		<ul> <li>Critical Thinking</li> <li>Collaboration</li> <li>Communication</li> </ul>

Stage 2 - Evidence		
Evaluative Criteria	Assessment Evidence	
	ASSESSMENT: Written Assessments or Projects	
	OTHER EVIDENCE: independent practice, classroom observations and discussions	

### **Unit 2: Numbers & Operations - Fractions & Decimals**

Stage 1 Desired Results				
ESTABLISHED GOALS:	Trai	nsfer		
Students will continue their study of mathematics in the	Students will be able to independently use their lea	rning to		
area of numbers and operations. In this unit, students	• fluently add, subtract, multiply, and divide ration	nal numbers using the standard algorithm with speed		
will master fraction and decimal operations and apply	and accuracy without the use of math tools (cal	culator).		
them to real-life applications.	• apply their knowledge to real-life applications as	s well as future algebraic topics		
	Меа	ining		
Content Standards:	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS		
<ul> <li>CCSS.6.NS.1. Interpret and compute quotients of fractions, and solve word problems involving division of fractions by fractions.</li> <li>CCSS.6.NS.2. Fluently divide multi-digit numbers using the standard algorithm.</li> <li>CCSS.6.NS.3. Fluently add, subtract, multiply, and divide multi-digit decimals using the standard algorithm for each operation.</li> <li>CCSS.6.NS.4. Find the greatest common factor of the standard and the standard algorithm for each operation.</li> </ul>	<ul> <li>Multiplication and division are inverse operations.</li> <li>Operations on decimals and whole numbers are based upon place value relationships.</li> <li>Number lines are visual models used to represent the density principle: between any two whole numbers are many rational numbers, including decimals and fractions.</li> <li>The magnitude of numbers affects the outcome</li> </ul>	<ul> <li>the dividend or divisor?</li> <li>What is the relationship between a mixed number and an improper fraction?</li> <li>What strategies do you use to find equivalent fractions?</li> <li>What is the connection between fractions,</li> </ul>		
two whole numbers less than or equal to 100 and the least common multiple of two whole numbers less than or equal to 12. Use the distributive property to express a sum of two whole numbers	most effective and efficient strategy when applicable.	decimals, and percents?		
1-100 with a common factor as a multiple of a	Acquisition			
sum of two whole numbers with no common factor.	Students will understand: • Factors	<ul> <li>Students will be skilled at</li> <li>Dividing fractions by fractions</li> </ul>		
<ul> <li>CCSS.MP4 Model with mathematics.</li> </ul>	Multiples	Dividing decimal numbers		
CCSS.MP5 Use appropriate tools strategically.	Place Value	• Adding, subtracting, multiplying and dividing		
• CCSS.MP7 Look for and make use of structure.	Reciprocal	mixed numbers		

	<ul> <li>Dividend</li> <li>Divisor</li> <li>Quotient</li> <li>the value of a digit in relationship to its position in a number</li> </ul>	<ul> <li>Simplifying numerical expressions using the order of operations.</li> <li>Finding common factors, greatest common factors, and multiples, least common multiple</li> </ul>
Used in Content Area Standards		21 <sup>st</sup> Century Skills
		Critical Thinking
		Communication
		Collaboration

Stage 2 - Evidence		
Evaluative Criteria	Assessment Evidence	
	ASSESSMENT: Written Assessments or Projects	
	Other Evidence: independent practice, classroom observations and discussions	

### **Unit 3: Numbers & Operations - Integers**

Stage 1 Desired Results			
ESTABLISHED GOALS:	Transfer		
Students will continue their study of mathematics in the	Students will be able to independently use their lea	rning to	
area of numbers and operations. In this unit, students	<ul> <li>explain the necessity for both positive and negative</li> </ul>	tive numbers.	
will understand rational numbers with an emphasis on	<ul> <li>understand the importance of the sign and direct</li> </ul>	ction of a number in real world applications.	
integers.	<ul> <li>discuss the real world significance of an ordered</li> </ul>	pair as a location on a coordinate plane.	
	Меа	ining	
Content Standards:	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS	
<ul> <li>CCSS.6.NS.5. Understand that positive and negative numbers are used together to describe quantities having opposite directions or values; use positive and negative numbers to represent quantities in real-world contexts, explaining the meaning of 0 in each situation.</li> <li>CCSS.6.NS.6. Understand a rational number as a point on the number line. Extend number line diagrams and coordinate axes familiar from previous grades to represent points on the line and</li> </ul>	<ul> <li>Positive and negative numbers are used together to describe quantities having opposite directions or values</li> <li>All rational numbers can be represented as a point on the number line.</li> <li>Students will understand that absolute value is the distance from zero on a number line.</li> <li>The coordinate plane can be used to describe location in two dimensions, defined by an ordered pair.</li> </ul>	<ul> <li>What is the value in distinguishing between positive and negative numbers?</li> <li>How is the coordinate plane configured?</li> </ul>	
in the plane with negative number coordinates.	Acqui	isition	
<ul> <li>CCSS.6.NS.7. Understand ordering and absolute value of rational numbers.</li> <li>CCSS.6.NS.8. Solve real-world and mathematical problems by graphing points in all four quadrants of the coordinate plane. Include use of coordinates and absolute value to find distances between points with the same first coordinate plane. Include use of coordinates and absolute value to</li> </ul>	<ul> <li>Integers</li> <li>Rational Number</li> <li>Absolute Value</li> </ul>	<ul> <li>Students will be skilled at</li> <li>Creating a number line with integers</li> <li>Determining the absolute value, direction, and opposite of a given integer</li> <li>Writing a number sentence which reflects the actions and changes in real world situations</li> <li>Graphing with positive and negative coordinates on a coordinate grid</li> </ul>	

<ul> <li>find distance between points with the same first coordinate or the same second coordinate.</li> <li>CCSS.MP4 Model with mathematics.</li> <li>CCSS.MP5 Use appropriate tools strategically.</li> <li>CCSS.MP7 Look for and make use of structure.</li> </ul>	<ul> <li>Y Axis</li> <li>Reflection</li> <li>Horizontal</li> <li>Vertical</li> <li>absolute value as the distance away from zero on a number line</li> </ul>	
Used in Content Area Standards		21 <sup>st</sup> Century Skills
		Critical Thinking
		Communication
		Collaboration

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
OTHER EVIDENCE: independent practice, classroom observations and discussions		

## **Unit 4: Algebraic Thinking - Expressions**

Stage 1 Desired Results			
ESTABLISHED GOALS:	Transfer		
Students will continue their study of mathematics in the	he Students will be able to independently use their learning to		
area of Algebraic Thinking. In this unit, students will	• write algebraic expressions to solve real world p	problems	
create, simplify, and evaluate expressions.	<ul> <li>use their knowledge of algebraic expressions as</li> </ul>	they solve algebraic equations	
<ul> <li>Content Standards:</li> <li>CCSS.6.EE.1 Write and evaluate numerical expressions involving whole-number exponents.</li> <li>CCSS.6.EE.2. Write, read, and evaluate expressions in which letters stand for numbers.</li> <li>CCSS.6.EE.3. Apply the properties of operations to generate equivalent expressions.</li> <li>CCSS.6.EE.4. Identify when two expressions are equivalent (i.e., when the two expressions name the same number regardless of which value is</li> </ul>	<ul> <li>ENDURING UNDERSTANDINGS</li> <li>Expressions are powerful tools for exploring, reasoning about, and representing situations.</li> </ul>	<ul> <li>ESSENTIAL QUESTIONS</li> <li>What is meant by an "algebraic expression"?</li> <li>How can algebraic expressions be used to represent real-life situations?</li> <li>How is a variable used in the real world?</li> <li>Why do we need an order of operations?</li> <li>Why is algebraic reasoning important?</li> </ul>	
<ul> <li>substituted into them).</li> <li>CCSS.6.EE.6. Use variables to represent numbers and write expressions when solving a real-world or mathematical problem; understand that a variable</li> </ul>		isition	
	Students will understand	Students will be skilled at	
<ul> <li>on the purpose at hand, any number in a specified set.</li> <li>CCSS.MP1 Make sense of problems and persevere</li> </ul>	<ul><li>Algebraic expressions</li><li>Exponents</li></ul>	<ul> <li>simplifying algebraic expressions with whole numbers.</li> </ul>	
<ul> <li>CCSS.MP1 Make sense of problems and persevere in solving them.</li> <li>CCSS.MP3 Construct viable arguments and critique</li> </ul>	<ul> <li>Constant</li> <li>Coefficient</li> <li>Term</li> </ul>	<ul> <li>creating algebraic expressions from verbal, written and interpretational expressions</li> <li>applying and extending previous</li> </ul>	
<ul><li>the reasoning of others.</li><li>CCSS.MP7 Look for and make use of structure.</li></ul>	Like Terms	understandings of arithmetic to algebraic	

	Variable	expressions, including whole number
	Distributive Property	exponents
Used in Content Area Standards		21 <sup>st</sup> Century Skills
		Collaboration
		Critical Thinking
		Communication

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
OTHER EVIDENCE: independent practice, classroom observations and discussions		

# Windham School District Curriculum **Mathematics - Grade 6 Unit 5: Algebraic Thinking - Equations**

	Stage 1 Desired Results		
ESTABLISHED GOALS:	Transfer		
Students will continue their study of mathematics in the	Students will be able to independently use their lea	rning to	
area of Algebraic Thinking. In this unit, students will	<ul> <li>use their knowledge of equation writing and sol</li> </ul>	ving as a technique for solving problems.	
create and solve one-step questions. They will also use	Меа	ning	
this knowledge in real-life applications.	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS	
<ul> <li>Content Standards:</li> <li>CCSS.6.EE.3. Apply the properties of operations to generate equivalent expressions.</li> <li>CCSS.6.EE.5. Understand solving an equation or inequality as a process of answering a question: which values from a specified set, if any, make the equation or inequality true? Use substitution to</li> </ul>	<ul> <li>Solving an equation is a process of answering a question by finding the value of the variable that makes the equation true.</li> <li>An equation is two equivalent expressions.</li> <li>Variables are used to represent two quantities in a real world problem that change in relationship to one another.</li> </ul>	<ul> <li>Why do we use inverse operations to solve algebraic equations?</li> <li>What is a variable in the real world?</li> <li>How is algebra used in the world we live in every day?</li> <li>What does it mean to be unequal?</li> </ul>	
determine whether a given number in a specified	Acquisition		
<ul> <li>set makes an equation or inequality true.</li> <li>CCSS.6.EE.7. Solve real-world and mathematical problems by writing and solving equations of the form x + P = q and px = q for cases in which p, q and x are all nonnegative rational numbers.</li> <li>CCSS.6.EE.8. Write an inequality of the form x &gt; c or x &lt; c have infinitely many solutions; represent solutions of such inequalities on number line diagrams.</li> <li>CCSS.6.EE.9. Use variable to represent two quantities in a real-world problem that change in relationship to one another; write an equation to</li> </ul>		<ul> <li>Students will be skilled at</li> <li>Writing an equation to express one quantity, thought of as the dependent variable, in terms of the other quantity, thought of as the independent variable.</li> <li>Writing an equation from data tables and graphs</li> <li>Defining a variable and create an equation and / or an inequality from a word problem</li> <li>Solving one step equations and inequalities</li> </ul>	

<ul> <li>express one quantity, thought of as the dependent variable, in terms of the other quantity, thought of as the independent variable. Analyze the relationship between the dependent and independent variables using graphs and tables, and relate these to the equation.</li> <li>CCSS.MP1 Make sense of problems and persevere in solving them.</li> <li>CCSS.MP3 Construct viable arguments and critique the reasoning of others.</li> <li>CCSS.MP7 Look for and make use of structure.</li> </ul>	
Used in Content Area Standards	21 <sup>st</sup> Century Skills
	Collaboration
	Critical Thinking
	Communication

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
OTHER EVIDENCE: independent practice, classroom observations and discussions		

### Unit 6: Geometry & Data - Area & Surface Area

Stage 1 Desired Results		
ESTABLISHED GOALS:	Transfer	
Students will continue their study of mathematics	Students will be able to independently use their learning to	
in the area of Geometry. In this unit, students will	<ul> <li>find the surface area of any solid.</li> </ul>	
continue their understanding of area, surface	<ul> <li>apply area formulas when solving real life scenarios.</li> </ul>	
area.	Meaning	
<ul> <li>Content Standards:</li> <li>CCSS.6.G.1. Find the area of right triangles, other triangles, special quadrilaterals, and polygons by composing into rectangles or decomposing into triangles and other shapes; apply these techniques in the context of solving real-world and mathematical problems.</li> <li>CCSS.6.G.3. Draw polygons in the coordinate plane given coordinates for the vertices; use coordinates to find the length of a side joining points with the same first coordinate or the same second coordinate. Apply these</li> </ul>	<ul> <li>ENDURING UNDERSTANDINGS</li> <li>The area of all 2-dimensional figures can be calculated by breaking irregular shapes into rectangles or triangles.</li> <li>A three-dimensional figure can be represented by two-dimensional nets, which can help determine the surface area of three-dimensional figures.</li> </ul>	<ul> <li>ESSENTIAL QUESTIONS</li> <li>How is geometry part of the world?</li> <li>How can proportional reasoning help you find the length of a corresponding side of a similar figure?</li> <li>Why are there different formulas to find the area of different polygons?</li> <li>How can the use of a coordinate plane aid in finding the area, lengths, and widths of a polygon?</li> <li>How can a net make it easier to find the surface area of a 3-dimensional object?</li> <li>How can nets be used to find surface area on irregular polygons?</li> </ul>
techniques in the context of solving	Acquisition	
<ul> <li>real-world and mathematical problems.</li> <li>CCSS.6.G.4. Represent three-dimensional figures using nets made up of rectangles and triangles, and use the nets to find the surface area of these figures. Apply these techniques in the context of solving real-world and</li> </ul>	<ul><li>Length</li><li>Width</li></ul>	<ul> <li>Students will be skilled at</li> <li>calculating the area of irregular shapes (composite figures).</li> <li>drawing a net for a given solid.</li> <li>identifying faces, edges and vertices.</li> </ul>

<ul> <li>mathematical problems.</li> <li>CCSS.MP1 Make sense of problems and persevere in solving them.</li> <li>CCSS.MP6 Attend to precision.</li> <li>CCSS.MP8 Look for and express regularity in repeated reasoning.</li> </ul>	<ul> <li>Area as space inside a figure</li> <li>Area of a parallelogram A = bh</li> <li>Area of a triangle A = ½ bh</li> <li>Area of a trapezoid A = ½ (b1 + b2)h</li> <li>Units squared</li> <li>Net</li> <li>Surface Area</li> <li>Area</li> <li>Composite Figures</li> <li>Kite</li> <li>Compose</li> <li>decompose</li> <li>irregular shapes</li> <li>Two-dimensional figures</li> <li>three-dimensional figures</li> <li>faces, edges, vertices.</li> <li>Solid</li> <li>prism</li> <li>lateral surface area</li> <li>area is the surface inside a flat, closed figure.</li> <li>irregular shapes are the combination of multiple figures.</li> </ul>	<ul> <li>calculating surface area of rectangular prisms.</li> <li>Calculating area and surface area using models</li> <li>Fluently, calculating area and surface area using formulas</li> <li>Calculating surface area of rectangular prisms</li> </ul>
	• nets are three-dimensional figures drawn on a surface.	
	• surface area is the sum of the areas of all faces.	
Used in Content Area Standards		21 <sup>st</sup> Century Skills
		<ul><li>Collaboration</li><li>Critical Thinking</li></ul>
		Communication

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
OTHER EVIDENCE: independent practice, classroom observations and discussions		

## Unit 7: Geometry & Data - Volume

Stage 1 Desired Results			
ESTABLISHED GOALS:		Transfer	
Students will continue their study of mathematics in the area of	Students will be able to independently	y use their learning to	
Geometry. In this unit, students will continue their understanding of	<ul> <li>apply volume formulas in the context of solving real-world problems</li> </ul>		
volume.	• explain the difference between su	irface area and volume of objects.	
		Meaning	
Content Standards:	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS	
• CCSS.6.G.2. Find the volume of a right rectangular prism with	• Volume is the number of cubes	• What does volume mean?	
fractional edge lengths by packing it with unit cubes of the	that can fit inside of a solid.	• How can the volume of a triangular prism be	
appropriate unit fraction edge lengths, and show that the volume is		found by placing unit cubes inside it?	
the same as would be found by multiplying the edge lengths of the	the area of the base multiplied by	,	
prism. Apply the formulas V = I w h and V = b h to find volumes of	the height.		
right rectangular prisms with fractional edge lengths in the context	Acquisition		
of solving real-world and mathematical problems.	Students will understand	Students will be skilled at	
• CCSS.MP1 Make sense of problems and persevere in solving them.	Polygon	• Finding volume by packing it with unit cubes	
CCSS.MP6 Attend to precision.	Polyhedron	of the appropriate unit fraction edge lengths	
• CCSS.MP8 Look for and express regularity in repeated reasoning	• Edge	(modeling)	
	Vertex	<ul> <li>Calculating volume using models</li> </ul>	
	• Length	• Fluently calculating volume using formulas	
	Width	• Solving real word problems involving volume	
	• Depth		
	Cubic Units		
	<ul> <li>Formula: V=LWH or V=Bh</li> </ul>		
	Irregular Figures		
	• Prism		
	<ul> <li>volume as the space inside a</li> </ul>		
	solid.		

Used in Content Area Standards	21 <sup>st</sup> Century Skills
	Collaboration
	Critical Thinking
	Communication

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
OTHER EVIDENCE: independent practice, classroom observations and discussions		

# Windham School District Curriculum Mathematics - Grade 6 Unit 8: Geometry & Data - Statistics & Probability

	Stage 1 Desired Results		
ESTABLISHED GOALS:	Transfer		
Students will continue their study of mathematics in the	Students will be able to independently use their lea	arning to	
area of Data. In this unit, students will continue their	<ul> <li>analyze graphs found in multiple sources</li> </ul>		
understanding of data analysis and statistical graphs.	<ul> <li>describe data using graphs and measures of cer</li> </ul>	ntral tendency.	
	Me	aning	
<ul> <li>Content Standards:</li> <li>CCSS.6.SP.1. Recognize a statistical question as one that anticipates variability in the data related to the question and accounts for it in the answers. CCSS.6.SP.2. Understand that a set of data collected to answer a statistical question has a distribution, which can be described by its center, spread, and overall shape.</li> <li>CCSS.6.SP.3. Recognize that a measure of center for a numerical data set summarizes all of its values with a single number, while a measure of variation describes how its values vary with a</li> </ul>	<ul> <li>ENDURING UNDERSTANDINGS</li> <li>A statistical question anticipates variability in the data related to the question and accounts for it in the answers.</li> <li>A set of data collected to answer a statistical question has a distribution, which can be described by its center, spread, and overall shape.</li> <li>A measure of center for a numerical data set summarizes all of its values with a single number, while a measure of variation describes how its values vary with a single number.</li> </ul>	<ul> <li>ESSENTIAL QUESTIONS</li> <li>How are statistics used to collect, analyze, and draw conclusions in today's society?</li> <li>Why are statistics important in the world?</li> <li>What are the ways that data can be represented visually?</li> <li>Why is it better to use different graphs and diagrams to understand data?</li> <li>What are the different ways in which we can summarize data sets?</li> </ul>	
single number.		isition	
<ul> <li>CCSS.6.SP.4. Display numerical data in plots on a number line, including dot plots, histograms, and box plots.</li> <li>CCSS.6.SP.5. Summarize numerical data sets in relation to their context, such as by:</li> <li>CCSS.6.SP.5. a. Reporting the number observations.</li> </ul>	<ul> <li>Students will understand</li> <li>Variability</li> <li>Data</li> <li>statistical questioning</li> <li>statistical process</li> <li>Sample</li> <li>bar graph</li> </ul>	<ul> <li>Students will be skilled at</li> <li>Determining measures of central tendency and variation</li> <li>Choosing which measure of central tendency is appropriate for a given set of points</li> <li>Analyzing data from a given dot plot, histogram, and box plots</li> </ul>	

<ul> <li>CCSS.6.SP.5. b. Describing the nature of the attribute under investigation, including how it was measured and its units of measurement.</li> <li>CCSS.6.SP.5. c. Giving quantitative measures of center (median and/or mean) and variability (interquartile range and/or mean absolute deviation), as well as describing any overall pattern and any striking deviations from the overall pattern with reference to the context in which the data were gathered.</li> <li>CCSS.6.SP.5. d. Relating the choice of measures of center and variability to the shape of the data distribution and the context in which the data were gathered.</li> <li>CCSS.MP2 Reason abstractly and quantitatively.</li> <li>CCSS.MP5 Use appropriate tools strategically.</li> <li>CCSS.MP6 Attend to precision</li> </ul>	-	•	Reporting observations about data using mathematical vocabulary: giving quantitative measures of center (median and/or mean) and variability (interquartile range and/or mean absolute deviation).
Used in Content Area Standards			21 <sup>st</sup> Century Skills
		•	Communication Critical Thinking Perseverance

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
OTHER EVIDENCE: independent practice, classroom observations and discussions		

### Title of Curriculum: 6th Grade Accelerated Math

Unit Name	What (content, vocab)	Why (enduring understandings)	How (skills)
Unit 1: Number and Operations: Ratios and Proportional Relationships	<ul> <li>Ratios</li> <li>Unit Rates</li> <li>Proportions</li> <li>Fraction, decimal, percent conversions</li> <li>Terminating and repeating decimals</li> <li>ratios as a fraction or percentage</li> <li>equivalent ratios</li> <li>a rate is a ratio involving units</li> <li>100% is all of the original amount</li> </ul>	<ul> <li>A ratio or rate describes the relationship between two quantities.</li> <li>Ratio reasoning can be applied to many different types of mathematical and real-life problems</li> <li>A rate is a type of ratio that represents a measure or quantity. Therefore the process for solving ratio problems can be applied to rates.</li> </ul>	<ul> <li>Simplify ratios</li> <li>Compare ratios in different formats</li> <li>Find equivalent ratios</li> <li>Calculate unit rate</li> <li>Find a missing number in a proportion</li> <li>Convert between fractions, decimals and percents</li> <li>Find a missing percent</li> <li>Find percent of a quantity.</li> <li>Solve percent real world problems</li> </ul>
Unit 2: Number and Operations: Fractions and Decimals	<ul> <li>Factors</li> <li>Multiples</li> <li>Place Value</li> <li>Reciprocal</li> <li>Dividend</li> <li>Divisor</li> <li>Quotient</li> <li>the value of a digit in relationship to its position in a number</li> <li>Positive exponents</li> </ul>	<ul> <li>Multiplication and division are inverse operations.</li> <li>Operations on decimals and whole numbers are based upon place value relationships.</li> <li>Number lines are visual models used to represent the density principle: between any two whole numbers are many rational numbers, including decimals and fractions.</li> <li>The magnitude of numbers affects the outcome of operations on them.</li> <li>Computational fluency includes applying the most effective and efficient strategy when applicable.</li> </ul>	<ul> <li>Divide fractions by fractions</li> <li>Find common factors, greatest common factors, and multiples, least common multiple</li> <li>Add,subtract, multiply and divide mixed numbers</li> <li>Divide decimals</li> <li>Simplify numerical expressions using the order of operations</li> </ul>

Unit 3: Numbers and Operations: Integers	<ul> <li>Integers</li> <li>Rational Numbers</li> <li>Absolute Value</li> <li>Coordinate Grid</li> <li>Opposite</li> <li>Number Line</li> <li>Coordinate Plane</li> <li>X Axis</li> <li>Y Axis</li> <li>Reflection</li> <li>Horizontal</li> <li>Vertical</li> </ul>	<ul> <li>are used together to describe quantities having opposite directions(number line) or values</li> <li>All rational numbers can be represented as a point on a number line</li> <li>Understand that absolute value is the distance from zero on a</li> </ul>	<ul> <li>Create a number line with integers</li> <li>Understand the relationship between a positive or negative number and its opposite</li> <li>Determine the absolute value, direction of number line movement, and opposite of a given integer</li> <li>Write a number sentence which reflects the actions and changes in real world situations</li> <li>Graph with positive and negative coordinates on a coordinate grid</li> <li>Add, subtract, multiply and divide integers</li> </ul>
Unit 4: Algebraic Thinking: Expressions	<ul> <li>Algebraic expressions</li> <li>Exponents</li> <li>Constant</li> <li>Coefficient</li> <li>Term</li> <li>Like Terms</li> <li>Variable</li> <li>Distributive Property</li> <li>Integer</li> <li>Rational number</li> </ul>	<ul> <li>Expressions are powerful tools for exploring, reasoning about, and representing situations.</li> <li>Variables have many different meanings, depending on context and purpose.</li> <li>Variables permit writing expressions whose values are unknown or vary under different circumstances.</li> <li>Two or more expressions may be equivalent, even when their symbolic forms differ.</li> <li>Linear expressions may be</li> </ul>	<ul> <li>simplify algebraic expressions with whole numbers.</li> <li>create algebraic expressions from verbal, written and interpretational expressions</li> <li>apply and extend previous understandings of arithmetic to algebraic expressions, including whole number exponents</li> </ul>

Unit 5: Algebraic Thinking: Equations	<ul> <li>multi-step algebraic equations and inequalities</li> <li>dependent and independent variables.</li> <li>Integers</li> <li>Like terms</li> <li>Rational numbers</li> <li>like terms</li> <li>equivalent expressions</li> </ul>	<ul> <li>added to or subtracted from one another.</li> <li>Solving an equation is a process of answering a question by finding the value of the variable that makes the equation true.</li> <li>An equation is two equivalent expressions.</li> <li>Variables are used to represent two quantities in a real world problem that change in relationship to one another.</li> </ul>	<ul> <li>Write an equation to express one quantity, thought of as the dependent variable, in terms of the other quantity, thought of as the independent variable.</li> <li>Write an equation from data tables and graphs</li> <li>Define a variable and create an equation and / or an inequality from a word problem</li> <li>Solve multi step equations and inequalities</li> </ul>
Unit 6: Geometry and Data: Area and Surface Area	<ul> <li>Length</li> <li>Width</li> <li>Parallelogram</li> <li>Altitude</li> <li>Trapezoid</li> <li>Area as space inside a figure</li> <li>Area of a parallelogram A = bh</li> <li>Area of a triangle A = ½ bh</li> <li>Area of a trapezoid A = ½ (b1 + b2)h</li> <li>Units squared</li> <li>Net</li> <li>Surface Area</li> <li>Composite (irregular) Figures</li> <li>Kite</li> <li>irregular shapes</li> <li>Two-dimensional figures</li> <li>faces, edges, vertices.</li> <li>Solid</li> </ul>	<ul> <li>The area of all 2-dimensional figures can be calculated by breaking irregular shapes into rectangles or triangles.</li> <li>A three-dimensional figure can be represented by two-dimensional nets, which can help determine the surface area of three-dimensional figures.</li> </ul>	<ul> <li>calculating the area of irregular shapes (composite figures).</li> <li>drawing a net for a given solid.</li> <li>identifying faces, edges and vertices.</li> <li>calculating surface area of rectangular prisms.</li> <li>Calculating area and surface area using models</li> <li>Fluently, calculating area and surface area using formulas</li> <li>Calculating surface area of rectangular prisms, triangular prisms, cone and cylinder and pyramids</li> </ul>

Unit 7: Geometry and Data: Triangles	<ul> <li>prism</li> <li>lateral surface area</li> <li>Radius</li> <li>Circumference</li> <li>Diameter</li> <li>Pi</li> <li>180 degrees in every triangle.</li> <li>classifications of triangles for both sides and angles: acute, obtuse, right, scalene, isosceles, equilateral</li> <li>supplementary, complementary, vertical, and adjacent angles</li> <li>Angle pair relationships: adjacent, vertical, complementary, supplementary, linear pair</li> </ul>	<ul> <li>differences between geometrical figures.</li> <li>Analyzing geometric relationships develops reasoning and justification skills.</li> <li>Angle relationships can be used to determine missing angle measures in diagrams.</li> </ul>	<ul> <li>and/or angles</li> <li>Determine the missing angles in triangles</li> <li>Classify triangles by their sides and angles</li> <li>Identify values of angles in complementary and supplementary relationships</li> <li>Use vertical, complementary, and supplementary angle relationships to find missing angles</li> <li>Solve for unknown angles using equations</li> </ul>
Unit 8: Geometry and Data: Volume	<ul> <li>Polygon</li> <li>Polyhedron</li> <li>Edge</li> <li>Vertex</li> <li>Length</li> <li>Width</li> <li>Depth</li> <li>Cubic Units</li> <li>Formula: V=LWH or V=Bh</li> <li>Irregular Figures</li> <li>Prism</li> <li>volume as the space inside a solid.</li> </ul>	<ul> <li>Area, surface area and volume have applications in real world situations.</li> <li>Dimension is a measure of the width, height, or length of a figure.</li> <li>Different 3-dimensional figures can have the same volume even if the dimensions are not all the same.</li> </ul>	<ul> <li>Calculate volume using models</li> <li>Fluently calculate volume using formulas</li> <li>Apply the formulas for volume of three- dimensional figures</li> <li>Differentiate between volume and the surface area to solve problem for three-dimensional figures</li> <li>Calculate and explain how to find the area, volume, and surface area for two- and three- dimensional objects from real-world situations</li> </ul>
Unit 9: Geometry and Data: Statistics and Probability	<ul><li>Data</li><li>statistical questioning</li></ul>	• A statistical question anticipates variability in the data related to	<ul> <li>Determine measures of central tendency</li> </ul>

# Windham School District Curriculum Accelerated Math - Grade 6 Unit 1: Number & Operations Ratios & Proportional Relationships

Stage 1 Desired Results			
ESTABLISHED GOALS:	Transfer		
Students will continue their study of mathematics in	Students will be able to independently use their learning to		
the area of numbers and operations. In this unit,	<ul> <li>apply their knowledge of ratios and proportion</li> </ul>	s to real-life applications.	
students will explore the concepts and ratios and	Mea	ining	
proportions and how they relate to real-world	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS	
applications.	• A ratio or rate describes the relationship	• What does 100% represent?	
	between two quantities.	How can you define a part to whole	
Content Standards:	• Ratio reasoning can be applied to many	relationship?	
• CCSS.6.RP.1. Understand the concept of a ratio	different types of mathematical and real-life	How can proportions be used for problem	
and use ratio language to describe a ratio	problems	solving?	
relationship between two quantities.	• A rate is a type of ratio that represents a	• Can you give an example of a rate in a real	
• CCSS.6.RP.2 Understand the concept of a unit rate	measure or quantity. Therefore the process for	world setting?	
a/b associated with a ratio a:b with b $\neq$ 0, and use	solving ratio problems can be applied to rates.	• What is the difference between a rate and a	
rate language in the context of a ratio		ratio?	
relationship.	Acqui	isition	
• CCSS.6.RP.3. Use ratio and rate reasoning to solve	Students will understand	Students will be skilled at	
real-world and mathematical problems, e.g., by	ratios	Simplifying ratios	
reasoning about tables of equivalent ratios, tape	unit rates	Comparing ratios in different formats	
diagrams, double number line diagrams, or	• proportions	<ul> <li>Finding equivalent ratios</li> </ul>	
equations.	• Fraction, decimals percent connections	Calculating unit rate	
CCSS.MP1 Make sense of problems and persevere	<ul> <li>Terminating and repeating decimals</li> </ul>	• Finding the missing number in a proportion.	
in solving them.	<ul> <li>Ratio as a fraction or percentage</li> </ul>	• Conversions between fractions, decimals and	
CCSS.MP3 Construct viable arguments and	Equivalent ratios	percents	
critique the reasoning of others.	A rate is a ratio involving units	Finding a missing percent	

<ul> <li>CCSS.MP6 Attend to precision.</li> <li>CCSS.MP8 Look for and express regularity in repeated reasoning</li> </ul>	<ul> <li>100% is all of the original amount</li> <li>Numbers can be expressed in different formats based on a given situation</li> </ul>	<ul> <li>Finding the percent of a quantity</li> <li>Solving percent word problems</li> </ul>
Used in Content Area Standards		21 <sup>st</sup> Century Skills
		Critical Thinking
		Collaboration
		Communication

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
OTHER EVIDENCE: independent practice, classroom observations and discussions		

# Windham School District Curriculum Accelerated Math - Grade 6

### **Unit 2: Number & Operations - Fractions & Decimals**

### **Stage 1 Desired Results** ESTABLISHED GOALS: Transfer Students will continue their study of mathematics in the Students will be able to independently use their learning to... area of numbers and operations. In this unit, students fluently perform all operations on positive rational numbers with speed and accuracy without the will master fraction and decimal operations and apply use of math tools (calculator) them to real-life applications. • apply this knowledge to real-life applications as well as future algebraic topics. Meaning Content Standards: ENDURING UNDERSTANDINGS ESSENTIAL QUESTIONS • CCSS.6.NS.1. Interpret and compute quotients of Is the product of two numbers always greater Multiplication and division are inverse • fractions, and solve word problems involving operations. than either factor? division of fractions by fractions. Operations on decimals and whole numbers are Why is the quotient of two fractions larger than CCSS.6.NS.2. Fluently divide multi-digit numbers • based on place value relationships. the dividend or divisor? using the standard algorithm. Number lines are visual models used to What is the relationship between a mixed • • CCSS.6.NS.3. Fluently add, subtract, multiply, and number and an improper fraction? represent the density principle: between any divide multi-digit decimals using the standard two whole numbers are many rational • What strategies do you use to find equivalent algorithm for each operation. numbers, including decimals and fractions. fractions? CCSS.6.NS.4. Find the greatest common factor of • The magnitude of numbers affects the outcome • What is the connection between fractions. two whole numbers less than or equal to 100 and decimals, and percents? of operations on them. the least common multiple of two whole numbers • Computational fluency includes applying the less than or equal to 12. Use the distributive most effective and efficient strategy when property to express a sum of two whole numbers applicable. 1-100 with a common factor as a multiple of a sum Acquisition of two whole numbers with no common factor. Students will understand ... Students will be skilled at... CCSS.MP4 Model with mathematics. • Dividing fractions by fractions Factors • • CCSS.MP5 Use appropriate tools strategically. Multiples **Dividing decimal numbers** • CCSS.MP7 Look for and make use of structure. Adding, subtracting, multiplying and dividing Place value • Reciprocal mixed numbers •

	<ul> <li>Dividend</li> <li>Divisor</li> <li>quotient</li> <li>the value of a digit in relationship to its position in a number</li> <li>positive exponents</li> </ul>	<ul> <li>Simplifying numerical expressions using the order of operations.</li> <li>Finding common factors, greatest common factors, and multiples, least common multiple</li> </ul>
Used in Content Area Standards		21 <sup>st</sup> Century Skills
		Critical Thinking
		Communication
		Collaboration

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
Other Evidence: independent practice, classroom observations and discussions		

# Windham School District Curriculum **Accelerated Math - Grade 6 Unit 3: Number & Operations - Integers**

	Stage 1 Desired Results		
ESTABLISHED GOALS:	Transfer		
Students will continue their study of mathematics in the	Students will be able to independently use their learning to		
area of numbers and operations. In this unit, students	<ul> <li>explain the necessity for both positive and negative numbers.</li> </ul>		
will understand rational numbers with an emphasis on	<ul> <li>understand the significance of a number having</li> </ul>	both a sign and direction.	
integers.	• Discuss the real world significance of an ordered pair as a location on a coordinate plane (for		
	example: on a map)		
Content Standards:	Fluently perform operations on integers		
<ul> <li>CCSS.6.NS.5. Understand that positive and</li> </ul>	Mea	aning	
negative numbers are used together to describe	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS	
quantities having opposite directions or values;	<ul> <li>Positive and negative numbers are used</li> </ul>	How can a number line be used to determine	
use positive and negative numbers to represent	together to describe quantities having opposite	size and direction of a number?	
quantities in real-world contexts, explaining the	directions with the same values	What is the value in distinguishing between	
meaning of 0 in each situation.	All rational numbers can be represented as a	positive and negative numbers?	
• CCSS.6.NS.6. Understand a rational number as a	point on the number line.	<ul> <li>How is the coordinate plane configured?</li> </ul>	
point on the number line. Extend number line	• Absolute value is the distance from zero on a	What are some situations in everyday life	
diagrams and coordinate axes familiar from	number line.	where you use negative as well as positive	
previous grades to represent points on the line and		numbers?	
in the plane with negative number coordinates.	location in two dimensions, defined by an		
CCSS.6.NS.7. Understand ordering and absolute	ordered pair.		
value of rational numbers.	Acquisition		
CCSS.6.NS.8. Solve real-world and mathematical		Students will be skilled at	
problems by graphing points in all four quadrants	Integers	<ul> <li>Creating a number line with integers</li> </ul>	
of the coordinate plane. Include use of coordinates		<ul> <li>Understanding the relationship between a</li> </ul>	
and absolute value to find distances between	Absolute value	positive or negative number and its opposite	
points with the same first coordinate plane.	Opposite	• Determining the absolute value, direction, and	
Include use of coordinates and absolute value to	Number line	opposite of a given integer	

<ul> <li>find distance between points with the same first coordinate or the same second co</li> <li>CCSS.MP4 Model with mathematics.</li> <li>CCSS.MP5 Use appropriate tools strategically.</li> <li>CCSS.MP7 Look for and make use of structure.ordinate.</li> </ul>	<ul> <li>Coordinate plane</li> <li>x-axis</li> <li>y-axis</li> <li>Reflection</li> <li>Horizontal</li> <li>vertical</li> <li>absolute value as the distance away from zero on a number line</li> </ul>	•	Writing a number sentence which reflects the actions and changes in real world situations Graphing with positive and negative coordinates on a coordinate grid Add, subtract, multiply and divide integers
Used in Content Area Standards			21 <sup>st</sup> Century Skills
		٠	Critical Thinking
		•	Communication
		•	Collaboration

Stage 2 - Evidence			
Evaluative Criteria Assessment Evidence			
	ASSESSMENT: Written Assessments or Projects		
Other Evidence: independent practice, classroom observations and discussions			

# Windham School District Curriculum Accelerated Math - Grade 6 Unit 4: Algebraic Thinking - Expressions

Stage 1 Desired Results		
ESTABLISHED GOALS:	Transfer	
	Students will be able to independently use their lea	rning to
Students will continue their study of mathematics in the	• write algebraic expressions to solve real world p	problems
area of Algebraic Thinking. In this unit, students will	<ul> <li>use their knowledge of algebraic expressions as</li> </ul>	they solve algebraic equations
create, simplify, and evaluate expressions.	Мес	aning
<ul> <li>Content Standards:</li> <li>CCSS.6.EE.1 Write and evaluate numerical expressions involving whole-number exponents.</li> <li>CCSS.6.EE.2. Write, read, and evaluate expressions in which letters stand for numbers.</li> <li>CCSS.6.EE.3. Apply the properties of operations to generate equivalent expressions.</li> <li>CCSS.6.EE.4. Identify when two expressions are equivalent (i.e., when the two expressions name the same number regardless of which value is substituted into them).</li> </ul>	<ul> <li>ENDURING UNDERSTANDINGS</li> <li>Expressions are powerful tools for exploring, reasoning about, and representing situations.</li> <li>Variables have many different meanings, depending on context and purpose.</li> <li>Variables permit writing expressions whose values are unknown or vary under different circumstances.</li> <li>Two or more expressions may be equivalent, even when their symbolic forms differ.</li> <li>Linear expressions may be added to or subtracted from one another.</li> </ul>	<ul> <li>ESSENTIAL QUESTIONS</li> <li>What is meant by an "algebraic expression"?</li> <li>How can algebraic expressions be used to represent real-life situations?</li> <li>How is a variable used in the real world?</li> <li>Why do we need an order of operations?</li> <li>Why is algebraic reasoning important?</li> </ul>
• CCSS.6.EE.6. Use variables to represent numbers	Acqu	isition
<ul> <li>and write expressions when solving a real-world or mathematical problem; understand that a variable can represent an unknown number, or, depending on the purpose at hand, any number in a specified set.</li> <li>CCSS.MATH.CONTENT.7.EE.A.1 Apply properties of operations as strategies to add, subtract, factor,</li> </ul>	<ul> <li>Students will understand</li> <li>Algebraic expressions</li> <li>Exponents</li> <li>Constant</li> <li>Coefficient</li> <li>Term</li> <li>Like Terms</li> <li>Variable</li> </ul>	<ul> <li>Students will be skilled at</li> <li>simplifying algebraic expressions with whole numbers.</li> <li>creating algebraic expressions from verbal, written and interpretational expressions</li> <li>applying and extending previous understandings of arithmetic to algebraic expressions, including whole number</li> </ul>

<ul> <li>and expand linear expressions with rational coefficients.</li> <li>CCSS.MATH.CONTENT.7.EE.A.2 Understand that rewriting an expression in different forms in a problem context can shed light on the problem and how the quantities in it are related. For example, a + 0.05a = 1.05a means that "increase by 5%" is the same as "multiply by 1.05."</li> <li>CCSS.MP1 Make sense of problems and persevere in solving them.</li> <li>CCSS.MP3 Construct viable arguments and critique the reasoning of others.</li> <li>CCSS.MP7 Look for and make use of structure.</li> </ul>	<ul> <li>Distributive Property</li> <li>Integer</li> <li>Rational number</li> </ul>	exponents
Used in Content Area Standards		21 <sup>st</sup> Century Skills
		Collaboration
		Critical Thinking
		Communication

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
	OTHER EVIDENCE: independent practice, classroom observations and discussions	

# Windham School District Curriculum **Accelerated Math - Grade 6 Unit 5: Algebraic Thinking - Equations**

	Stage 1 Desired Results	
ESTABLISHED GOALS:	Tran	nsfer
itudents will continue their study of mathematics in the Students will be able to independently use their learning to		
area of Algebraic Thinking. In this unit, students will	<ul> <li>write and solve equations as a technique for solve</li> </ul>	ving problems
create and solve multi-step equations. They will also		t and independent variables using graphs and tables,
use this knowledge in real-life applications.	and relate these to the equation.	
	Меа	ining
Content Standards:	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS
• CCSS.6.EE.3. Apply the properties of operations to	• Solving an equation is a process of answering a	<ul> <li>Why do we use inverse operations to solve</li> </ul>
generate equivalent expressions.	question by finding the value of the variable	algebraic equations?
CCSS.6.EE.5. Understand solving an equation or	that makes the equation true.	<ul> <li>What is a variable in the real world?</li> </ul>
inequality as a process of answering a question:	An equation is two equivalent expressions.	<ul> <li>How is algebra used in the world we live in</li> </ul>
which values from a specified set, if any, make the	• Variables are used to represent two quantities	every day?
equation or inequality true? Use substitution to	in a real world problem that change in	<ul> <li>What does it mean to be unequal?</li> </ul>
determine whether a given number in a specified	relationship to one another.	
set makes an equation or inequality true. CCSS.6.EE.7. Solve real-world and mathematical	· · · · · · · · · · · · · · · · · · ·	isition
problems by writing and solving equations of the		Students will be skilled at
form $x + P = q$ and $px = q$ for cases in which p, q	• multi-step algebraic equations and inequalities.	<ul> <li>Solving multi-step equations and inequalities</li> </ul>
and x are all nonnegative rational numbers.	the difference between dependent and	• Writing an equation to express one quantity,
• CCSS.6.EE.8. Write an inequality of the form $x > c$	independent variables.	thought of as the dependent variable, in terms
or x < c have infinitely many solutions; represent	Integers	of the other quantity, thought of as the
solutions of such inequalities on number line	Like terms	independent variable.
diagrams.	Rational numbers	<ul> <li>Writing an equation from data tables and</li> </ul>
<ul> <li>CCSS.6.EE.9. Use variables to represent two</li> </ul>	like terms     aquivalant expressions	graphs
quantities in a real-world problem that change in	equivalent expressions	<ul> <li>Defining a variable and creating an equation and / or an inequality from a word problem</li> </ul>
relationship to one another; write an equation to		and / or an inequality from a word problem

<ul> <li>express one quantity, thought of as the dependent variable, in terms of the other quantity, thought of as the independent variable. Analyze the relationship between the dependent and independent variables using graphs and tables, and relate these to the equation.</li> <li>CCSS.MATH.CONTENT.7.EE.B.4: Use variables to represent quantities in a real-world or mathematical problem, and construct simple equations and inequalities to solve problems by reasoning about the quantities.</li> <li>CCSS.MP1 Make sense of problems and persevere in solving them.</li> <li>CCSS.MP7 Look for and make use of structure.</li> </ul>	
Used in Content Area Standards	21 <sup>st</sup> Century Skills
	<ul><li>Collaboration</li><li>Critical Thinking</li><li>Communication</li></ul>

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
OTHER EVIDENCE: independent practice, classroom observations and discussions		

# Windham School District Curriculum Accelerated Math - Grade 6

## Unit 6: Geometry & Data - Area & Surface Area

Stage 1 Desired Results					
ESTABLISHED GOALS:	Transfer				
Students will continue their study of mathematics in the	Students will be able to independently use their lea	rning to			
area of Geometry. In this unit, students will continue to	• find the surface area of any solid				
build their understanding of area and surface area and	apply area formulas when solving real life scenarios				
use it to solve problems.	Meaning				
<ul> <li>Content Standards:</li> <li>CCSS.6.G.1. Find the area of right triangles, other triangles, special quadrilaterals, and polygons by composing into rectangles or decomposing into triangles and other shapes; apply these techniques</li> </ul>	<ul> <li>The area of all 2-dimensional figures can be calculated by breaking irregular shapes into rectangles or triangles.</li> <li>A three-dimensional figure can be represented</li> </ul>	<ul> <li>ESSENTIAL QUESTIONS</li> <li>How is geometry part of the world?</li> <li>Why are there different formulas to find the area of different polygons?</li> <li>How can a net make it easier to find the surface area of a 3-dimensional object?</li> </ul>			
<ul> <li>in the context of solving real-world and mathematical problems.</li> <li>CCSS.6.G.3. Draw polygons in the coordinate plane given coordinates for the vertices; use coordinates to find the length of a side joining points with the same first coordinate or the same second coordinate. Apply these techniques in the context of solving real-world and mathematical problems.</li> <li>CCSS.6.G.4. Represent three-dimensional figures using nets made up of rectangles and triangles, and use the nets to find the surface area of these figures. Apply these techniques in the context of solving real-world and mathematical problems.</li> </ul>	determine the surface area of three-dimensional figures.	<ul> <li>How can nets be used to find surface area on irregular polygons?</li> <li>isition</li> </ul>			
	<ul> <li>Students will understand</li> <li>Dimensions: Length, width, altitude</li> <li>Parallelogram, trapezoid, kite</li> <li>Area as space inside a figure</li> <li>Area of a parallelogram A = bh</li> <li>Area of a triangle A = ½ bh</li> <li>Area of a trapezoid A = ½ (b1 + b2)h</li> <li>Units squared</li> <li>Composite (irregular) Figures</li> <li>Two-dimensional figures</li> <li>three-dimensional figures (solids)</li> <li>faces, edges, vertices.</li> </ul>	<ul> <li>Students will be skilled at</li> <li>calculating the area of irregular shapes (composite figures).</li> <li>Calculate the area and circumference of circles.</li> <li>drawing a net for a given solid.</li> <li>identifying faces, edges and vertices.</li> <li>calculating surface area of rectangular prisms.</li> <li>Calculate area and surface area using models and formulas</li> <li>Calculate surface area of rectangular prisms, triangular prisms, cones, cylinders, and pyramids</li> </ul>			

<ul> <li>CCSS.7.G.4 Know the formulas for the area and circumference of a circle and use them to solve problems; give an informal derivation of the relationship between the circumference and area of a circle.</li> <li>CCSS.7.G.6 Solve real-world and mathematical problems involving area, volume and surface area of two- and three-dimensional objects composed of triangles, quadrilaterals, polygons, cubes, and right prisms.</li> <li>CCSS.MP1 Make sense of problems and persevere in solving them.</li> <li>CCSS.MP6 Attend to precision.</li> <li>CCSS.MP8 Look for and express regularity in repeated reasoning.</li> </ul>	<ul> <li>prism</li> <li>nets are three-dimensional figures drawn on a surface.</li> <li>surface area and lateral surface area</li> <li>Radius and diameter of a circle</li> <li>Circumference</li> <li>Pi</li> </ul>	
Used in Content Area Standards		21 <sup>st</sup> Century Skills
		<ul><li>Collaboration</li><li>Critical Thinking</li><li>Communication</li></ul>

Stage 2 - Evidence			
Evaluative Criteria Assessment Evidence			
ASSESSMENT: Written Assessments or Projects			
Other Evidence: independent practice, classroom observations and discussions			

# Windham School District Curriculum **Accelerated Math - Grade 6 Unit 7: Geometry - Triangles**

#### **Stage 1 Desired Results**

#### ESTABLISHED GOALS: Transfer Students will continue their study of Students will be able to independently use their learning to... mathematics in the area of geometry. In this unit, use their knowledge of triangles to solve real-world problems involving geometric figures. ٠ students will gain a deeper understanding of Meanina angles and triangles and will solve real-world ENDURING UNDERSTANDINGS ESSENTIAL QUESTIONS problems involving geometric figures. Drawings and constructions help to see the How do geometric models describe spatial relationships and differences between geometrical relationships? Content Standards: • How are geometric shapes and objects figures. CCSS.7.G.2. Draw (freehand, with ruler and Analyzing geometric relationships develops reasoning • classified? protractor, and with technology) geometric and justification skills. What are the major classifications and • shapes with given conditions. Focus on • Angle relationships can be used to determine missing relationships of angles, polygons and solids? constructing triangles from three measures angle measures in diagrams. of angles or sides, noticing when the Acquisition conditions determine a unique triangle, Students will understand... Students will be skilled at... more than one triangle, or no triangle. creating triangles given specific sides and/or the requirements for three segments to form a ٠ • CCSS.MATH.CONTENT.7.G.B.5: Use facts • triangle. angles. about supplementary, complementary, • there are 180 degrees in every triangle. finding missing angles in a triangle. vertical, and adjacent angles in a multi-step the classifications of triangles for both sides and classifying a triangle by both its sides and its problem to write and solve simple equations angles: acute, obtuse, right, scalene, isosceles, angles. for an unknown angle in a figure. Identifying values of angles in complementary equilateral CCSS.MP4 Model with mathematics. • Facts about supplementary, complementary, vertical, and supplementary relationships • CCSS.MP5 Use appropriate tools and adjacent angles • Using vertical, complementary, and strategically. Angle pair relationships: adjacent, vertical, supplementary angle relationships to find • CCSS.MP6 Attend to precision. complementary, supplementary, linear pair missing angles conditions needed to construct a unique triangle, Solving for unknown angles using equations • more than one triangle, or no triangle.

Used in Content Area Standards	21 <sup>st</sup> Century Skills	
	<ul> <li>Communication</li> <li>Critical Thinking</li> <li>Collaboration</li> </ul>	

Stage 2 - Evidence			
Evaluative Criteria Assessment Evidence			
ASSESSMENT: Written Assessments or Projects			
Other Evidence: independent practice, classroom observations and discussions			

# Windham School District Curriculum **Accelerated Math - Grade 6** Unit 8: Geometry & Data - Volume

	Stage 1 Desired Results			
ESTABLISHED GOALS:		ansfer		
Students will continue their study of mathematics in the area of				
Geometry. In this unit, students will continue their	• apply volume formulas in the context of so			
understanding of volume.	• explain the difference between surface are			
	M	eaning		
Content Standards:	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS		
<ul> <li>CCSS.6.G.2. Find the volume of a right rectangular prism with fractional edge lengths by packing it with unit cubes of the appropriate unit fraction edge lengths, and show that the volume is the same as would be found by multiplying the edge lengths of the prism. Apply the formulas V = I w h and V = b h to find volumes of right rectangular prisms with fractional edge lengths in the</li> </ul>	<ul> <li>Area, surface area and volume have applications in real world situations.</li> <li>Dimension is a measure of the width, height, or length of a figure.</li> <li>Different 3-dimensional figures can have the same volume even if the dimensions are not all the same.</li> </ul>	<ul> <li>What does volume mean?</li> <li>How are the volumes of rectangular prism and triangular prism related?</li> <li>What is the difference between volume and surface area?</li> </ul>		
context of solving real-world and mathematical problems.	Acquisition			
<ul> <li>CCSS. 7.G.6 Solve real-world and mathematical problems.</li> <li>CCSS. 7.G.6 Solve real-world and mathematical problems involving area, volume and surface area of two- and three-dimensional objects composed of triangles, quadrilaterals, polygons, cubes, and right prisms.</li> <li>CCSS.MP1 Make sense of problems and persevere in solving them.</li> <li>CCSS.MP6 Attend to precision.</li> <li>CCSS.MP8 Look for and express regularity in repeated reasoning.</li> </ul>	Students will understand Polygon Polyhedron Edge Vertex Length Width Depth Cubic Units Formulas for prism: V=LWH or V=Bh Irregular Figures Prism	<ul> <li>Students will be skilled at</li> <li>Calculating volume using models</li> <li>Fluently calculating volume using formulas</li> <li>Applying the formulas for volume of three- dimensional figures</li> <li>Differentiating between volume and the surface area to solve problem for three-dimensional figures</li> <li>Calculating and explaining how to find the area, volume, and surface area for two- and three- dimensional objects from real-world situations</li> </ul>		

	•	volume as the space inside a solid.		
Used in Content Area Standards				21 <sup>st</sup> Century Skills
			•	Collaboration Critical Thinking Communication

Stage 2 - Evidence			
Evaluative Criteria Assessment Evidence			
ASSESSMENT: Written Assessments or Projects			
Other Evidence: independent practice, classroom observations and discussions			

# Windham School District Curriculum **Accelerated Math - Grade 6**

## **Unit 9: Geometry & Data - Statistics & Probability**

Stage 1 Desired Results					
ESTABLISHED GOALS:	Transfer				
Students will continue their study of mathematics in the Students will be able to independently use their learning to					
area of Geometry and Data. In this unit, students will	analyze graphs found in multiple sources				
continue their understanding of data analysis and	<ul> <li>describe data using graphs and measures of central tendency</li> </ul>				
statistical graphs.	Меа	ining			
<ul> <li>Content Standards:</li> <li>CCSS.6.SP.1. Recognize a statistical question as one that anticipates variability in the data related to the question and accounts for it in the answers. CCSS.6.SP.2. Understand that a set of data collected to answer a statistical question has a distribution, which can be described by its center, spread, and overall shape.</li> <li>CCSS.6.SP.3. Recognize that a measure of center for a numerical data set summarizes all of its</li> </ul>	<ul> <li>ENDURING UNDERSTANDINGS</li> <li>A statistical question anticipates variability in the data related to the question and accounts for it in the answers.</li> <li>A set of data collected to answer a statistical question has a distribution, which can be described by its center, spread, and overall shape.</li> <li>A measure of center for a numerical data set summarizes all of its values with a single number, while a measure of variation describes how its values vary with a single number.</li> </ul>	<ul> <li>ESSENTIAL QUESTIONS</li> <li>How are statistics used to collect, analyze, and draw conclusions in today's society?</li> <li>Why are statistics important in the world?</li> <li>What are the ways that data can be represented visually?</li> <li>Why is it better to use different graphs and diagrams to understand data?</li> <li>What are the different ways in which we can summarize data sets?</li> </ul>			
values with a single number, while a measure of variation describes how its values vary with a	Acquisition				
<ul> <li>single number.</li> <li>CCSS.6.SP.4. Display numerical data in plots on a number line, including dot plots, histograms, and box plots.</li> <li>CCSS.6.SP.5. Summarize numerical data sets in relation to their context, such as by:</li> <li>CCSS.6.SP.5. a. Reporting the number observations.</li> </ul>	<ul> <li>line plots, histograms, bar graphs, and scatter plots as visual representations of data.</li> <li>measures of central tendency: mean, median, and the mode.</li> <li>data can be misleading</li> </ul>	<ul> <li>Students will be skilled at</li> <li>Determining measures of central tendency and variation</li> <li>Choosing which measure of central tendency is appropriate for a given set of points</li> <li>Analyzing data from a given dot plot, histogram, and box plots</li> <li>Reporting observations about data using</li> </ul>			

<ul> <li>CCSS.6.SP.5. b. Describing the nature of the attribute under investigation, including how it was measured and its units of measurement.</li> <li>CCSS.6.SP.5. c. Giving quantitative measures of center (median and/or mean) and variability (interquartile range and/or mean absolute deviation), as well as describing any overall pattern and any striking deviations from the overall pattern with reference to the context in which the data were gathered.</li> <li>CCSS.6.SP.5. d. Relating the choice of measures of center and variability to the shape of the data distribution and the context in which the data were gathered.</li> <li>CCSS.MP2 Reason abstractly and quantitatively.</li> <li>CCSS.MP5 Use appropriate tools strategically.</li> <li>CCSS.MP6 Attend to precision</li> </ul>	<ul> <li>Frequency</li> <li>Distribution</li> <li>Symmetric</li> <li>Outliers</li> <li>balance point</li> <li>measures of variation: range, quartile, interquartile range (IQR), absolute deviation, mean absolute deviation</li> <li>Box-and-whisker plot</li> </ul>	•	mathematical vocabulary Summarize and describe distributions using both measures of central tendency as well as variation data Make predictions from graphs
Used in Content Area Standards			21 <sup>st</sup> Century Skills
		•	Communication
		•	Critical Thinking Technology Literacy

Stage 2 - Evidence			
Evaluative Criteria Assessment Evidence			
ASSESSMENT: Written Assessments or Projects			
Other Evidence: independent practice, classroom observations and discussions			

#### Title of Curriculum: 7th Grade Math Curriculum

Unit Name	What (content, vocab)	Why (enduring understandings)	How (skills)
Unit 1: Ratio and Proportional Relationships	<ul> <li>Ratio, rate, unit rate</li> <li>Equivalent ratios</li> <li>Proportional relationship</li> <li>Percent Proportion and Equation</li> <li>Constant rate of change</li> <li>Complex fractions</li> <li>Markups, discounts, sales tax, commission, simple interest</li> </ul>	<ul> <li>A proportion is an equality of ratios.</li> <li>Proportional relationships guide many aspects of life: nature, drawings, and financial scenarios.</li> <li>The connections between percents, decimals, and fractions are critical to help order, analyze, construct, and make predictions in everyday real-world and mathematical situations.</li> </ul>	<ul> <li>Solve percent equations using proportions</li> <li>Calculate discount or sale price of an item</li> <li>Calculate sales tax</li> <li>Solve percent word problems including percent change and percent error</li> <li>Express proportions in tables and graphs</li> <li>Express a proportional relationship in an equation</li> <li>Graph proportional relationship</li> </ul>
Unit 2: The Number System	<ul> <li>Absolute value</li> <li>Zero pairs</li> <li>Additive inverse</li> <li>Operations with integers</li> <li>Order of Operations</li> <li>Rational Numbers</li> <li>Terminating and repeating decimals</li> </ul>	<ul> <li>The properties of operations for whole numbers hold true for rational numbers.</li> <li>Rational numbers are all numbers that can be written as a fraction including natural numbers, whole numbers and integers.</li> </ul>	<ul> <li>numbers on a number line</li> <li>Add, subtract, multiply, and divide with integers</li> </ul>
Unit 3: Expressions and Equations	<ul> <li>Distributive Property</li> <li>Algebraic Properties</li> <li>Inequalities</li> </ul>	Real world situations can be represented symbolically	<ul> <li>Simplify algebraic expressions with rational numbers</li> </ul>

	<ul> <li>Variables, constants, and coefficients</li> <li>Like terms</li> <li>Equivalent expressions and equations</li> </ul>	<ul> <li>with expressions and equations.</li> <li>An equation is formed by two equivalent expressions.</li> <li>Equivalent equations represent the same value in unique forms.</li> </ul>	<ul> <li>Create algebraic expressions from verbal expressions</li> <li>Define a variable and create an equation from a word problem</li> <li>Create and solve one-step equations with integers by balancing the equation</li> <li>Solve two-step equations by using equivalent equations</li> <li>Create and solve one- and two- step inequalities</li> <li>Graph inequalities on a number line</li> <li>Rewrite expressions in different forms</li> <li>Solve problems with fractional coefficients</li> <li>Check for reasonableness of solutions</li> <li>Finding the Greatest Common Factor for monomials</li> <li>Factor linear expressions using the distributive property</li> </ul>
Geometry - Circle/Scale	<ul> <li>Circumference and area</li> <li>Composite figures</li> <li>Scale drawings</li> <li>Scale factor</li> </ul>	<ul> <li>Scale drawings are proportional to one another by a measure called the scale factor.</li> <li>Proportional relationships can be used to draw geometric figures at differing scales.</li> <li>A circle is a closed shape that is defined by the set of points that are the same distance from the center of the circle.</li> </ul>	<ul> <li>Explain the change in area and volume when applying scale factor</li> </ul>
Geometry – Angles and Triangles	<ul> <li>Properties of triangles</li> <li>Classification of triangles: acute, obtuse, right</li> </ul>	<ul> <li>Drawings and constructions help to see the relationships and differences between geometrical figures.</li> </ul>	<ul> <li>Create triangles given specific sides and/or angles</li> <li>Determine the missing angles in triangles</li> <li>Classify triangles by their sides and angles</li> </ul>

		•	Analyzing geometric relationships develops reasoning and justification skills. Angle relationships can be used to determine missing angle measures in diagrams.	•	determine the missing angles in polygons. break polygons into triangles and computing the sum of interior angles. classify angle pair relationships. create algebraic equations using angle pair relationships.
Statistics	<ul> <li>Measures of Central Tendency</li> <li>Dispersion of data</li> <li>Variation</li> <li>Sampling Techniques</li> <li>Bias</li> <li>Valid and Invalid inferences</li> <li>Comparing data sets</li> </ul>	•	A statistical question anticipates variability in the data related to the question and accounts for it in the answers. A set of data collected to answer a statistical question has a distribution, which can be described by its center, spread, and overall shape.	• • •	Create data with specific mode, median, and mean Identify when a measure of center is not an accurate reflection of data Use data from a random sample to draw inferences about a population Analyze data to make predictions Display two samples of data on a box plot to illustrate variability Create a line plot to compare two samples
Probability	<ul> <li>Probability is between and includes 0 and 1</li> <li>Experimental probability</li> <li>Theoretical Probability</li> <li>Tree diagrams</li> <li>Dependent and independent events</li> <li>Compound probability</li> <li>possible and favorable outcomes</li> </ul>	•	Probability is used to predict the likelihood of an event and make decisions. Key to valuable experimental probability is good data.	•	Perform an activity, record results and calculate experimental probability. Compare different experimental probabilities for the same activity and explain the differences. Compare and explain experimental versus theoretical probability. Make predictions based on probability. Create tree diagrams to find total possible outcomes. Express probability as fractions and percents. Identify an event that would have a probability of zero and one. Calculate compound probability of both dependent and independent events.

# **Unit 1: Ratio & Proportional Relationships**

	Stage 1 Desired Results			
ESTABLISHED GOALS:	Transfer			
Students will continue their study of mathematics in the Students will be able to independently use their learning to				
area of algebra. In this unit, students will gain a deeper	<ul> <li>solve real-world problem using proportional relationships and percent relationships</li> </ul>			
understanding of ratio and proportional relationships	connect proportional relationships to linear relationships			
and apply to real world applications.	apply proportional reasoning to solve problems	involving scale factor		
	Меа	nning		
Content Standards:	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS		
• CCSS.7.RP.1. Compute unit rates associated with	• A proportion is an equality of ratios.	• What is the better deal?		
ratios of fractions, including ratios of lengths,	• Proportional relationships guide many aspects	• How can proportions be used to solve a variety		
areas and other quantities measured in like or	of life: nature, drawings, and financial	of problems?		
different units.	scenarios.			
CCSS.7.RP.2. Recognize and represent	• The connections between percents, decimals,			
proportional relationships between quantities.	and fractions are critical to help order, analyze,			
CCCC 7 DD2 lies are artical relationships to	construct, and make predictions in everyday			
CCSS.7.RP.3. Use proportional relationships to     column and percent problems	real-world and mathematical situations.			
solve multistep ratio and percent problems.		isition		
		Students will be skilled at		
markdowns, gratuities and commissions, fees,	• unit rate is the rate of change based on one.	<ul> <li>calculating complex unit rates.</li> </ul>		
percent increase and decrease, percent error.	• a proportion is two ratios that are equivalent.	<ul> <li>solving a percent equation using proportions.</li> </ul>		
CCSS.MP1 Make sense of problems and persevere	• a complex fraction is a comparison of decimals	• calculating the discount and the sale price of an		
in solving them.	or mactions and may be expressed as a simple	item.		
<ul> <li>CCSS.MP2 Reason abstractly and quantitatively.</li> </ul>	fraction.	• calculating sales tax.		
<ul> <li>CCSS.MP2 Reason abstractly and quantitatively.</li> <li>CCSS.MP6 Attend to precision.</li> </ul>	constant of proportionality is the rate of	<ul> <li>solving percent word problems involving</li> </ul>		
<ul> <li>CCSS.MP7 Look for and make use of structure.</li> </ul>	change.	percent change and percent error.		
	• the graph of a proportional relationship is a	• expressing proportions in tables and graphs.		
	straight line that goes through the origin.			

<ul> <li>CCSS.MP8 Look for and express regularity in repeated reasoning.</li> </ul>	<ul> <li>the concept of interest.</li> <li>commission is money earned based on sales.</li> <li>markups, markdowns, and sales tax are related to sales.</li> </ul>	•	expressing a proportional relationship in an equation. graphing proportional relationships. interpreting a point in the graph in the context of a word problem.
Used in Content Area Standards		<b>21</b> <sup>st</sup>	<sup>t</sup> Century Skills
		٠	Critical Thinking
		•	Communication

Stage 2 - Evidence			
Evaluative Criteria	Assessment Evidence		
	ASSESSMENT: Written Assessments or Projects		
Other Evidence: independent practice, classroom observations and discussions			

## **Unit 2: The Number System**

	Stage 1 Desired Results			
ESTABLISHED GOALS:	Trar	nsfer		
Students will continue their study of mathematics in the	Students will be able to independently use their lea	rning to		
area of numbers and operations. In this unit, students	<ul> <li>recognize rational numbers, especially signed nι</li> </ul>	umbers, as they relate to real world scenarios		
will gain a deeper understanding of the number system,	<ul> <li>fluently add, subtract, multiply and divide ration</li> </ul>	al numbers.		
and will operate with rational numbers.	<ul> <li>solve equations and inequalities with rational nu</li> </ul>	umbers.		
	Меа	ining		
<ul> <li>Content Standards:</li> <li>CCSS.7.NS.1. Apply and extend previous understandings of addition and subtraction to add and subtract rational numbers; represent addition and subtraction on a horizontal or vertical number line diagram.</li> <li>CCSS.7.NS.2. Apply and extend previous</li> </ul>	<ul> <li>ENDURING UNDERSTANDINGS</li> <li>The properties of operations for whole numbers hold true for rational numbers.</li> <li>Rational numbers are all numbers that can be written as a fraction including natural numbers, whole numbers and integers.</li> </ul>	<ul> <li>ESSENTIAL QUESTIONS</li> <li>How are integers related to science, social studies and language arts?</li> <li>How do you represent rational numbers?</li> </ul>		
understandings of multiplication and division and	Acquisition			
<ul> <li>understandings of multiplication and division and of fractions to multiply and divide rational numbers.</li> <li>CCSS.7.NS.3. Solve real-world and mathematical problems involving the four operations with rational numbers.</li> <li>CCSS.MP1 Make sense of problems and persevere in solving them.</li> <li>CCSS.MP2 Reason abstractly and quantitatively.</li> <li>CCSS.MP4 Model with mathematics.</li> </ul>		<ul> <li>Students will be skilled at</li> <li>ordering and comparing rational numbers.</li> </ul>		

	•	converting common fractions to decimals without a calculator. solving real world problems involving rational numbers.
Used in Content Area Standards		21 <sup>st</sup> Century Skills
	•	Critical Thinking
	•	Problem solving
	•	Communication

Stage 2 - Evidence			
Evaluative Criteria	Assessment Evidence		
	ASSESSMENT: Written Assessments or Projects		
Other Evidence: independent practice, classroom observations and discussions			

# **Unit 3: Expressions & Equations**

Stage I Desired Results					
ESTABLISHED GOALS:	Transfer				
Students will continue their study of mathematics in the Students will be able to independently use their learning to					
area of algebra. In this unit, students will gain a deeper	<ul> <li>represent scenarios using expressions and equations.</li> </ul>				
understanding of solving real-world problems involving	<ul> <li>use equations as a method to solve real-world p</li> </ul>	roblems.			
expressions and equations.	Меа	ining			
<ul> <li>Content Standards:</li> <li>CCSS.7.EE.1. Apply properties of operations as strategies to add, subtract, factor, and expand linear expressions with rational coefficients.</li> <li>CCSS.7.EE.2. Understand that rewriting an expression in different forms in a problem context</li> </ul>	<ul> <li>Real world situations can be represented symbolically with expressions and equations.</li> <li>An equation is formed by two equivalent expressions.</li> <li>Equivalent equations represent the same value</li> </ul>	<ul> <li>ESSENTIAL QUESTIONS</li> <li>How do you compare algebraic solutions to arithmetic solutions?</li> <li>How do you translate real world problems to algebraic expressions?</li> <li>Does my answer make sense?</li> </ul>			
can shed light on the problem and how the	Acquisition				
<ul> <li>quantities in it are related.</li> <li>CCSS.7.EE.3. Solve multi-step real-life and mathematical problems posed with positive and negative rational numbers in any form (whole numbers, fractions, and decimals), using tools strategically. Apply properties of operations to calculate with numbers in any form; convert between forms as appropriate; and assess the reasonableness of answers using mental computation and estimation strategies.</li> <li>CCSS.7.EE.4. Use variables to represent quantities in a real-world or mathematical problem, and</li> </ul>	<ul> <li>Students will understand</li> <li>the difference between a constant and a coefficient, including coefficients of one.</li> <li>like terms are terms with the same variable.</li> <li>equivalent expressions have the same value.</li> <li>an algebraic equation may have a solution.</li> <li>an inequality states two values are not the same.</li> <li>commutative, associative, identity, distributive, and inverse properties.</li> <li>a monomial is a single term.</li> </ul>	<ul> <li>Students will be skilled at</li> <li>simplifying algebraic expressions with rational numbers.</li> <li>creating algebraic expressions from verbal expressions.</li> <li>defining a variable and creating an equation from a word problem.</li> <li>creating and solving one-step equations with integers by balancing the equation.</li> <li>solving two-step equations by using equivalent equations.</li> <li>graphing inequalities on a number line.</li> </ul>			

<ul> <li>construct simple equations and inequalities to solve problems by reasoning about the quantities.</li> <li>CCSS.MP1 Make sense of problems and persevere in solving them.</li> <li>CCSS.MP3 Construct viable arguments and critique the reasoning of others.</li> <li>CCSS.MP7 Look for and make use of structure.</li> </ul>	<ul> <li>creating and solving one and two-step inequalities.</li> <li>rewriting expressions in a different form; example ½ of x = .5x = x/2</li> <li>solving problems with fractional coefficients.</li> <li>checking for the reasonableness of the solution.</li> <li>finding the Greatest Common Factor for monomials.</li> <li>factoring linear expressions using distributive property.</li> </ul>
Used in Content Area Standards	21 <sup>st</sup> Century Skills
	<ul> <li>Critical Thinking</li> <li>Collaboration</li> <li>Communication</li> </ul>

Stage 2 - Evidence			
Evaluative Criteria	Assessment Evidence		
	ASSESSMENT: Written Assessments or Projects		
	Other Evidence: independent practice, classroom observations and discussions		

# **Unit 4: Geometry - Circles/Scale**

	Stage 1 Desired Results			
ESTABLISHED GOALS:	Transfer			
Students will continue their study of mathematics in the	Students will be able to independently use their learn	ing to		
area of geometry. In this unit, students will gain a	• apply areas and circumferences of circles when fir			
deeper understanding of finding area and	real-life problems.			
circumference of a circle, as well as using scale to	<ul> <li>apply proportional reasoning to solve problems in</li> </ul>	volving scale factor		
produce new figures.	Mean	ing		
	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS		
Content Standards:	• Scale drawings are proportional to one another	<ul> <li>How can we determine area, given</li> </ul>		
CCSS.7.G.A.1 Solve problems involving scale	by a measure called the scale factor.	circumference?		
drawings of geometric figures, including	• Proportional relationships can be used to draw	• Can we determine diameter or radius, given		
computing actual lengths and areas from a scale	geometric figures at differing scales.	area or circumference?		
drawing and reproducing a scale drawing at a	• A circle is a closed shape that is defined by the	• What kinds of problems can you solve using		
different scale.	set of points that are the same distance from the			
• CCSS.7.G.B.4 Know the formulas for the area and	center of the circle.	• How can you use proportions to investigate		
circumference of a circle and use them to solve		real-world and mathematical objects at		
problems; give an informal derivation of the relationship between the circumference and area		different scales?		
of a circle.	Acquisi			
		Students will be skilled at		
• CCSS.MP1 Make sense of problems and persevere in solving them.	• circumference of a circle is the distance around	• Calculating circumference and area of circles		
<ul> <li>CCSS.MP2 Reason abstractly and quantitatively.</li> </ul>	the circle.	Drawing similar figures using scale factor		
<ul> <li>CCSS.MP2 Reason abstractly and quantitatively.</li> <li>CCSS.MP5 Use appropriate tools strategically.</li> </ul>	• formula for calculating the circumference of a	• Finding missing lengths given similar figures		
<ul> <li>CCSS.MP6 Attend to precision.</li> </ul>	circle is C = d $\pi$ or C = 2 $\pi$ r where C is the	• Explaining the change in area and volume		
• cess.ivii o Attenu to precision.	circumference of a circle, d is the length of the	when applying scale factor		
	diameter of the circle, r is the length of the radius			
	of the circle, and $\pi$ is represented using the			
	approximation 3.14.			

	<ul> <li>formula for calculating the area of a circle is A = πr<sup>2</sup></li> <li>Scale drawings are representations of real objects or places that are in proportion to the real objects or places they represent.</li> <li>scale of a drawing is the ratio drawing length : actual length</li> <li>scale of a map is the ratio map distance : actual distance.</li> <li>When calculating the area of a scaled figure, the scale must be applied to all dimensions of the figure.</li> </ul>	
Used in Content Area Standards		21 <sup>st</sup> Century Skills
•		<ul> <li>Technology Literacy</li> <li>Critical Thinking</li> <li>Collaboration</li> </ul>

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
Other Evidence: independent practice, classroom observations and discussions		

# **Unit 5: Geometry - Angles & Triangles**

	Stage 1 Desired Results		
ESTABLISHED GOALS:	Transfer		
Students will continue their study of mathematics in	Students will be able to independently use their learning to		
the area of geometry. In this unit, students will gain a	<ul> <li>use angles and triangles to solve real-world problems involving geometric figures.</li> </ul>		
deeper understanding of angles and triangles, and will	<ul> <li>use vocabulary and properties in future studies of Geometry.</li> </ul>		
solve real-world problems involving geometric figures.	Мес	aning	
		ESSENTIAL QUESTIONS	
Content Standards:	• Drawings and constructions help to see the	How do geometric models describe spatial	
• CCSS.7.G.2. Draw (freehand, with ruler and	relationships and differences between	relationships?	
protractor, and with technology) geometric	geometrical figures.	What are the major classifications and	
shapes with given conditions. Focus on	Analyzing geometric relationships develops	relationships of angles and triangles?	
constructing triangles from three measures of angles or sides, noticing when the conditions	reasoning and justification skills.		
determine a unique triangle, more than one	Angle relationships can be used to determine		
triangle, or no triangle.	missing angle measures in diagrams.	• • • •	
<ul> <li>CCSS.7.G.5. Use facts about supplementary,</li> </ul>	•	isition	
complementary, vertical, and adjacent angles in a		Students will be skilled at	
multi-step problem to write and solve simple	<ul> <li>the requirements for three segments to form a triangle</li> </ul>		
equations for an unknown angle in a figure.	triangle.	angles.	
<ul> <li>CCSS.MP4 Model with mathematics.</li> </ul>	• there are 180 degrees in every triangle.	<ul> <li>finding missing angles in a triangle.</li> </ul>	
<ul> <li>CCSS.MP5 Use appropriate tools strategically.</li> </ul>	<ul> <li>the classifications of triangles for both sides</li> </ul>	<ul> <li>classifying a triangle by both its sides and its</li> </ul>	
<ul> <li>CCSS.MP6 Attend to precision.</li> </ul>	and angles.	angles.	
	<ul> <li>the characteristics of a regular polygon.</li> <li>the different angle pair relationships: adjacent.</li> </ul>	<ul> <li>determining the missing angles in polygons.</li> <li>broaking polygons into triangles and computing</li> </ul>	
		<ul> <li>breaking polygons into triangles and computing the sum of interior angles</li> </ul>	
	vertical, complementary, supplementary, and linear pair.	<ul><li>the sum of interior angles.</li><li>classifying angle pair relationships.</li></ul>	
	<ul> <li>congruent angles are angles with the same</li> </ul>	<ul> <li>creating algebraic equations using angle pair</li> </ul>	
	measure.	relationships.	

Used in Content Area Standards	21 <sup>st</sup> Century Skills
	Critical Thinking
	Communication

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
Other Evidence: independent practice, classroom observations and discussions		

# Windham School District Curriculum Mathematics - Grade 7 Unit 6: Statistics

Stage 1 Desired Results			
ESTABLISHED GOALS:	Transfer		
Students will continue their study of mathematics in the Students will be able to independently use their learning to			
area of data and problem solving. In this unit, students	<ul> <li>analyze and interpret data from real-world situations.</li> </ul>		
will gain a deeper understanding of statistics, by	Мес	aning	
analyzing and interpreting data from real-world	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS	
problems.	• A statistical question anticipates variability in the data related to the question and accounts	<ul> <li>How do you interpret data from statistical representations?</li> </ul>	
Content Standards:	for it in the answers.		
• CCSS.7.SP.1 Understand that statistics can be used	• A set of data collected to answer a statistical		
to gain information about a population by	question has a distribution, which can be		
examining a sample of the population;	described by its center, spread, and overall		
generalizations about a population from a sample	shape.		
are valid only if the sample is representative of	Acqu	isition	
that population. Understand that random sampling	Students will understand	Students will be skilled at	
tends to produce representative samples and	<ul> <li>characteristics of each measure of central</li> </ul>	• creating data with a specific mode, median and	
support valid inferences.	tendency.	mean.	
CCSS.7.SP.2. Use data from a random sample to	• dispersion of data is the way it is spread out.	<ul> <li>identifying when a measure of central tendency</li> </ul>	
draw inferences about a population with an unknown characteristic of interest. Generate	• the less variation a set has, the closer the	would not be an accurate reflection of the data.	
	numbers are to each other.	<ul> <li>using data from a random sample to draw</li> </ul>	
multiple samples (or simulated samples) of the	<ul> <li>random sampling gives unbiased data.</li> </ul>	inferences about a population.	
same size to gauge the variation in estimates or predictions.	• a valid inference is a prediction based on a	analyzing data to make a prediction.	
<ul> <li>CCSS.7.SP.3. Informally assess the degree of visual</li> </ul>	random sample.	• displaying two samples of data in a box plot to	
overlap of two numerical data distributions with		illustrate variability.	
similar variabilities, measuring the difference		• creating a line plot to compare two samples.	
	1	1	

<ul> <li>between the centers by expressing it as a multiple of a measure of variability.</li> <li>CCSS.7.SP.4. Use measures of center and measures of variability for numerical data from random samples to draw informal comparative inferences about two populations.</li> <li>CCSS.MP3 Construct viable arguments and critique the reasoning of others.</li> <li>CCSS.MP4 Model with mathematics.</li> <li>CCSS.MP5 Use appropriate tools strategically.</li> </ul>	
Used in Content Area Standards	21 <sup>st</sup> Century Skills
	Communication
	Critical Thinking

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
Other Evidence: independent practice, classroom observations and discussions		

# Windham School District Curriculum Mathematics - Grade 7 Unit 7: Probability

Stage 1 Desired Results			
ESTABLISHED GOALS:	Transfer		
Students will continue their study of mathematics in the Students will be able to independently use their learning to			
area of data and problem solving. In this unit, students	solve real-world problems involving chance.		
will gain a deeper understanding of probability to solve	<ul> <li>make good choices by using their knowledge of the second se</li></ul>	the probability of events	
real-world problems involving chance.	Меа	ning	
	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS	
Content Standards:	• Probability is used to predict the likelihood of	<ul> <li>What makes a game fair?</li> </ul>	
• CCSS.7.SP.C.5 Understand that the probability of a	an event and make decisions.	<ul> <li>How are probabilities used to make everyday</li> </ul>	
chance event is a number between 0 and 1 that	<ul> <li>Key to valuable experimental probability is</li> </ul>	decisions?	
expresses the likelihood of the event occurring.	good data.		
Larger numbers indicate greater likelihood. A	Acqui	isition	
	Students will understand	Students will be skilled at	
probability around 1/2 indicates an event that is	• probability is the likelihood that something will	<ul> <li>performing an activity, recording results and</li> </ul>	
neither unlikely nor likely, and a probability near 1	happen.	calculating experimental probability.	
indicates a likely event.	<ul> <li>experimental probability is based on someone's</li> </ul>		
<ul> <li>CCSS.7.SP.C.6 Approximate the probability of a change guest by collecting data on the change</li> </ul>	results.	for the same activity and explaining the	
chance event by collecting data on the chance	• theoretical probability is based on what exists.	difference.	
process that produces it and observing its long-run	<ul> <li>possible outcomes and favorable outcomes.</li> </ul>	• comparing and explaining experimental versus	
relative frequency, and predict the approximate	<ul> <li>equally likely outcomes are results that have</li> </ul>	theoretical probability.	
relative frequency given the probability.	the same probability of happening.	<ul> <li>making predictions based on probability.</li> </ul>	
<ul> <li>CCSS.7.SP. C.7 Develop a probability model and use it to find probabilities of events. Compare</li> </ul>	<ul> <li>tree diagrams as a method for finding all</li> </ul>	<ul> <li>creating tree diagrams to find total possible</li> </ul>	
probabilities from a model to observed	possible outcomes.	outcomes.	
frequencies; if the agreement is not good, explain	• probability of an outcome ranges between 0	<ul> <li>expressing probability as fractions and</li> </ul>	
possible sources of the discrepancy.	(never happening) and 1 (always happening).	percents.	
possible sources of the discrepancy.	• compound probability is used when more than	<ul> <li>identifying an event that would have a</li> </ul>	
	one event is happening.	probability of zero.	

<ul> <li>CCSS.7.SP.C.8 Find probabilities of compound events using organized lists, tables, tree diagrams, and simulation.</li> <li>CCSS.MP2 Reason abstractly and quantitatively.</li> <li>CCSS.MP4 Model with mathematics.</li> </ul>	• probability is either independent or dependent.	<ul> <li>identifying an event that would have a probability of one.</li> <li>calculating compound probability of both dependent and independent events.</li> </ul>
Used in Content Area Standards		21 <sup>st</sup> Century Skills
		Communication
		Critical Thinking

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
Other Evidence: independent practice, classroom observations and discussions		

Title of Curriculum: 7th Grade Accelerated Math

Unit Name	What (content, vocab)	Why (enduring understandings)	How (skills)
Unit 1: Ratio and Proportional Relationships	<ul> <li>Ratio, rate, unit rate</li> <li>Equivalent ratios</li> <li>Proportional relationship</li> <li>Percent Proportion and Equation</li> <li>Constant rate of change</li> <li>Complex fractions</li> <li>Markups, discounts, sales tax, commission, simple interest</li> </ul>	<ul> <li>A proportion is an equality of ratios.</li> <li>Proportional relationships guide many aspects of life: nature, drawings, and financial scenarios.</li> <li>The connection between percents, decimals, and fractions is essential to help order, analyze, construct, and make predictions in everyday real-world and mathematical situations.</li> </ul>	<ul> <li>Calculate complex unit rates</li> <li>Solve a percent equation</li> <li>Calculate discount or sale price of an item</li> <li>Calculate sales tax</li> <li>Solve percent word problems including percent change and percent error</li> <li>Express proportions in tables and graphs</li> <li>Express a proportional relationship in an equation</li> <li>Interpret a point on a graph in context</li> </ul>
Unit 2: The Number System	<ul> <li>Absolute value</li> <li>Zero pairs</li> <li>Additive inverse</li> <li>Operations with integers</li> <li>Order of Operations</li> <li>Rational Numbers</li> <li>terminating and repeating decimals</li> </ul>	<ul> <li>The properties of operations for whole numbers hold true for rational numbers.</li> <li>Rational numbers are all numbers that can be written as a fraction including natural numbers, whole numbers and integers.</li> </ul>	<ul> <li>Order and compare rational numbers</li> <li>Determine if a number is rational or irrational</li> </ul>

Unit 3: Expressions and Equations	<ul> <li>Distributive Property</li> <li>Monomials</li> <li>Binomials</li> <li>Algebraic Properties</li> <li>Inequalities</li> <li>Variables, constants, and coefficients</li> <li>Like terms</li> <li>Equivalent expressions and equations</li> </ul>	<ul> <li>Real world situations can be represented symbolically with expressions and equations.</li> <li>An equation is formed by two equivalent expressions.</li> <li>Equivalent equations represent the same value in unique forms.</li> </ul>	<ul> <li>Estimate, to the nearest whole number, non-perfect square roots</li> <li>Simplify algebraic expressions with rational numbers</li> <li>Create algebraic expressions from verbal expressions</li> <li>Define a variable and create an equation from a word problem</li> <li>Solve one-step equations with integers by balancing the equation</li> <li>Solve two-step equations by using equivalent equations</li> <li>Create and solve one- and two- step inequalities</li> <li>Rewrite expressions in different forms</li> <li>Solve problems with fractional coefficients</li> <li>Check for reasonableness of solutions</li> <li>Find GCF for monomials</li> <li>Factor linear expressions using the distributive property</li> </ul>
Unit 4: Transformations	<ul> <li>Transformations</li> <li>Congruence</li> <li>Similarity</li> </ul>	<ul> <li>Congruent objects can be transformed on top of each other.</li> <li>Similar objects are a combination of rigid motions and dilation.</li> </ul>	<ul> <li>Transform polygons using dilations, translations, reflections, and rotations.</li> <li>Identify coordinates of transformed figures.</li> <li>Describe sequence of transformations that result in congruent or similar figures.</li> </ul>
Unit 5: Angles and Transversals	<ul> <li>Triangle angle relationships</li> <li>Angles formed by parallel lines cut by a transversal</li> <li>Interior, exterior, and corresponding angles</li> </ul>	<ul> <li>Analyzing geometric relationships develops reasoning and justification skills.</li> <li>Angle relationships can be used to determine missing angle measures in diagrams.</li> </ul>	<ul> <li>classify angle pair relationships.</li> <li>create algebraic equations using angle pair relationships.</li> </ul>

Unit 6: Pythagorean Theorem	<ul> <li>Pythagorean Theorem</li> <li>Right Triangles</li> <li>Area of squares</li> <li>Radicals</li> </ul>	<ul> <li>Right triangles have a special relationship among the side lengths which can be represented by a model and a formula.</li> </ul>	<ul> <li>and interior angles, and parallel lines cut by a transversal.</li> <li>Informally prove the Pythagorean Theorem</li> <li>Determine if a triangle is a right triangle using its converse.</li> <li>Apply the Pythagorean Theorem to find missing triangle side lengths.</li> <li>Apply the Pythagorean Theorem to solve problems</li> </ul>
Unit 7: Geometry - Volume	<ul> <li>Cylinder</li> <li>Cones</li> <li>Spheres</li> </ul>	<ul> <li>Everyday objects have a variety of attributes, each of which can be measured in many ways.</li> <li>Area, surface area and volume have applications in real world situations.</li> <li>Different 3-dimensional figures can have the same volume even if the dimensions are not all the same.</li> </ul>	<ul><li>and spheres using appropriate formulas and units.</li><li>Use volume formulas to solve real world problems.</li></ul>
Unit 8: Statistics	<ul> <li>Measures of Central Tendency</li> <li>Dispersion of data</li> <li>Variation</li> <li>Sampling Techniques</li> <li>Bias</li> <li>Valid and Invalid inferences</li> <li>Comparing data sets</li> </ul>	<ul> <li>A statistical question anticipates variability in the data related to the question and accounts for it in the answers.</li> <li>A set of data collected to answer a statistical question has a distribution, which can be described by its center, spread, and overall shape.</li> </ul>	not an accurate reflection of data
Unit 9: Probability	<ul> <li>Probability is between and includes 0 and 1</li> <li>Experimental probability</li> </ul>	• Probability is used to predict the likelihood of an event and make decisions.	• Perform an activity, record results and calculate experimental probability.

<ul> <li>Theoretical Probability</li> <li>Tree diagrams</li> <li>Dependent and independent events</li> <li>Compound probability</li> <li>possible and favorable outcomes</li> </ul>	<ul> <li>Key to valuable experimental probability is good data.</li> </ul>	<ul> <li>Compare different experimental probabilities for the same activity and explain the differences.</li> <li>Make predictions based on probability.</li> <li>Create tree diagrams to find total possible outcomes.</li> <li>Express probability as fractions and percents.</li> <li>Identify an event that would have a probability of zero and one.</li> <li>Calculate compound probability of both dependent and independent events.</li> </ul>
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# Windham School District Curriculum **Accelerated Mathematics - Grade 7 Unit 1: Ratio & Proportional Relationships**

Stage 1 Desired Results		
ESTABLISHED GOALS:	Trai	nsfer
Students will continue their study of mathematics in the	Students will be able to independently use their lea	rning to
area of algebra. In this unit, students will gain a deeper	<ul> <li>solve real-world problem using proportional relation</li> </ul>	ationships and percent relationships
understanding of ratio and proportional relationships	<ul> <li>connect proportional relationships to linear relationships</li> </ul>	ntionships
and apply these concepts to real world applications.	<ul> <li>apply proportional reasoning to solve problems</li> </ul>	involving scale factor
Content Standards:	Мес	aning
<ul> <li>CCSS.7.RP.1. Compute unit rates associated with ratios of fractions, including ratios of lengths, areas and other quantities measured in like or different units.</li> <li>CCSS.7.RP.2. Recognize and represent proportional relationships between quantities.</li> <li>CCSS.7.RP.3. Use proportional relationships to solve multistep ratio and percent problems.</li> </ul>	<ul> <li>Proportional relationships guide many aspects of life: nature, drawings, and financial scenarios.</li> <li>The connection between percents, decimals, and fractionsis critical to help order, analyze,</li> </ul>	<ul> <li>ESSENTIAL QUESTIONS</li> <li>What is the better deal?</li> <li>How can proportions be used to solve a variety of problems?</li> </ul>
Examples: simple interest, tax, markups and markdowns, gratuities and commissions, fees, percent increase and decrease, percent error.	construct, and make predictions in everyday real-world and mathematical situations. Acqu Students will understand	<b>isition</b> Students will be skilled at
<ul> <li>CCSS.MP1 Make sense of problems and persevere in solving them.</li> <li>CCSS.MP2 Reason abstractly and quantitatively.</li> <li>CCSS.MP6 Attend to precision.</li> <li>CCSS.MP7 Look for and make use of structure.</li> <li>CCSS.MP8 Look for and express regularity in repeated reasoning.</li> </ul>	<ul> <li>unit rate is the rate of change based on one.</li> <li>a proportion is two ratios that are equivalent.</li> <li>a complex fraction is a comparison of decimals or fractions and may be expressed as a simple fraction.</li> <li>constant of proportionality is the rate of change.</li> <li>linear equation will graph as a line due to constant rate of change.</li> </ul>	<ul> <li>calculating complex unit rates.</li> <li>solving a percent equation using proportions.</li> <li>calculating the discount and the sale price of an item.</li> <li>calculating sales tax.</li> <li>solving percent word problems involving percent change and percent error.</li> <li>expressing proportions in tables and graphs.</li> </ul>

	<ul> <li>graph of a proportional relationship is a straight line that goes through the origin.</li> <li>percent is the ratio of the percent to one hundred.</li> <li>Interest as both extra return and extra payment</li> <li>commission is money earned based on sales.</li> <li>markups, markdowns, and sales tax are related to sales.</li> </ul>	<ul><li>equation.</li><li>intercepting a point in the graph in the context of a word problem.</li></ul>
Used in Content Area Standards		21 <sup>st</sup> Century Skills
		Critical Thinking
		Communication

Stage 2 - Evidence	
Evaluative Criteria	Assessment Evidence
ASSESSMENT: Written Assessments or Projects	
Other Evidence: independent practice, classroom observations and discussions	

# Windham School District Curriculum Accelerated Mathematics - Grade 7 Unit 2: The Number System

	Stage I Desired Results	
ESTABLISHED GOALS:	Trar	nsfer
Students will continue their study of mathematics in the	Students will be able to independently use their lea	rning to
area of numbers and operations. In this unit, students	<ul> <li>fluently add, subtract, multiply and divide ration</li> </ul>	nal numbers.
will gain a deeper understanding of the number system	<ul> <li>solve equations and inequalities with rational nu</li> </ul>	umbers.
and will calculate with rational numbers.	Меа	aning
<ul> <li>Content Standards:</li> <li>CCSS.7.NS.1. Apply and extend previous</li> </ul>	<ul> <li>ENDURING UNDERSTANDINGS</li> <li>The properties of operations for whole numbers hold true for rational numbers.</li> </ul>	<ul> <li>ESSENTIAL QUESTIONS</li> <li>How are integers related to science, social studies and language arts?</li> </ul>
understandings of addition and subtraction to add and subtract rational numbers; represent addition and subtraction on a horizontal or vertical number line diagram.	<ul> <li>Rational numbers are all numbers that can be written as a fraction including natural numbers, whole numbers and integers.</li> </ul>	How do you represent rational numbers?
CCSS.7.NS.2. Apply and extend previous	Acqui	isition
<ul> <li>understandings of multiplication and division and of fractions to multiply and divide rational numbers.</li> <li>CCSS.7.NS.3. Solve real-world and mathematical problems involving the four operations with rational numbers.</li> <li>CCSS.MP1 Make sense of problems and persevere in solving them.</li> <li>CCSS.MP2 Reason abstractly and quantitatively.</li> <li>CCSS.MP4 Model with mathematics.</li> </ul>	<ul> <li>Students will understand</li> <li>additive inverses as zero pairs.</li> <li>that addition and subtraction are inverse operations and that subtraction problems can be changed to addition problems by adding the inverse.</li> <li>adding the additive inverse.</li> <li>the rules for addition, subtraction, multiplication and division of integers.</li> <li>exponents, square roots, and cube roots.</li> <li>that zero cannot be a divisor.</li> <li>that a fraction must be equivalent to either a terminating or a repeating decimal.</li> </ul>	<ul> <li>Students will be skilled at</li> <li>ordering and comparing rational numbers.</li> <li>determining if a number is rational or irrational.</li> <li>modeling addition and subtraction of signed numbers on a number line.</li> <li>adding, subtracting, multiplying and dividing rational numbers.</li> <li>using the order of operations with rational numbers.</li> <li>evaluating algebraic expressions with integers values.</li> <li>converting common fractions to decimals without a calculator.</li> </ul>

	<ul> <li>the difference between a rational and irrational number.</li> </ul>	<ul> <li>Solve real-world problems involving rational numbers.</li> <li>finding square roots of perfect squares and cube roots of perfect cubes.</li> <li>interpreting sums of rational numbers in a real-world context.</li> <li>solving real world problems involving rational numbers.</li> </ul>
Used in Content Area Standards		21 <sup>st</sup> Century Skills
		Critical Thinking
		Perseverance
		Communication

Stage 2 - Evidence	
Evaluative Criteria Assessment Evidence	
ASSESSMENT: Written Assessments or Projects	
Other Evidence: independent practice, classroom observations and discussions	

# Windham School District Curriculum Accelerated Mathematics - Grade 7 Unit 3: Expressions & Equations

Stage 1 Desired Results		
ESTABLISHED GOALS:	Tran	nsfer
Students will continue their study of mathematics in the Students will be able to independently use their learning to		
area of algebra. In this unit, students will gain a deeper	<ul> <li>solve real-world problems using numerical and a</li> </ul>	algebraic expressions and equations.
understanding of solving real-world problems involving	<ul> <li>use linear equations to solve more advanced ma</li> </ul>	athematical equations
expressions and equations.	Меа	ining
<ul> <li>Content Standards:</li> <li>CCSS.7.EE.1. Apply properties of operations as strategies to add, subtract, factor, and expand linear expressions with rational coefficients.</li> <li>CCSS.7.EE.2. Understand that rewriting an expression in different forms in a problem context</li> </ul>	<ul> <li>ENDURING UNDERSTANDINGS</li> <li>Real world situations can be represented symbolically with expressions and equations.</li> <li>An equation is formed by two equivalent expressions.</li> <li>Equivalent equations represent the same value in unique forms.</li> </ul>	<ul> <li>ESSENTIAL QUESTIONS</li> <li>How do you compare algebraic solutions to arithmetic solutions?</li> <li>How do you translate real world problems to algebraic expressions?</li> <li>Does my answer make sense?</li> </ul>
can shed light on the problem and how the		isition
<ul> <li>quantities in it are related.</li> <li>CCSS.7.EE.3. Solve multi-step real-life and mathematical problems posed with positive and negative rational numbers in any form (whole numbers, fractions, and decimals), using tools strategically. Apply properties of operations to calculate with numbers in any form; convert between forms as appropriate; and assess the reasonableness of answers using mental computation and estimation strategies.</li> <li>CCSS.7.EE.4. Use variables to represent quantities in a real-world or mathematical problem, and</li> </ul>	<ul> <li>Students will understand</li> <li>difference between a constant and a coefficient, including coefficients of one.</li> <li>like terms are terms with the same variable.</li> <li>equivalent expressions have the same value.</li> <li>an algebraic equation may have a solution.</li> <li>an inequality states two values are not the same.</li> <li>commutative, associative, identity, distributive, and inverse properties.</li> <li>a monomial is a single term.</li> </ul>	<ul> <li>Students will be skilled at</li> <li>simplifying algebraic expressions with rational numbers.</li> <li>creating algebraic expressions from verbal expressions.</li> <li>defining a variable and creating an equation from a word problem.</li> <li>solving one-step equations with integers by balancing the equation.</li> <li>solving two-step equations by using equivalent equations.</li> <li>solving equations with variables on both sides of the equation.</li> </ul>

<ul> <li>construct simple equations and inequalities to solve problems by reasoning about the quantities.</li> <li>CCSS.MP1 Make sense of problems and persevere in solving them.</li> <li>CCSS.MP3 Construct viable arguments and critique the reasoning of others.</li> <li>CCSS.MP7 Look for and make use of structure.</li> </ul>	<ul> <li>graphing inequalities on a number line.</li> <li>creating and solving one-step inequalities.</li> <li>creating and solving two-step inequalities.</li> <li>rewriting expressions in a different form; example ½ of x = .5x = x/2</li> <li>solving problems with fractional coefficients.</li> <li>checking for the reasonableness of the solution.</li> <li>finding the Greatest Common Factor for monomials.</li> <li>factoring linear expressions using distributive property.</li> </ul>
Used in Content Area Standards	21 <sup>st</sup> Century Skills
	Critical Thinking
	Communication

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
	ASSESSMENT: Written Assessments or Projects	
	Other Evidence: independent practice, classroom observations and discussions	

# Windham School District Curriculum Accelerated Mathematics - Grade 7 Unit 4: Geometry - Transformations

Used in Content Area Standards	21 <sup>st</sup> Century Skills
	<ul><li>Technology Literacy</li><li>Critical thinking</li></ul>

Stage 2 - Evidence	
Evaluative Criteria	Assessment Evidence
	ASSESSMENT: Written Assessments or Projects
	OTHER EVIDENCE: independent practice, classroom observations and discussions

## Windham School District Curriculum Accelerated Mathematics - Grade 7 Unit 5: Geometry - Angles & Transversals

ESTABLISHED GOALS:	Stage 1 Desired Results	
	Transfer	
	Students will be able to independently use their lea	-
geometry. In this unit, students will gain a deeper understanding	<b>o o</b> .	
of angles, angle relationships, and transversals and will solve	<ul> <li>use vocabulary and properties in future studies</li> </ul>	of Geometry.
real-world problems involving geometric figures.	Meaning	1
	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS
Content Standards:	Analyzing geometric relationships develops	• Who needs to use angles and how do
<ul> <li>CCSS.7.G.5. Use facts about supplementary,</li> </ul>	reasoning and justification skills.	they use them?
complementary, vertical, and adjacent angles in a multi-step	• Angle relationships can be used to determine	What special relationships exist
problem to write and solve simple equations for an	missing angle measures in diagrams.	between angles and lines?
unknown angle in a figure.		<ul> <li>How many pairs of congruent angles</li> </ul>
• CCSS.8.G.1 Verify experimentally the properties of rotations,		are created when two parallel lines
reflections, and translations.		are cut by a transversal?
• CCSS.8.G.2 Understand that a two-dimensional figure is	Acquisitio	
	Students will understand	Students will be skilled at
the first by a sequence of rotations, reflections, and		
translations; given two congruent figures, describe a	• different angle pair relationships: adjacent,	• classifying angle pair relationships.
sequence that exhibits the congruence between them.	vertical, complementary, supplementary, and	• creating algebraic equations using
<ul> <li>CCSS.8.G.3 Describe the effect of dilations, translations,</li> </ul>	linear pair.	angle pair relationships.
	<ul> <li>congruent angles are angles with the same</li> </ul>	<ul> <li>finding angle measurements using</li> </ul>
rotations, and reflections on two-dimensional figures using coordinates.	measure.	properties of similar figures, exterior
	<ul> <li>intersecting lines are lines with one point in</li> </ul>	and interior angles, and parallel lines
• CCSS.8.G.4 Understand that a two-dimensional figure is	common.	cut by a transversal.
similar to another if the second can be obtained from the	<ul> <li>angle relationships between exterior and</li> </ul>	
first by a sequence of rotations, reflections, translations,	interior triangle angles, similar triangles, and	
and dilations; given two similar two-dimensional figures,	parallel lines cut by a transversal.	

	describe a sequence that exhibits the similarity between	
	them.	
٠	CCSS.8.G.5 Use informal arguments to establish facts about	
	the angle sum and exterior angle of triangles, about the	
	angles created when parallel lines are cut by a transversal,	
	and the angle-angle criterion for similarity of triangles.	
٠	CCSS.MP4 Model with mathematics.	
٠	CCSS.MP5 Use appropriate tools strategically.	
٠	CCSS.MP6 Attend to precision.	
Use	d in Content Area Standards	21 <sup>st</sup> Century Skills
		Technology Literacy

Stage 2 - Evidence	
Evaluative Criteria Assessment Evidence	
	ASSESSMENT: Written Assessments or Projects
	OTHER EVIDENCE: independent practice, classroom observations and discussions

# Windham School District Curriculum **Accelerated Mathematics - Grade 7 Unit 6: Geometry - The Pythagorean Theorem**

#### as 1 Desired Result

	Stage 1 Desired Results	
ESTABLISHED GOALS:	Trai	nsfer
Students will continue their study of mathematics in the	Students will be able to independently use their lea	rning to
area of geometry. In this unit, students will gain a	apply pythagorean theorem to future geometric	concepts
deeper understanding of the pythagorean theorem and	<ul> <li>use pythagorean theorem and its converse to sc</li> </ul>	olve real-world problems.
its converse.	Меа	ning
<ul> <li>Content Standards:</li> <li>CCSS.8.G.6. Explain a proof of the Pythagorean Theorem and its converse.</li> <li>CCSS.8.G.7. Apply the Pythagorean Theorem to determine unknown side lengths in right triangles</li> </ul>	<ul> <li>ENDURING UNDERSTANDINGS</li> <li>Right triangles have a special relationship among the side lengths which can be represented by a model and a formula.</li> </ul>	<ul> <li>ESSENTIAL QUESTIONS</li> <li>How can right triangle relationships model real world phenomena?</li> <li>How can you use the Pythagorean Theorem to solve everyday problems?</li> </ul>
	Students will understand	<b>isition</b> Students will be skilled at
• CCSS8.G.8. Apply the Pythagorean Theorem to find the distance between two points in a	• Pythagorean Theorem equates the sum of the squares of the legs to the square of the	<ul> <li>Informally proving the Pythagorean Theorem</li> <li>(a<sup>2</sup> + b<sup>2</sup> = c<sup>2</sup>)</li> </ul>
<ul><li>coordinate system.</li><li>CCSS.MP.2 Reason abstractly and quantitatively.</li></ul>	<ul> <li>hypotenuse.</li> <li>converse of the Pythagorean Theorem can be</li> </ul>	• Determining if a triangle is a right triangle using its converse.
<ul><li>CCSS.MP.4 Model with mathematics.</li><li>CCSS.MP.6 Attend to precision.</li></ul>	used to determine whether a given triangle is a right triangle.	<ul> <li>Applying the Pythagorean Theorem to find missing triangle side lengths.</li> </ul>
		<ul> <li>Applying the Pythagorean Theorem to solve problems</li> </ul>
Used in Content Area Standards 21 <sup>st</sup> Century Skills		21 <sup>st</sup> Century Skills
		Technology Literacy
		Critical Thinking

Stage 2 - Evidence	
Evaluative Criteria	Assessment Evidence
	ASSESSMENT: Written Assessments or Projects
	OTHER EVIDENCE: independent practice, classroom observations and discussions

# Windham School District Curriculum Accelerated Mathematics - Grade 7 Unit 7: Geometry: Volume

Stage 1 Desired Results		
ESTABLISHED GOALS:	Transfer	
Students will continue their study of mathematics in	Students will be able to independently use their learning t	to
the area of geometry. In this unit, students will gain	<ul> <li>solve real-world problems including the volume of cyli</li> </ul>	nders, cones and spheres.
a deeper understanding of the volume of	Meaning	1
three-dimensional figures; such as cylinders, cones	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS
and spheres.	• Everyday objects have a variety of attributes, each of	• Will the size of a container indicate its
	which can be measured in many ways.	contents?
Content Standards:	• Area, surface area and volume have applications in	<ul> <li>How will the volume change if one</li> </ul>
• CCSS.8.G.9. Know the formulas for the volumes	real world situations.	dimension is changed?
of cones, cylinders, and spheres and use them	• Different 3-dimensional figures can have the same	<ul> <li>How does understanding two-dimensional</li> </ul>
to solve real-world and mathematical problems	volume even if the dimensions are not all the same.	figures help find the volume of
CCSS.MP1 Make sense of problems and		three-dimensional figures?
persevere in solving them.	Acquisitio	n
CCSS.MP4 Model with mathematics.	Students will understand	Students will be skilled at
CCSS.MP6 Attend to precision	<ul> <li>volume of some solid figures is calculated using the</li> </ul>	• calculating volume of cones, cylinders, and
<ul> <li>CCSS.MP8 Look for and express regularity in second according</li> </ul>	area of the base and its height.	spheres using appropriate formulas and
repeated reasoning.	• connection between finding volume of one base vs.	units.
	two base figures.	<ul> <li>using volume formulas to solve real-world</li> </ul>
	• formulas for finding volume of cones, cylinders, and	problems.
	spheres.	
Used in Content Area Standards		21 <sup>st</sup> Century Skills
		Technology Literacy
		Critical Thinking

Stage 2 - Evidence	
Evaluative Criteria	Assessment Evidence
	ASSESSMENT: Written Assessments or Projects
	OTHER EVIDENCE: independent practice, classroom observations and discussions

### Windham School District Curriculum **Accelerated Mathematics - Grade 7 Unit 8: Statistics**

	Stage 1 Desired Results	
ESTABLISHED GOALS:	Trar	nsfer
Students will continue their study of mathematics in the area of	Students will be able to independently use thei	r learning to
data and problem solving. In this unit, students will gain a deeper	• analyze and interpret data from real-world	situations.
understanding of statistics, by analyzing and interpreting data	<ul> <li>understand when real-life data is misleadin</li> </ul>	g
from real-world problems.	Меа	ning
<ul> <li>CCSS.7.SP.1 Understand that statistics can be used to gain information about a population by examining a sample of the population; generalizations about a population from a sample are valid only if the sample is representative of that population. Understand that random sampling tends to produce representative samples and support valid</li> </ul>	<ul> <li>A statistical question anticipates variability in the data related to the question and accounts for it in the answers.</li> <li>A set of data collected to answer a</li> </ul>	<ul> <li>ESSENTIAL QUESTIONS</li> <li>How do you interpret data from statistical representations?</li> </ul>
inferences.	Acqui	sition
<ul> <li>inferences about a population with an unknown characteristic of interest. Generate multiple samples (or simulated samples) of the same size to gauge the variation in estimates or predictions.</li> <li>CCSS.7.SP.3. Informally assess the degree of visual overlap of two numerical data distributions with similar variabilities, measuring the difference between the centers by</li> </ul>	<ul> <li>measure of central tendency: mean, median, mode</li> <li>dispersion of data is the spread of data</li> <li>the less variation a set has the closer the numbers are to each other.</li> </ul>	<ul> <li>Students will be skilled at</li> <li>creating data with a specific mode, median and mean.</li> <li>identifying when a measure of central tendency would not be an accurate reflection of the data.</li> <li>using data from a random sample to draw inferences about a population.</li> <li>analyzing data to make a prediction.</li> <li>displaying two samples of data in a box plot to illustrate variability.</li> </ul>

٠	CCSS.7.SP.4. Use measures of center and measures of	• creating a line plot to compare two
	variability for numerical data from random samples to draw	samples.
	informal comparative inferences about two populations.	
•	CCSS.MP3 Construct viable arguments and critique the	
	reasoning of others.	
•	CCSS.MP4 Model with mathematics.	
•	CCSS.MP5 Use appropriate tools strategically.	
Used	l in Content Area Standards	21 <sup>st</sup> Century Skills
		Communication
		Critical Thinking

Stage 2 - Evidence	
Evaluative Criteria Assessment Evidence	
	ASSESSMENT: Written Assessments or Projects
	OTHER EVIDENCE: independent practice, classroom observations and discussions

## Windham School District Curriculum **Accelerated Mathematics - Grade 7 Unit 9: Probability**

Stage 1 Desired Results			
ESTABLISHED GOALS:	Transfer		
Students will continue their study of mathematics in the	Students will be able to independently use their lea	rning to	
area of data and problem solving. In this unit, students	• solve real-world problems involving chance.		
will gain a deeper understanding of probability to solve			
real-world problems involving chance.	Меа		
	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS	
Content Standards:	<ul> <li>Probability is used to predict the likelihood of</li> </ul>	<ul> <li>What makes a game fair?</li> </ul>	
• CCSS.7.SP.C.5 Understand that the probability of a	an event and make decisions.	<ul> <li>How are probabilities used to make everyday</li> </ul>	
chance event is a number between 0 and 1 that	<ul> <li>Key to valuable experimental probability is</li> </ul>	decisions?	
expresses the likelihood of the event occurring.	good data.		
Larger numbers indicate greater likelihood. A	Acqui	isition	
probability near 0 indicates an unlikely event, a	Students will understand	Students will be skilled at	
probability around 1/2 indicates an event that is	<ul> <li>probability is the likelihood that something</li> </ul>	<ul> <li>performing an activity, recording results and</li> </ul>	
neither unlikely nor likely, and a probability near 1	will happen.	calculating experimental probability.	
indicates a likely event.	<ul> <li>experimental probability is based on</li> </ul>	• comparing different experimental probabilities	
• CCSS.7.SP.C.6 Approximate the probability of a	someone's results.	for the same activity and explaining the	
chance event by collecting data on the chance	• theoretical probability is based on what exists.	difference.	
process that produces it and observing its long-run	<ul> <li>possible outcomes and favorable outcomes.</li> </ul>	<ul> <li>making predictions based on probability.</li> </ul>	
relative frequency, and predict the approximate	<ul> <li>equally likely outcomes are results that have</li> </ul>	<ul> <li>creating tree diagrams to find total possible</li> </ul>	
relative frequency given the probability.	the same probability of happening.	outcomes.	
CCSS.7.SP. C.7 Develop a probability model and use	<ul> <li>tree diagrams as a method for finding all</li> </ul>	<ul> <li>expressing probability as fractions and</li> </ul>	
it to find probabilities of events. Compare	possible outcomes.	percents.	
probabilities from a model to observed	<ul> <li>probability of an outcome ranges between 0</li> </ul>	<ul> <li>identifying an event that would have a</li> </ul>	
frequencies; if the agreement is not good, explain	(never happening) and 1 (always happening).	probability of zero.	
possible sources of the discrepancy.	<ul> <li>compound probability is used when more than</li> </ul>	<ul> <li>identifying an event that would have a</li> </ul>	
	one event is happening.	probability of one.	

<ul> <li>CCSS.7.SP.C.8 Find probabilities of compound events using organized lists, tables, tree diagrams, and simulation.</li> <li>CCSS.MP2 Reason abstractly and quantitatively.</li> <li>CCSS.MP4 Model with mathematics.</li> </ul>	<ul> <li>probability is either independent or dependent.</li> </ul>	<ul> <li>calculating compound probability of both dependent and independent events.</li> </ul>
Used in Content Area Standards		21 <sup>st</sup> Century Skills
		Communication
		Critical Thinking

Stage 2 - Evidence		
Evaluative Criteria	Assessment Evidence	
ASSESSMENT: Written Assessments or Projects		
OTHER EVIDENCE: independent practice, classroom observations and discussions		

#### Title of Curriculum: 8th Grade Math

Unit Name	What (content, vocab)	Why (enduring understandings)	How (skills)
Unit 1: Numbers & Operations: The Real Number System	<ul> <li>Rational numbers</li> <li>Irrational numbers</li> <li>Radicals (square and cube roots)</li> <li>Exponents</li> <li>Scientific notation</li> <li>Compare real numbers</li> </ul>	<ul> <li>Real numbers include rational and irrational numbers which can be approximated using rational numbers.</li> <li>Real numbers can be represented using mathematical symbols.</li> </ul>	<ul><li>irrational or rational</li><li>Approximate rational numbers</li><li>Compare and order rational and</li></ul>
Unit 2: Algebraic Thinking: Solving Equations	<ul> <li>Equivalent expressions</li> <li>Equations</li> <li>Inverse operations</li> <li>Rational number coefficients</li> </ul>	<ul> <li>Mathematical properties and inverse operations can be applied to efficiently solve equations and interpret solutions.</li> </ul>	<ul> <li>Solve two-step equations, with integers using inverse operations</li> <li>Solve multi-step equations with variables on both sides</li> <li>Simplify expressions</li> <li>Solve equations with rational number coefficients</li> <li>Apply mathematics to problem solving situations</li> </ul>
Unit 3: Algebraic Thinking: Linear Functions	<ul> <li>Linear and nonlinear functions</li> <li>Slope</li> <li>y-intercept</li> <li>Proportional relationships</li> <li>Tables, graphs, equations</li> </ul>	<ul> <li>Proportional relationships can be represented as a linear equation that passes through the origin.</li> <li>Linear relationships can be represented using tables, graphs and equations.</li> <li>Linear functions model relationships between quantities.</li> </ul>	<ul> <li>nonlinear</li> <li>Write and interpret linear equations in slope intercept (y=mx+b) form</li> <li>Analyze and translate information for linear relationships between tables, graphs and equations</li> </ul>

			<ul> <li>Find and interpret the initial value (y-intercept, b) using table, graph, and equation</li> <li>Represent and compare proportional relationships from different representations</li> </ul>
Unit 4: Algebraic Thinking: Linear Systems	<ul> <li>Graphs of Linear systems</li> <li>Solutions (intersection point, infinite, none)</li> </ul>	<ul> <li>Solutions to linear systems can be used to represent real world phenomena.</li> </ul>	<ul> <li>Solve linear systems using graphing methods</li> <li>Determine whether lines will be parallel or intersecting</li> <li>Interpret the solution to a linear system in real world situations</li> </ul>
Unit 5: Algebraic Thinking: Bivariate Data	<ul> <li>Scatterplots</li> <li>Association (Correlation)</li> <li>Best fit line</li> <li>Qualitative graphs and descriptions</li> </ul>	<ul> <li>Bivariate data can be graphed to show correlation.</li> <li>Linear data can be modeled with an equation to answer questions and make predictions</li> <li>Functions can model relationships between quantities.</li> </ul>	<ul> <li>Construct and interpret scatter plots to investigate patterns of association between two quantities</li> <li>Describe patterns of association for two quantities. (positive, negative, no association)</li> <li>Create and use lines of best fit to make and evaluate predictions</li> <li>Interpret the relationships between two variables on qualitative graphs</li> </ul>
Unit 6: Geometry: Transformations	<ul> <li>Transformations: dilations, translations, reflections, rotations</li> <li>Congruence</li> <li>Similarity</li> </ul>	<ul> <li>Transformations can result in congruent or similar figures.</li> </ul>	<ul> <li>Transform polygons using dilations, translations, reflections, and rotations</li> <li>Identify coordinates of transformed figures</li> <li>Describe sequence of transformations that result in congruent or similar figures</li> </ul>
Unit 7: Geometry: Angles	<ul> <li>Triangle angle relationships</li> <li>Angles formed by parallel lines cut by a transversal</li> <li>Interior and exterior angles</li> </ul>	<ul> <li>Special angle relationships are formed by triangles and parallel lines cut by a transversal.</li> <li>Angle relationships can be used to determine missing angle measures in diagrams.</li> </ul>	<ul> <li>Find angle measurements using properties of similar figures, exterior and interior angles, and parallel lines cut by a transversal</li> </ul>

Unit 8: Geometry: Pythagorean Theorem	<ul> <li>Pythagorean Theorem</li> <li>Converse of the Pythagorean Theorem</li> <li>Squares and square roots</li> <li>Distance on the coordinate plane</li> </ul>	<ul> <li>Right triangles have a special relationship among the side lengths which can be represented by a model and a formula.</li> </ul>	<ul> <li>Informally prove the Pythagorean Theorem</li> <li>Determine if a triangle is a right triangle using its converse</li> <li>Apply the Pythagorean Theorem to find missing triangle side lengths</li> <li>Apply the Pythagorean Theorem to solve problems</li> <li>Apply the Pythagorean Theorem to find distance between two points on the coordinate plane</li> </ul>
Unit 9: Geometry: Volume	<ul> <li>Volume and Surface area of right prisms and pyramids</li> <li>Nets</li> <li>Volume of Cylinder, Cones and Spheres</li> </ul>	<ul> <li>Everyday objects have a variety of attributes, each of which can be measured in many ways.</li> <li>Area, surface area and volume have applications in real world situations.</li> <li>Different 3-dimensional figures can have the same volume even if the dimensions are not all the same.</li> </ul>	<ul> <li>and pyramids using appropriate formulas and units</li> <li>Calculate surface area of triangular prisms and pyramids</li> <li>Calculate volumes of cones, cylinders, and spheres using appropriate formulas</li> </ul>

#### **Unit 1: Numbers & Operations - The Real Number System**

#### Stage 1 Desired Results

ESTABLISHED GOALS:	Transfel	r
Students will continue their study of mathematics in the area of the	Students will be able to independently use their le	earning to
real number system. In this unit, students will gain a deeper	understand the different types of numbers wit	thin the real number systems
understanding of rational and irrational numbers.	<ul> <li>connect those understandings to numbers the</li> </ul>	ey see in their daily life.
<ul> <li>understanding of rational and irrational numbers.</li> <li>Content Standards: <ul> <li>CCSS.8.NS.1. Know that numbers that are not rational are called irrational. Understand informally that every number has a decimal expansion; for rational numbers show that the decimal expansion repeats eventually, and convert a decimal expansion that repeats eventually into a rational number.</li> <li>CCSS.8.NS.2. Use rational approximations of irrational numbers to compare the size of irrational numbers, locate them approximately on a number line diagram, and estimate the value of expressions (e.g., π2)</li> <li>CCSS.8.EE.1. Know and apply the properties of integer exponents to generate equivalent numerical expressions.</li> <li>CCSS.8.EE.2. Use square root and cube root symbols to represent solutions to equations of the form x 2 = p and x 3 = p, where p is a positive rational number.</li> </ul> </li> </ul>	<ul> <li>connect those understandings to numbers the Meaning</li> <li>ENDURING UNDERSTANDINGS</li> <li>Real numbers include rational and irrational numbers which can be approximated using rational numbers.</li> <li>Real numbers can be represented using mathematical symbols.</li> <li>Acquisitie</li> <li>Students will understand</li> <li>real numbers are made up of rational and irrational numbers</li> <li>different subsets of the real number system are comparable.</li> <li>finding perfect square roots help to estimate the values of square roots that are not</li> </ul>	ey see in their daily life. g ESSENTIAL QUESTIONS • When are numbers exact? • How can mathematics make really large or really small numbers understandable?
<ul> <li>of small perfect squares and cube roots of small perfect cubes. Know that V2 is irrational.</li> <li>CCSS.8.EE.3. Use numbers expressed in the form of a single digit times a whole-number power of 10 to estimate very large or very small quantities.</li> <li>CCSS.MP2 Reason abstractly and quantitatively.</li> </ul>	<ul> <li>radical symbols indicate square or cube roots.</li> <li>equivalent expressions can be written using integer exponents.</li> </ul>	

<ul> <li>CCSS.MP3 Construct viable arguments and critique the reasoning of others.</li> <li>CCSS.MP6 Attend to precision.</li> <li>CCSS.MP7 Look for and make use of structure.</li> <li>CCSS.MP8 Look for and express regularity in repeated reasoning.</li> </ul>	
Used in Content Area Standards	21 <sup>st</sup> Century Skills
	<ul><li>Communication</li><li>Technology Literacy</li></ul>

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
OTHER EVIDENCE: independent practice, classroom observations and discussions		

#### **Unit 2: Algebraic Thinking - Solving Equations**

	Stage 1 Desired Results	
ESTABLISHED GOALS:		Transfer
Students will continue their study of	Students will be able to independently use their lear	ning to
mathematics in the area of algebraic thinking.	<ul> <li>understand how mathematical operations are inv</li> </ul>	versely connected
In this unit, students will gain a deeper	<ul> <li>use equations to solve real world problems.</li> </ul>	
understanding of solving equations.		Meaning
	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS
Content Standards:	Mathematical properties and inverse operations	• Are all things created equal?
CCSS.8.EE.7. Solve linear equations in	can be applied to efficiently solve equations and	<ul> <li>What situations can be modeled using equations?</li> </ul>
one variable.	interpret solutions.	• How can two equations look different but be the same?
CCSS.MP2 Reason abstractly and	Acquisition	
quantitatively.	Students will understand	Students will be skilled at
CCSS.MP3 Construct viable arguments	<ul> <li>an equation involves inverse operations and</li> </ul>	<ul> <li>solving two-step equations with integers using inverse</li> </ul>
and critique the reasoning of others.	maintaining balance.	operations.
CCSS.MP4 Model with mathematics.	<ul> <li>equivalent expressions are created by</li> </ul>	• solving multi-step equations with variables on both sides.
CCSS.MP7 Look for and make use of	properties of mathematics.	<ul> <li>simplifying expressions</li> </ul>
structure.	<ul> <li>rational number coefficients</li> </ul>	<ul> <li>solving equations with rational number coefficients.</li> </ul>
		<ul> <li>applying mathematics to problem solving situations.</li> </ul>
Used in Content Area Standards		21 <sup>st</sup> Century Skills
		Critical Thinking
		Communication

Stage 2 - Evidence		
Evaluative Criteria	Assessment Evidence	
ASSESSMENT: Written Assessments or Projects		
OTHER EVIDENCE: independent practice, classroom observations and discussions		

#### **Unit 3: Algebraic Thinking - Linear Functions**

Stage 1 Desired Results	
Transfer	
Students will be able to independently use their lea	rning to
<ul> <li>model real world situations using graphs, tables,</li> </ul>	, and equations.
<ul> <li>connect linear functions to future algebraic functions</li> </ul>	ction understandings.
Меа	ning
<ul> <li>Proportional relationships can be represented as a linear equation that passes through the origin.</li> <li>Linear relationships can be represented using tables, graphs and equations.</li> <li>Linear functions model relationships between</li> </ul>	<ul> <li>ESSENTIAL QUESTIONS</li> <li>How can functions represent real world phenomena?</li> <li>When do two variables represent a linear relationship?</li> </ul>
-	<ul> <li>Students will be skilled at</li> <li>determining if a relationship is linear or nonlinear.</li> <li>writing and interpreting linear equations in slope intercept (y = mx + b) form.</li> <li>analyzing and translating information for linear relationships between tables, graphs and equations.</li> <li>finding and interpreting the rate of change (slope, m) using tables, graphs, and equations.</li> </ul>
	<ul> <li>Tran</li> <li>Students will be able to independently use their lea</li> <li>model real world situations using graphs, tables</li> <li>connect linear functions to future algebraic functions</li> <li>Connect linear functions to future algebraic functions</li> <li>Proportional relationships can be represented as a linear equation that passes through the origin.</li> <li>Linear relationships can be represented using tables, graphs and equations.</li> <li>Linear functions model relationships between quantities.</li> <li>Students will understand</li> <li>linear and nonlinear functions can be shown using different representations.</li> <li>proportional and nonproportional relationships.</li> <li>connections between verbal descriptions and graphical representations of linear functions.</li> </ul>

<ul> <li>CCSS.8.F.3. Interpret the equation y = mx + b as a defining a linear function, whose graph is a straight line; give examples of functions that are not linear.</li> <li>CCSS.8.F.4. Construct a function to model a linear relationship between two quantities. Determine the rate of change and initial value of the function from a description of a relationship or from two (x, y) values, including reading these from a table or from a graph. Interpret the rate of change and initial value of the situation it models, and in terms of its graph or a table of values.</li> <li>CCSS.MP1 Make sense of problems and persevere in solving them.</li> <li>CCSS.MP3 Construct viable arguments and critique the reasoning of others.</li> <li>CCSS.MP4 Model with mathematics.</li> <li>CCSS.MP7 Look for and make use of structure.</li> <li>CCSS.MP8 Look for and express regularity in repeated reasoning</li> </ul>	<ul> <li>finding and interpreting the initial value (y-intercept, b) using tables, graphs, and equations.</li> <li>representing and comparing proportional relationships from different representations.</li> </ul>
Used in Content Area Standards	21 <sup>st</sup> Century Skills
	<ul> <li>Technology Literacy</li> <li>Critical Thinking</li> </ul>

Stage 2 - Evidence			
Evaluative Criteria Assessment Evidence			
ASSESSMENT: Written Assessments or Projects			
Other Evidence: independent practice, classroom observations and discussions			

#### **Unit: Algebraic Thinking - Linear Systems**

	Stage 1 Desired Results		
ESTABLISHED GOALS:	Transfer		
Students will continue their study of mathematics in the	Students will be able to independently use their le	earning to	
area of algebraic thinking. In this unit, students will gain	model multiple linear relationships and interpretered	et their intersection point.	
a deeper understanding of the relationships between	Ме	aning	
different linear scenarios.	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS	
	• Solutions to linear systems can be used to	• What can happen when you have two lines?	
Content Standards:	represent real world phenomena.	How does the intersection of a linear system	
<ul> <li>CCSS.8.EE.8. Analyze and solve pairs of</li> </ul>		model real world phenomena?	
simultaneous linear equations.	Acquisition		
CCSS.MP1 Make sense of problems and persevere	Students will understand	Students will be skilled at	
in solving them.	<ul> <li>lines may or may not intersect.</li> </ul>	• solving linear systems using graphing methods.	
CCSS.MP4 Model with mathematics.	<ul> <li>graphs of Linear systems</li> </ul>	<ul> <li>determining whether lines will be parallel or</li> </ul>	
CCSS.MP5 Use appropriate tools strategically	<ul> <li>solutions (intersection point, infinite, none)</li> </ul>	intersecting.	
		• interpreting the solution to a linear system in	
		real world situations.	
Used in Content Area Standards		21 <sup>st</sup> Century Skills	
		Technology Literacy	
		Critical thinking	

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
	OTHER EVIDENCE: independent practice, classroom observations and discussions	

#### **Unit 5: Algebraic Thinking - Bivariate Data**

	Stage 1 Desired Results	
ESTABLISHED GOALS:	Tra	nsfer
Students will continue their study of mathematics in the area of	Students will be able to independently use the	eir learning to
algebraic thinking. In this unit, students will gain a deeper	• interpret and model data using scatterplot	ts.
understanding of how data can be represented using scatterplots.	Мес	aning
<ul> <li>Content Standards:</li> <li>CCSS.8.SP.1. Construct and interpret scatter plots for bivariate measurement data to investigate patterns of association between two quantities. Describe patterns such as clustering, outliers, positive or negative association, linear association, and nonlinear association. CCSS.8.SP.2. Know that straight lines are widely used to model relationships between two</li> </ul>	<ul> <li>Linear data can be modeled with an equation to answer questions and make predictions</li> <li>Functions can model relationships between quantities.</li> </ul>	<ul> <li>ESSENTIAL QUESTIONS</li> <li>How can mathematics be used to model and make predictions for real world phenomena?</li> </ul>
quantitative variables. For scatter plots that suggest a linear	Acqu	isition
<ul> <li>association, informally fit a straight line, and informally assess the model fit by judging the closeness of the data points to the line.</li> <li>CCSS.8.SP.3. Use the equation of a linear model to solve problems in the context of bivariate measurement of data, interpreting the slope and interpret.</li> <li>CCSS.8.SP.4. Understand that patterns of association can also be seen in bivariate categorical data by displaying frequencies and relative frequencies in a two-way table. Construct and interpret a two-way table summarizing data on two categorical variables collected from the same subjects. Use relative frequencies calculated for rows or columns to describe possible association between the two variables.</li> </ul>	<ul> <li>scatter plots show relationships between two variables.</li> <li>some data can be modeled using a linear equation.</li> <li>linear models can be used to make predictions about data.</li> </ul>	<ul> <li>Students will be skilled at</li> <li>constructing and interpreting scatter plots to investigate patterns of association between two quantities.</li> <li>describing patterns of association for two quantities.</li> <li>creating and using lines of best fit to make and evaluate predictions.</li> <li>interpreting the relationships between two variables on qualitative graphs</li> </ul>

•	CCSS.MP 3 Construct viable arguments and critique the		
	reasoning of others.		
•	CCSS.MP 4 Model with mathematics.		
Use	ed in Content Area Standards		21 <sup>st</sup> Century Skills
		•	Communication
		•	Technology Literacy

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
OTHER EVIDENCE: independent practice, classroom observations and discussions		

## Windham School District Curriculum Mathematics - Grade 8 Unit 6: Geometry - Transformations

Stage	1 Desired Results	
ESTABLISHED GOALS:		Transfer
Students will continue their study of mathematics in the area of geometry.	Students will be able to independently	y use their learning to
In this unit, students will gain a deeper understanding of congruence and	determine if figures are congruen	t or similar using the coordinate plane.
similarity on the coordinate plane.		Meaning
<ul> <li>Content Standards:</li> <li>CCSS.8.G.1. Verify experimentally the properties of rotations, reflections, and translations.</li> <li>CCSS.8.G.2. Understand that a two-dimensional figure is congruent to</li> </ul>	<ul> <li>ENDURING UNDERSTANDINGS</li> <li>Transformations can result in congruent or similar figures.</li> </ul>	<ul> <li>ESSENTIAL QUESTIONS</li> <li>What movements preserve or change shapes?</li> <li>How can a house fit on a piece of paper?</li> </ul>
<ul> <li>another if the second can be obtained from the first by a sequence of rotations, reflections, and translations; given two congruent figures, describe a sequence that exhibits the congruence between them.</li> <li>CCSS.8.G.3. Describe the effect of dilations, translations, rotations, and reflections on two-dimensional figures using coordinates.</li> <li>CCSS.8.G.4. Understand that a two-dimensional figure is similar to another if the second can be obtained from the first by a sequence of rotations, reflections, translations, and dilations; given two similar two-dimensional figures, describe a sequence that exhibits the similarity between them</li> <li>CCSS.MP1 Make sense of problems and persevere in solving them.</li> <li>CCSS.MP7 Look for and make use of structure.</li> </ul>	<ul> <li>transformations as dilations, translations, reflections, and rotations</li> <li>transformations preserve congruence of polygons, lines,</li> </ul>	<ul> <li>Students will be skilled at</li> <li>transforming polygons using dilations, translations, reflections, and rotations.</li> <li>identifying coordinates of transformed figures.</li> <li>describing sequences of transformations that result in congruent or similar figures.</li> </ul>
Used in Content Area Standards	•	21 <sup>st</sup> Century Skills
		Critical Thinking

Stage 2 - Evidence			
Evaluative Criteria Assessment Evidence			
ASSESSMENT: Written Assessments or Projects			
OTHER EVIDENCE: independent practice, classroom observations and discussions			

# Windham School District Curriculum Mathematics - Grade 8 Unit 7: Geometry - Angles

#### **Stage 1 Desired Results**

	Stage I Desired Results		
ESTABLISHED GOALS:	Transfer		
Students will continue their study of mathematics in the	Students will be able to independently use their lea	irning to	
area of geometry. In this unit, students will gain a	• use angle relationships in more advanced study of Geometry.		
deeper understanding of angle relationships.	<ul> <li>use the relationships between angles and lines to solve real life problems.</li> </ul>		
	Med	aning	
Content Standards:	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS	
• CCSS.8.G.5. Use informal arguments to establish facts about the angle sum and exterior angle of triangles, about the angles created when parallel lines are cut by a transversal, and the angle-angle	<ul> <li>Special angle relationships are formed by triangles and parallel lines cut by a transversal.</li> <li>Angle relationships can be used to determine missing angle measures in diagrams.</li> </ul>	<ul> <li>How do intersecting lines create angle relationships?</li> </ul>	
criterion for similarity of triangles.	Acquisition		
<ul> <li>CCSS.MP1 Make sense of problems and persevere in solving them.</li> <li>CCSS.MP6 Attend to precision</li> <li>CCSS.MP7 Look for and make use of structure.</li> </ul>	<ul> <li>Students will understand</li> <li>angle relationships between exterior and interior triangle angles, similar triangles, and parallel lines cut by a transversal.</li> </ul>	<ul> <li>Students will be skilled at</li> <li>finding angle measurements using properties of similar figures, exterior angles, interior angles, and parallel lines cut by a transversal.</li> </ul>	
Used in Content Area Standards		21 <sup>st</sup> Century Skills	
		<ul><li>Critical thinking</li><li>Communication</li></ul>	

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
OTHER EVIDENCE: independent practice, classroom observations and discussions		

#### **Unit 8: Geometry - Pythagorean Theorem**

	Stage 1 Desired Results		
ESTABLISHED GOALS:	Transfer		
Students will continue their study of mathematics in the Students will be able to independently use their learning to			
area of geometry . In this unit, students will gain a	apply pythagorean theorem to future geometric concepts		
deeper understanding of problem solving using the	• use pythagorean theorem and its converse	e to solve real-world problems.	
Pythagorean Theorem.		Meaning	
<ul> <li>Content Standards:</li> <li>CCSS.8.G.6. Explain a proof of the Pythagorean Theorem and its converse.</li> <li>CCSS.8.G.7. Apply the Pythagorean Theorem to</li> </ul>	<ul> <li>ENDURING UNDERSTANDINGS</li> <li>Right triangles have a special relationship among the side lengths which can be represented by a model and a formula.</li> </ul>	<ul> <li>ESSENTIAL QUESTIONS</li> <li>How can right triangle relationships model real world phenomena?</li> <li>How can you use the Pythagorean Theorem to solve everyday problems?</li> </ul>	
determine unknown side lengths in right triangles		Acquisition	
<ul> <li>in real-world and mathematical problems in two and three dimensions.</li> <li>CCSS.8.G.8. Apply the Pythagorean Theorem to find the distance between two points in a coordinate system.</li> <li>CCSS.MP2 Reason abstractly and quantitatively.</li> <li>CCSS.MP4 Model with mathematics.</li> <li>CCSS.MP6 Attend to precision.</li> </ul>	<ul> <li>Students will understand</li> <li>Pythagorean Theorem equates the sum of the squares of the legs to the square of the hypotenuse in right triangles.</li> <li>converse of the Pythagorean Theorem can be used to determine whether a given triangle is a right triangle.</li> </ul>	<ul> <li>Students will be skilled at</li> <li>informally proving the Pythagorean Theorem (a<sup>2</sup> + b<sup>2</sup> = c<sup>2</sup>).</li> <li>determining if a triangle is a right triangle using its converse.</li> <li>applying the Pythagorean Theorem to find missing triangle side lengths.</li> <li>applying the Pythagorean Theorem to solve problems.</li> <li>applying the Pythagorean Theorem to find distance between two points on the coordinate plane.</li> </ul>	
Used in Content Area Standards		21 <sup>st</sup> Century Skills	
		<ul><li>Critical Thinking</li><li>Communication</li></ul>	

Stage 2 - Evidence		
Evaluative Criteria	Assessment Evidence	
	ASSESSMENT: Written Assessments or Projects	
	OTHER EVIDENCE: independent practice, classroom observations and discussions	

## Windham School District Curriculum Mathematics - Grade 8 Unit 9: Geometry - Volume

	Stage 1 Desired Results	
ESTABLISHED GOALS:	Transf	er
Students will continue their study of mathematics	Students will be able to independently use their learning	to
in the area of geometry. In this unit, students will	<ul> <li>solve real world problems involving volume and surface</li> </ul>	ice area.
gain a deeper understanding of solving real world	Meanii	ng
problems involving geometric solids.	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS
<ul> <li>Content Standards:</li> <li>CCSS.7.G.6. Solve real-world and mathematical problems involving area, volume and surface area of two- and three dimensional objects composed of triangles, quadrilaterals, polygons, cubes, and right</li> </ul>	<ul> <li>Everyday objects have a variety of attributes, each of which can be measured in many ways.</li> <li>Area, surface area and volume have applications in real world situations.</li> <li>Different 3-dimensional figures can have the same volume even if the dimensions are not all the same.</li> </ul>	<ul> <li>Will the size of a container indicate its contents?</li> <li>How will the volume change if one dimension is changed?</li> <li>How does understanding two-dimensional figures help find the volume of three-dimensional figures?</li> </ul>
prisms.	Acquisit	ion
<ul> <li>CCSS.8.G.9. Know the formulas for the volumes of cones, cylinders, and spheres and use them to solve real-world and mathematical problems.</li> <li>CCSS.MP1 Make sense of problems and persevere in solving them.</li> <li>CCSS.MP4 Model with mathematics.</li> <li>CCSS.MP6 Attend to precision</li> <li>CCSS.MP8 Look for and express regularity in repeated reasoning.</li> </ul>	<ul> <li>Students will understand</li> <li>volume of some solid figures is calculated using the area of the base and its height.</li> <li>connection between finding volume of one base vs. two base figures.</li> <li>formulas for finding volume of cones, cylinders, and spheres.</li> <li>a net is a two-dimensional drawing of a three-dimensional figure.</li> <li>characteristics of right prisms and pyramids.</li> </ul>	<ul> <li>Students will be skilled at</li> <li>calculating volume of triangular prisms and pyramids using appropriate formulas and units.</li> <li>calculating surface area of triangular prisms and pyramids.</li> <li>calculating volumes of cones, cylinders, and spheres using appropriate formulas and units</li> <li>using volume formulas to solve real world problems.</li> <li>drawing nets of solid figures.</li> </ul>

	• surface area is the sum of the areas of the faces and bases in a three dimensional figure.	
Used in Content Area Standards		21 <sup>st</sup> Century Skills
		Critical Thinking
		Communication

Stage 2 - Evidence		
Evaluative Criteria	Assessment Evidence	
	ASSESSMENT: Written Assessments or Projects	
	OTHER EVIDENCE: independent practice, classroom observations and discussions	

Title of Curriculum: 8th grade Algebra 1

Unit Name	What (content, vocab)	Why (enduring understandings)	How (skills)
Unit 1: Algebraic Expressions and Functions: Foundations of Functions and Expressions	<ul> <li>Functions</li> <li>Representations of relations</li> <li>Function notation</li> <li>Translations between verbal and algebraic expressions</li> <li>Mathematical properties</li> <li>Order of operations</li> <li>Domain and range of functions</li> </ul>	<ul> <li>Relations and functions can represent real world phenomena</li> <li>Variables represent unknown numbers or values that can change</li> </ul>	<ul> <li>Translate between verbal and algebraic expressions</li> <li>Perform order of operations</li> <li>Determine whether a relation is a function</li> <li>Evaluate a function in function notation</li> <li>Apply mathematical properties to simplify expressions</li> <li>Recognize and evaluate functions</li> <li>Identify and use the algebraic properties</li> <li>Write function rules from tables and word problems</li> <li>Determine domain and range of various functions</li> </ul>
Unit 2: Algebraic Expressions and Functions: Exponential Expressions and Functions	<ul> <li>Properties of exponents</li> <li>Scientific notation</li> <li>Geometry applications</li> <li>Exponential Functions</li> </ul>	<ul> <li>Very large and small numbers can be represented efficiently using scientific notation</li> <li>Exponent properties can be proven through expansion</li> <li>Exponential functions model real world phenomena.</li> </ul>	<ul> <li>Use the rules of exponents to simplify monomials</li> <li>Apply geometric formulas to problems involving monomials</li> <li>Write large or small numbers in scientific notation</li> <li>Perform operations on numbers expressed in scientific notation</li> <li>Graph exponential functions</li> </ul>
Unit 3: Algebraic Equations: Solving Equations and Inequalities	<ul> <li>Literal and algebraic equations</li> <li>Absolute value</li> <li>Percents</li> <li>Proportions</li> <li>Inequalities</li> <li>Compound inequalities</li> <li>Absolute value inequalities</li> </ul>	<ul> <li>Operations performed on one side of an equation must be performed on the other side(s) in order to preserve the equality.</li> <li>Solutions to inequalities represent a range of values rather than a single value.</li> </ul>	Write and solve multi-step equations with rational coefficients

Unit 4: Functions: Linear Relationships	<ul> <li>Slope</li> <li>Forms of linear equations</li> <li>Arithmetic sequences</li> <li>Direct variation</li> <li>Linear representations</li> <li>Parallel and perpendicular</li> </ul>	<ul> <li>Linear relationships have a constant rate of change.</li> <li>Tables, graphs, and equations are all ways of representing functions and real world phenomena.</li> </ul>	<ul> <li>Solve literal equations</li> <li>Write and solve proportions, including with binomials in numerator and denominator</li> <li>Write and Solve application percent problems</li> <li>Solve absolute value inequalities</li> <li>Calculate slope between two points</li> <li>Determine the slope of a line, given an equation, table, or graph</li> <li>Find and determine intercepts</li> <li>Graph linear equations</li> <li>Determine whether lines are parallel, provide the properties</li> </ul>
	<ul> <li>lines</li> <li>Properties of horizontal and vertical lines</li> </ul>	<ul> <li>Slope can be referenced in many different ways.</li> </ul>	<ul> <li>perpendicular, or neither</li> <li>Write linear equations in slope-intercept, standard and point-slope form</li> <li>Create and interpret linear equations from real world data</li> <li>Write a rule given an arithmetic sequence</li> </ul>
Unit 5: Functions: Bivariate Data (Scatterplots)	<ul> <li>Scatterplots</li> <li>Line of best fit</li> <li>Correlation</li> </ul>	<ul> <li>Scatter plots can model data, and be used to make predictions</li> </ul>	<ul> <li>Represent bivariate data with scatterplots</li> <li>Interpret scatterplots</li> <li>Calculate the line of best fit</li> <li>Use the line of best fit to find starting point represented by the y-intercept; to describe what the slope means; and to fin the values at a particular point including outside the given graph</li> <li>Determine if there is a correlation between bivariate data</li> <li>Make predictions based on the line of best fit</li> </ul>
Unit 6: Algebraic Equations: Linear Systems	<ul><li>Systems of equations</li><li>Systems of inequalities</li><li>Linear inequalities</li></ul>	<ul> <li>There is more than one way to solve a system of equations and students should</li> </ul>	<ul> <li>Write and solve linear systems using multiple methods</li> <li>Distinguish if a system of equations has</li> </ul>

		<ul> <li>determine the most efficient method.</li> <li>Systems of equations with two unknowns can be used to solve real world problems.</li> </ul>	<ul> <li>one solution, no solution, or infinitely many solutions</li> <li>Graph linear inequalities on a coordinate plane</li> <li>Graph systems of linear inequalities on a coordinate plane</li> <li>Create and interpret linear inequalities</li> <li>Model real world situations with systems of equations</li> </ul>
Unit 7: Algebraic Expressions and Equations: Polynomials and Quadratics	<ul> <li>Standard form and degree</li> <li>Operations with polynomials</li> <li>Factoring polynomials</li> <li>Quadratic equations</li> <li>Geometry applications</li> </ul>	<ul> <li>Mathematical properties extend to simplify polynomials.</li> </ul>	<ul> <li>Simplify polynomial expressions</li> <li>Solve quadratic equations by factoring</li> <li>Solve geometric problems involving polynomials</li> <li>Factor quadratics (leading coefficient is 1)</li> <li>Factor polynomials</li> </ul>
Unit 8: Algebraic Expressions and Equations: Radical Expressions and Equations	<ul> <li>Operations with radicals</li> <li>Pythagorean theorem</li> <li>Representations of radicals</li> <li>Radical Equations</li> <li>Extraneous solutions</li> </ul>	<ul> <li>Radicals represent numbers.</li> <li>In some operations, radicals mimic variables.</li> </ul>	<ul> <li>Simplify radicals</li> <li>Add, subtract, multiply, and divide radicals</li> <li>Solve problems involving the Pythagorean theorem</li> <li>Solve radical equations</li> <li>Determine extraneous solutions when solving radical equations</li> </ul>

# Windham School District Curriculum Algebra 1 - Grade 8 Unit 1: Algebraic Expressions & Function Foundations of Functions and Expressions

St	age 1 Desired Results	
ESTABLISHED GOALS:	Trans	fer
Students will continue their study of mathematics in the areas of	Students will be able to independently use thei	r learning to
algebraic expressions and functions. In this unit, students will gain a	• connect basic knowledge of functions in the	e study of advanced functions.
deeper understanding of function foundations for algebra.	Mean	ing
<ul> <li>Content Standards:</li> <li>CCSS.HSF.IF.A.1: Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If f is a function and x is an element of its domain, then f(x) denotes the output of f corresponding to the input x. The graph</li> </ul>	<ul> <li>Relations and functions can represent real world phenomena.</li> <li>Variables represent unknown numbers or values that can change.</li> </ul>	<ul> <li>ESSENTIAL QUESTIONS</li> <li>How can relations and functions relate to real world problems?</li> <li>How do you use variables, expressions, and equations to model real world problems?</li> </ul>
of f is the graph of the equation $y = f(x)$ .	Acquisi	ition
<ul> <li>CCSS.HSF.IF.A.2: Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context.</li> <li>CCSS.HSF.IF.B.6: Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph.</li> <li>CCSS.HSF.IF.C.8: Write a function defined by an expression in different but equivalent forms to reveal and explain different properties of the function.</li> <li>CCSS.HSF.IF.B.5: Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes.</li> </ul>	<ul> <li>verbal and algebraic expressions.</li> <li>order of operations.</li> <li>that mathematical properties simplify</li> </ul>	<ul> <li>Students will be skilled at</li> <li>translating between verbal and algebraic expressions.</li> <li>performing order of operations.</li> <li>determining whether a relation is a function.</li> <li>evaluating a function in function notation.</li> <li>applying mathematical properties to simplify expressions.</li> <li>recognizing and evaluating functions.</li> </ul>

<ul> <li>CCSS.HSF.BF.A.1: Write a function that describes a relationship between two quantities.</li> <li>CCSS.HSA.SSE.A.1: Interpret expressions that represent a quantity in terms of its context.</li> <li>CCSS.HSA.SSE.A.1.A: Interpret parts of an expression, such as terms, factors, and coefficients.</li> <li>CCSS.HSA.SSE.A.2: Use the structure of an expression to identify ways to rewrite it.</li> <li>CCSS.HSA.SSE.B.3: Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression.</li> <li>CCSS.HSF.BF.A.1.C: (+) Compose functions.</li> <li>CCSS.MP3 Construct viable arguments and critique the reasoning of others.</li> <li>CCSS.MP7 Look for and make use of structure.</li> </ul>	<ul> <li>identifying and using the algebraic properties.</li> <li>writing function rules from tables and word problems.</li> <li>determining the domain and range of various functions.</li> </ul>
Used in Content Area Standards	21 <sup>st</sup> Century Skills
	<ul><li>Technology Literacy</li><li>Communication</li></ul>

Stage 2 - Evidence		
Evaluative Criteria	Assessment Evidence	
	ASSESSMENT: Written Assessments or Projects	
	OTHER EVIDENCE: independent practice, classroom observations and discussions	

# Windham School District Curriculum Algebra 1 - Grade 8 Unit 2: Algebraic Expressions & Functions Exponential Expressions & Functions

	Stage 1 Desired Results	
ESTABLISHED GOALS:	Trai	nsfer
Students will continue their study of mathematics in the	Students will be able to independently use their lea	rning to
areas of algebraic expressions and functions. In this	• recognize the key characteristics of exponential	functions and its real-life applications
unit, students will gain a deeper understanding of	<ul> <li>use knowledge of exponential function in future</li> </ul>	e studies of logarithmic functions
exponential expressions and functions.	Мес	aning
<ul> <li>Content Standards:</li> <li>CCSS.HSA.SSE.A.2: Use the structure of an expression to identify ways to rewrite it.</li> <li>CCSS.HSA.SSE.B.3: Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by</li> </ul>	<ul> <li>ENDURING UNDERSTANDINGS</li> <li>Very large and small numbers can be represented efficiently using scientific notation</li> <li>Exponent properties can be proven through expansion.</li> <li>Exponential functions model real world phenomena.</li> </ul>	<ul> <li>ESSENTIAL QUESTIONS</li> <li>What are the rules of exponents and how are they applied to simplify expressions?</li> <li>How can exponents model real world data?</li> </ul>
the expression.	Acqu	isition
<ul> <li>CCSS.HSA.APR.A.1: Understand that polynomials form a system analogous to the integers; namely, they are closed under the operations of addition, subtraction, and multiplication; add, subtract, and multiply polynomials.</li> <li>CCSS.8A.IF.08.b: Use the properties of exponents to interpret expressions for exponential functions</li> <li>CCSS.MP1 Make sense of problems and persevere in solving them.</li> <li>CCSS.MP2 Reason abstractly and quantitatively.</li> <li>CCSS.MP7 Look for and make use of structure.</li> </ul>	<ul> <li>Students will understand</li> <li>properties of exponents can simplify monomial expressions.</li> <li>scientific notation can be used to write really large or small numbers.</li> <li>geometric applications of monomial expressions.</li> <li>negative exponents have a reciprocal relationship.</li> <li>exponential functions model real world phenomena.</li> </ul>	<ul> <li>Students will be skilled at</li> <li>using the rules of exponents to simplify monomials.</li> <li>applying geometric formulas to problems involving monomials.</li> <li>writing large or small numbers in scientific notation.</li> <li>performing operations on numbers expressed in scientific notation.</li> <li>graphing exponential functions.</li> </ul>

Used in Content Area Standards	21 <sup>st</sup> Century Skills
	Critical thinking
	Technology Literacy

Stage 2 - Evidence	
Evaluative Criteria	Assessment Evidence
	ASSESSMENT: Written Assessments or Projects
	OTHER EVIDENCE: independent practice, classroom observations and discussions

# Windham School District Curriculum Algebra 1 - Grade 8 Unit 3: Algebraic Equations Solving Equations & Inequalities

	Stage 1 Desired Results	
ESTABLISHED GOALS:	Tra	ansfer
Students will continue their study of mathematics in the areas of	Students will be able to independently use their learning to	
algebraic equations. In this unit, students will gain a deeper	• use their skills of writing and solving equa	tions as an effective problem solving technique.
understanding of solving equations and inequalities.	explain when an inequality should be writ	ten rather than an equation.
	Ме	aning
<ul> <li>Content Standards:.</li> <li>CCSS.HSA.CED.1. Create equations and inequalities in one variable and use them to solve problems.</li> <li>CCSS.HSF.A.REI.1. Understand solving equations as a process of reasoning and explain the reasoning. Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting</li> </ul>	<ul> <li>Operations performed on one side of an equation must be performed on the other side(s) in order to preserve the equality</li> <li>Solutions to inequalities represent a</li> </ul>	<ul> <li>How can an equation or inequality be manipulated to isolate a variable while preserving the value of the original</li> </ul>
from the assumption that the original equation has a	Δεαι	equation/inequality? uisition
<ul> <li>solution. Construct a viable argument to justify a solution method.</li> <li>CCSS.HSA.REI.3. Solve linear equations and inequalities in one variable, including equations with coefficients represented by letters.</li> <li>CCSS.HSA.CED.A.4: Rearrange formulas to highlight a quantity of interest, using the same reasoning as in solving equations. For example, rearrange Ohm's law V = IR to highlight resistance R</li> <li>CCSS.MP1 Make sense of problems and persevere in solving them.</li> </ul>	<ul> <li>Students will understand</li> <li>literal equations</li> <li>absolute value equations can have multiple solutions.</li> <li>percentages and proportions.</li> <li>connections between solving equations and solving inequalities.</li> </ul>	<ul> <li>Students will be skilled at</li> <li>writing and solving multi-step equations with rational coefficients.</li> <li>writing and solving multi-step one-variable inequalities and graphing them on a number line.</li> <li>solving and graphing compound inequalities.</li> <li>graphing inequalities on a number line.</li> <li>solving absolute value equations.</li> <li>solving literal equations.</li> </ul>

CCSS.MP3 Construct viable arguments and critique the	• writing and solving proportions, including
reasoning of others.	proportions with binomials in the
CCSS.MP4 Model with mathematics.	numerator or denominator.
CCSS.MP7 Look for and make use of structure.	<ul> <li>writing and solving application percent</li> </ul>
CCSS.MP8 Look for and express regularity in repeated	problems.
reasoning.	<ul> <li>solving absolute value inequalities.</li> </ul>
Used in Content Area Standards	21 <sup>st</sup> Century Skills
	Communication
	Critical thinking

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
OTHER EVIDENCE: independent practice, classroom observations and discussions		

## Windham School District Curriculum Algebra 1 - Grade 8

### **Unit 4: Functions - Linear Functions**

St	age 1 Desired Results	
ESTABLISHED GOALS: Students will continue their study of mathematics in the area of functions. In this unit, students will gain a deeper understanding of linear relationships.	Tran Students will be able to independently use th make connections between linear function use knowledge of linear functions as they	ons and real-life scenarios
<ul> <li>between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship.</li> <li>CCSS.HSF.IF.B.6: Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph.</li> <li>CCSS.HSF.IF.C.7.A: Graph linear and quadratic functions and show intercepts, maxima, and minima.</li> <li>CCSS.HSF.IF.C.8: Write a function defined by an expression in</li> </ul>	<ul> <li>ENDURING UNDERSTANDINGS</li> <li>Linear relationships have a constant rate of change</li> <li>Tables, graphs, and equations are all ways of representing functions and real</li> </ul>	<ul> <li>ESSENTIAL QUESTIONS</li> <li>How can graphs be used to solve linear equations?</li> <li>How do you determine the appropriate form of an equation for a line when given specific characteristics?</li> <li>What is the relationship between slope and rate of change and how can each be used to solve real world problems?</li> </ul>
	•	<ul> <li>isition</li> <li>Students will be skilled at</li> <li>calculating slope between two points</li> <li>determining the slope of a line, given an equation, table, or graph</li> <li>finding and determining intercepts.</li> <li>determining whether lines are parallel, perpendicular or neither.</li> <li>graphing linear equations.</li> </ul>

<ul> <li>CCSS.HSA.CED.A.2: Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.</li> <li>CCSS.HSA.REI.D.10: Understand that the graph of an equation in two variables is the set of all its solutions plotted in the coordinate plane, often forming a curve (which could be a line).</li> <li>CCSS.HSF.LE.A.2: Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or two input-output pairs (include reading these from a table).</li> <li>CCSS.HSF.LE.A.1.A: Prove that linear functions grow by equal differences over equal intervals, and that exponential functions grow by equal factors over equal intervals.</li> <li>CCSS.HSF.LE.A.1.B: Recognize situations in which one quantity changes at a constant rate per unit interval relative to another.</li> <li>CCSS.HSF.LE.B.5: Interpret the parameters in a linear or exponential function in terms of a context.</li> <li>CCSS.HSF.BF.A.2: Write arithmetic and geometric sequences both recursively and with an explicit formula, use them to model situations, and translate between the two forms.</li> <li>CCSS.MP7 Look for and make use of structure</li> </ul>	<ul> <li>writing linear equations in slope-intercept, standard and point-slope form.</li> <li>writing equations of a line passing through a given point, parallel/perpendicular to a given line.</li> <li>creating and interpreting linear equations from real world data.</li> <li>writing a rule given an arithmetic sequence.</li> </ul>
Used in Content Area Standards	21 <sup>st</sup> Century Skills
	<ul><li>Technology Literacy</li><li>Critical Thinking</li></ul>

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
	OTHER EVIDENCE: independent practice, classroom observations and discussions	

## Windham School District Curriculum Algebra 1 - Grade 8

### **Unit 5: Functions - Bivariate Data (Scatterplots)**

Stage 1 Desired Results		
ESTABLISHED GOALS:	Transfer	
Students will continue their study of mathematics in the	Students will be able to independently use their lea	arning to
area of functions. In this unit, students will gain a	<ul> <li>use their ability to analyze data in scatterplots t</li> </ul>	o analyze real-life data sets
deeper understanding of bivariate data.	<ul> <li>use their knowledge of scatterplots in future st</li> </ul>	udies of statistical data
	Me	aning
Content Standards:	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS
CCSS.HSS.ID.B.6: Represent data on two	• Scatter plots can model data and be used to	<ul> <li>How can mathematics be used to model and</li> </ul>
quantitative variables on a scatter plot, and	make predictions.	make predictions for real world phenomena?
describe how the variables are related.	Acqu	iisition
<ul> <li>CCSS.HSS.ID.B.6.c: Fit a linear function for a scatter plot that suggests a linear association.</li> <li>CCSS.HSF.S.ID.8 Interpreting linear models-Compute (using technology) and interpret the correlation coefficient of a linear fit.</li> <li>CCSS.MP4 Model with mathematics.</li> <li>CCSS.MP5 Use appropriate tools strategically</li> </ul>	<ul> <li>Students will understand</li> <li>scatter plots show relationships between two variables.</li> <li>some data can be modeled using a linear equation.</li> <li>equations of a line of best fit.</li> <li>Correlation of two variables</li> <li>not all data is linear.</li> </ul>	<ul> <li>Students will be skilled at</li> <li>representing bivariate data with scatterplots.</li> <li>interpreting scatterplots.</li> <li>calculating the line of best fit.</li> <li>using the line of best fit to find the starting point represented by the y-intercept; to describe what the slope means; and to find the values at a particular point including outside the given graph.</li> <li>determining if there is a correlation between bivariate data.</li> <li>making predictions based on the line of best fit.</li> </ul>
Used in Content Area Standards		21 <sup>st</sup> Century Skills
		Technology Literacy
		Critical thinking

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
OTHER EVIDENCE: independent practice, classroom observations and discussions		

## Windham School District Curriculum Algebra 1 - Grade 8

## **Unit 6: Algebraic Equations - Linear Systems**

ESTABLISHED GOALS:	age 1 Desired Results Trans	fer
Students will continue their study of mathematics in the area of algebraic equations. In this unit, students will gain a deeper	Students will be able to independently use the • extend their knowledge of linear systems to	ir learning to
understanding of linear systems.	Recognize systems of linear equations as a	valuable problem solving tool
<ul> <li>Content Standards:</li> <li>CCSS.HSF.A.CED.2: Create equations that describe numbers or relationships- Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.</li> <li>CCSS.HSA.CED.A.3: Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context.</li> <li>CCSS.HSA.REI.C.5: Prove that, given a system of two equations in</li> </ul>	<ul> <li>solving.</li> <li>Systems of equations with two unknowns can be used to solve real world problems.</li> </ul>	<ul> <li>ing</li> <li>ESSENTIAL QUESTIONS</li> <li>How do you solve real world problems using systems of equations?</li> <li>Which method is best and why?</li> <li>How can systems of equations be used to represent situations and solve problems?</li> <li>What does the number of solutions (none, one or infinite) of a system of linear equations represent?</li> </ul>
<ul> <li>two variables, replacing one equation by the sum of that equation and a multiple of the other produces a system with the same solutions. CCSS.HSA.REI.C.6: Solve systems of linear equations exactly and approximately (e.g., with graphs), focusing on pairs of linear equations in two variables.</li> <li>CCSS.HSA.REI.10. Represent and solve equations and inequalities graphically. Understand that the graph of an equation in two variables is the set of all its solutions plotted in the coordinate plane often forming a curve (which could be a line).</li> </ul>	<ul> <li>Acquisi</li> <li>Students will understand</li> <li>linear systems as a model</li> <li>Graphical and algebraic representations of linear systems</li> <li>linear inequalities and their graphical representation.</li> </ul>	Students will be skilled at • writing and solving linear systems by

<ul> <li>CCSS.HSA.REI.D.12: Graph the solutions to a linear inequality in two variables as a half-plane (excluding the boundary in the case of a strict inequality), and graph the solution set to a system of linear inequalities in two variables as the intersection of the corresponding half-planes.</li> <li>CCSS.MP1 Make sense of problems and persevere in solving</li> </ul>	<ul> <li>graphing systems of linear inequalities on a coordinate plane.</li> <li>creating and interpreting linear inequalities in one variable.</li> <li>modeling and solving real world situations with systems of equations.</li> </ul>
<ul> <li>them.</li> <li>CCSS.MP5 Use appropriate tools strategically.</li> <li>CCSS.MP6 Attend to precision.</li> <li>CCSS.MP7 Look for and make use of structure.</li> <li>CCSS.MP8 Look for and express regularity in repeated reasoning.</li> </ul>	
Used in Content Area Standards	21 <sup>st</sup> Century Skills
	Critical thinking
	Technology Literacy

Stage 2 - Evidence		
Evaluative Criteria Assessment Evidence		
ASSESSMENT: Written Assessments or Projects		
OTHER EVIDENCE: independent practice, classroom observations and discussions		

## Windham School District Curriculum Algebra 1 - Grade 8 Unit 7: Algebraic Expressions & Equations Polynomials & Quadratics

Stage 1 Desired Results			
ESTABLISHED GOALS:	Transfer		
Students will continue their study of mathematics in the	Students will be able to independently use their learning to		
area of algebraic expressions and equations. In this unit,	• connect their understanding of properties of po	lynomials to simplify complex numbers and radical	
students will gain a deeper understanding of simplifying			
polynomials and factoring and solving quadratics.	• use their understanding of solving quadratic equ	uations when solving higher order equations	
	Mea	ining	
Content Standards:	ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS	
CCSS.HSA.SSE.B.3: Choose and produce an	Mathematical properties extend to simplify	• What characteristics of a polynomial determine	
equivalent form of an expression to reveal and	polynomials.	how to factor it completely?	
explain properties of the quantity represented by	Acqu	isition	
<ul> <li>the expression.</li> <li>CCSS.HSA.SSE.B.3.a: Factor a quadratic expression to reveal the zeros of the function it defines.</li> <li>CCSS.HSA.APR.A.1: Understand that polynomials form a system analogous to the integers; namely, they are closed under the operations of addition, subtraction, and multiplication; add, subtract, and multiply polynomials.</li> <li>CCSS.HSA.REI.B.4: Solve quadratic equations in one variable</li> <li>CCSS.MP1 Make sense of problems and persevere in solving them.</li> <li>CCSS.MP2 Reason abstractly and quantitatively.</li> <li>CCSS.MP7 Look for and make use of structure.</li> </ul>	<ul> <li>Students will understand</li> <li>the degree and standard form of a polynomial</li> <li>factoring polynomials: greatest common factor, difference of squares, trinomial factoring</li> <li>quadratic equations.</li> </ul>	<ul><li>Students will be skilled at</li><li>simplifying polynomial expressions.</li></ul>	

Used in Content Area Standards	21 <sup>st</sup> Century Skills
	Communication
	Critical thinking

Stage 2 - Evidence		
Evaluative Criteria	Assessment Evidence	
	ASSESSMENT: Written Assessments or Projects	
	OTHER EVIDENCE: independent practice, classroom observations and discussions	

# Windham School District Curriculum Algebra 1 - Grade 8 Unit 8: Algebraic Expressions & Equations Radical Expressions & Equations

Stage 1 Desired Results				
ESTABLISHED GOALS: Students will continue their study of mathematics in the area of algebraic expressions and equations. In this unit, students will gain a deeper understanding of radical expressions and equations.	Transfer         Students will be able to independently use their learning to         • extend their understanding radical expressions to simplify expressions with rational roots.         • use their knowledge of solving radical equations to solve real world scenarios.         • Meaning			
<ul> <li>Content Standards:</li> <li>CCSS.HSA.SSE.A.2: Use the structure of an expression to identify ways to rewrite it.</li> <li>CCSS.HSA.SSE.B.3: Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression.</li> <li>CCSS.HSG.SRT.C.8: Use trigonometric ratios and the Pythagorean Theorem to solve right triangles in applied problems.</li> <li>CCSS.HSN.RN.A.2: Rewrite expressions involving radicals and rational exponents using the properties of exponents.</li> <li>CCSS.HSA.REI.A.2: Solve simple rational and radical equations in one variable, and give examples showing how extraneous solutions may arise.</li> <li>CCSS.MP7 Look for and make use of structure</li> <li>CCSS.MP8 Look for and express regularity in repeated reasoning.</li> </ul>	<ul> <li>ENDURING UNDERSTANDINGS</li> <li>Radicals represent numbers.</li> <li>In some operations, radicals mimic variables.</li> </ul>	<ul> <li>ESSENTIAL QUESTIONS</li> <li>How can finding roots help us solve problems?</li> </ul>		
	Acq Students will understand radical expressions. Pythagorean theorem equivalent representations of radical expressions. radical equations. extraneous solutions in radical equations.	<ul> <li>Students will be skilled at</li> <li>simplifying radical expressions.</li> <li>adding, subtracting, multiplying, and dividing radicals.</li> <li>solving problems involving the Pythagorean theorem.</li> <li>solving radical equations.</li> <li>determining extraneous solutions when solving radical equations.</li> </ul>		
Used in Content Area Standards		21 <sup>st</sup> Century Skills		
		Communication		

Stage 2 - Evidence		
Evaluative Criteria	Assessment Evidence	
	ASSESSMENT: Written Assessments or Projects	
	OTHER EVIDENCE: independent practice, classroom observations and discussions	